

# Tutorial

## Valuing flexibility in telecom infrastructure projects using real options thinking

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Networks 2012  
Tuesday Oct 16<sup>th</sup>, Rome, Italy

*Should I start  
deploying a  
wireless network?*

*Is it worth paying for  
a wireless license?*



# Deployment of a wireless network

Example case of investment problem with inherent flexibility

# LTE deployment

## Some background

- Peak rates
  - 300 Mbps downlink
  - 75 Mbps uplink
- Scalable carrier bandwidths
  - From 1.4 MHz to 20 MHz
- FDD and TDD

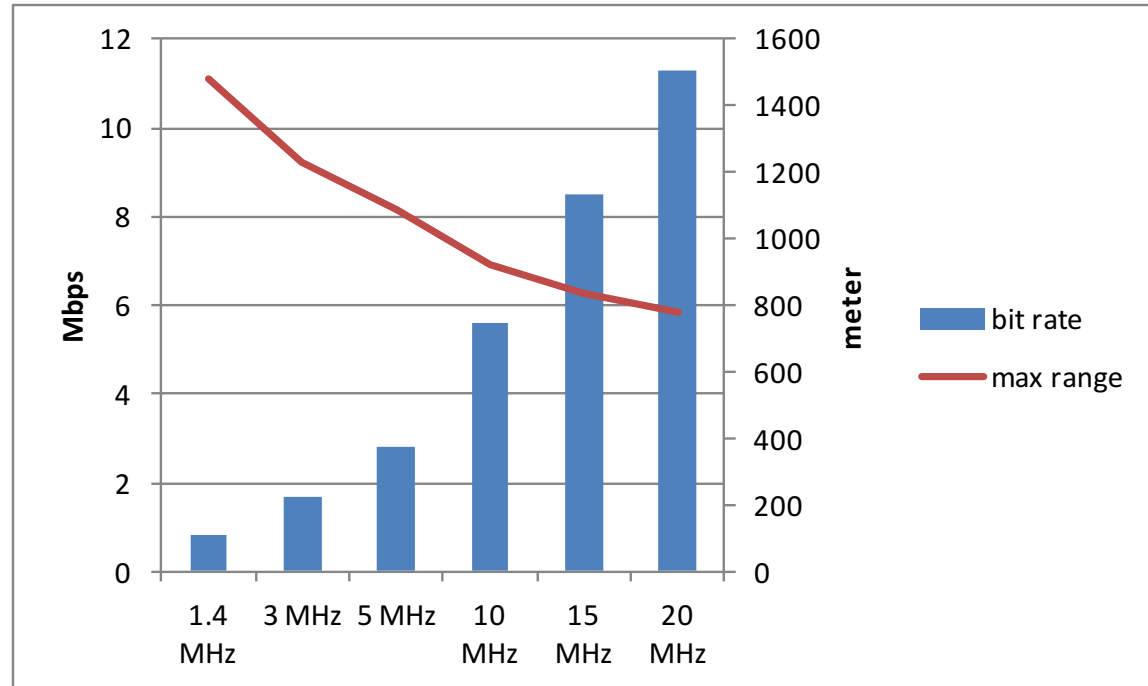


# LTE technology

## Features

### Different bandwidths

- Higher bandwidth
  - Higher bit rate
  - Lower range

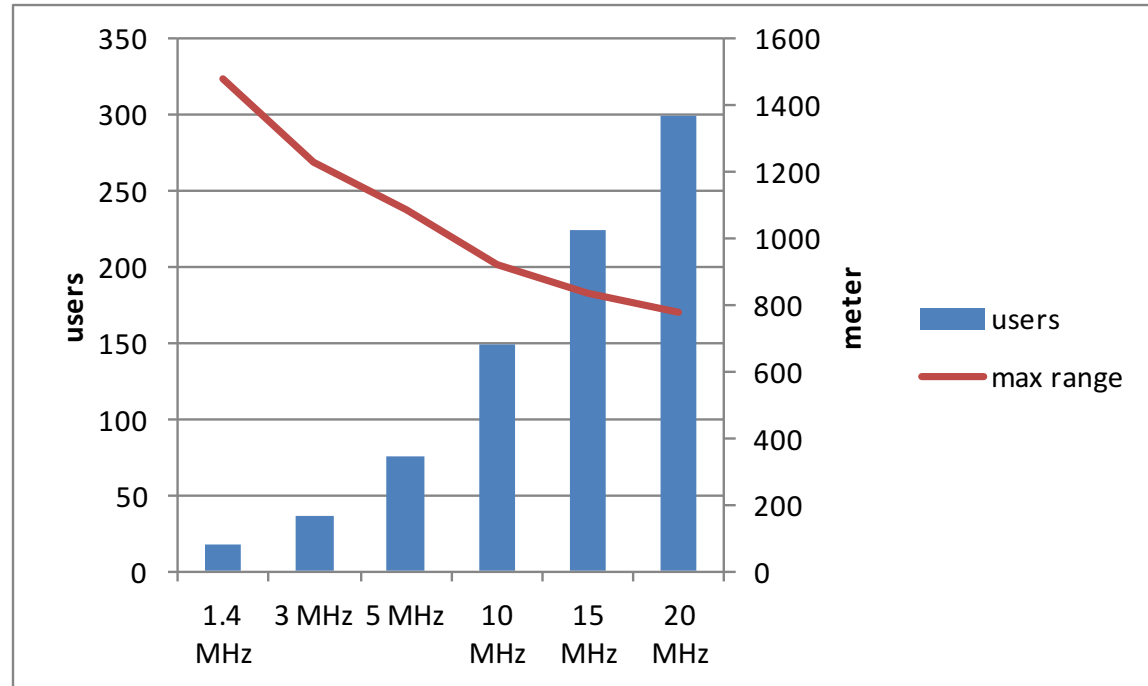


# LTE technology

## Features

### Different bandwidths

- Higher bandwidth
  - Extra users
  - Lower range



# Case study

## Deployment of LTE

- In 20 MHz band
- Offering 11.3 Mbps (in DL)
- BS reach = 780 m

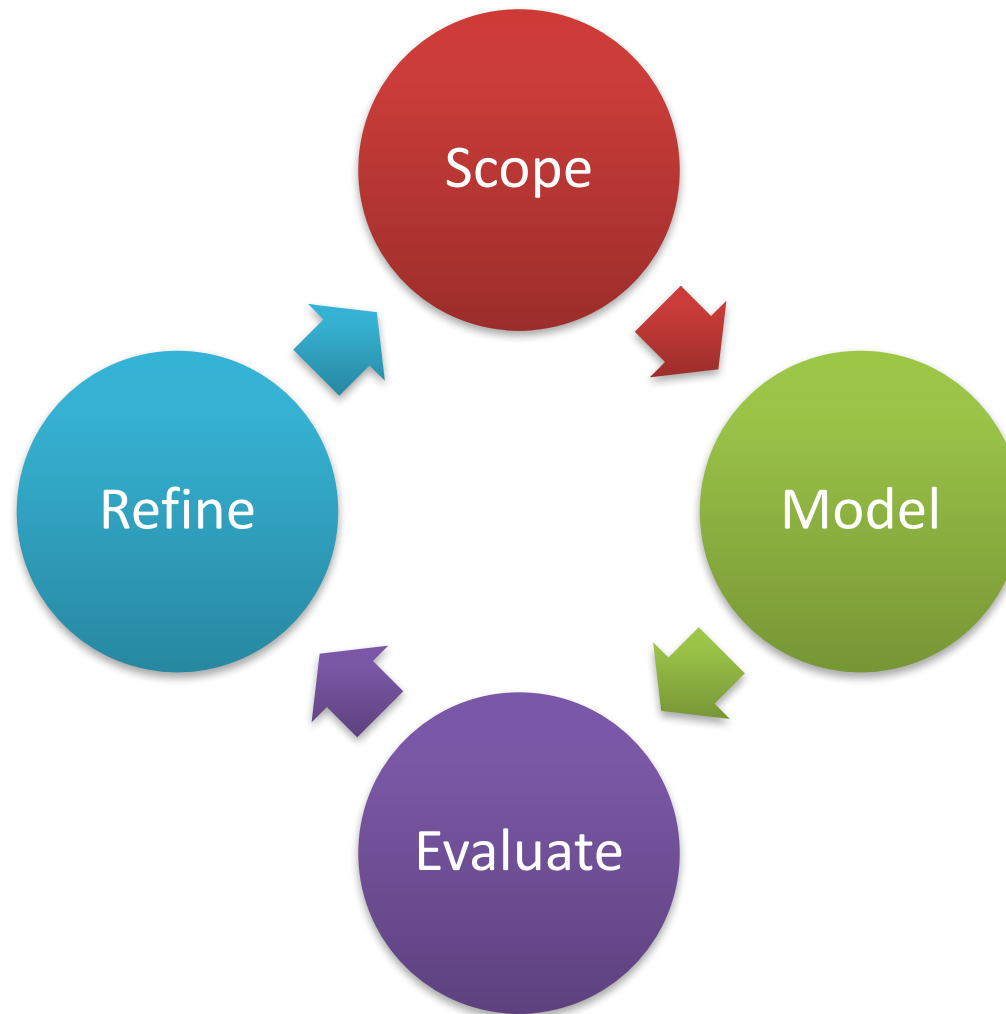
## in Ghent

- 243.366 inhabitants
- 156.2 km<sup>2</sup>



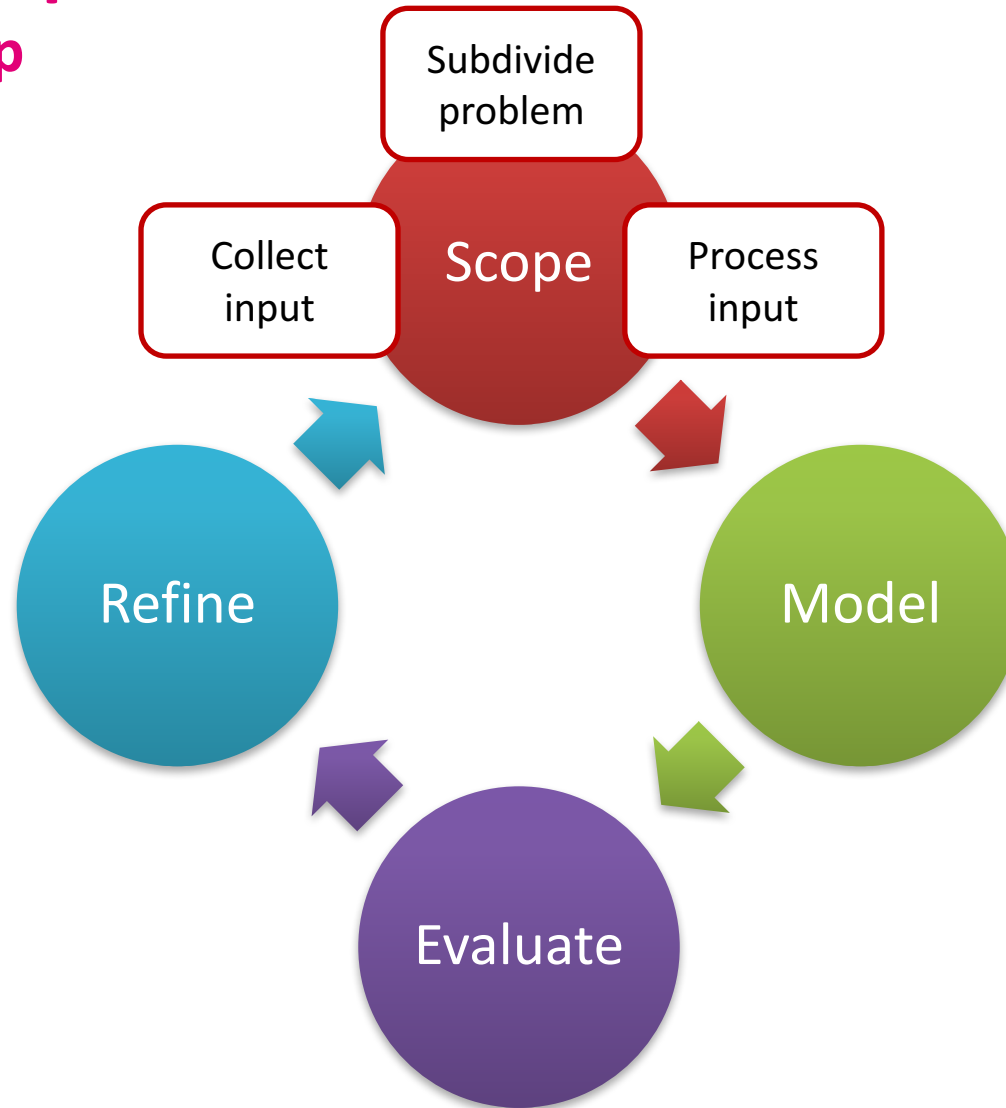
# Techno-economic methodology

analysis of an investment decision in 4 steps





# Scope the problem as a first step



# Collect input

for the investment problem at hand

## Area input

- 243.366 inhabitants
- 156.2 km<sup>2</sup>

## Technology input

- In 20 MHz band
- Offering 11.3 Mbps (in DL)
- BS reach = 780 m

# Cost input for wireless technology

Parameter	Cost	unit	Reference
License cost	€2	Per inhabitant	[1]
Base station	€50.000	Per BS	[2]
Installation cost	€4.000	Per BS	[2]
Rent location	€3.000	Per BS	[2]
Maintenance	€5.000	Per BS	[2]

[1] BIPT. (2012). PRESS RELEASE BIPT makes the results of the 4G auction public, (November 2011), 1–2. Retrieved from <http://www.bipt.be/ShowDoc.aspx?objectID=3639&lang=en>

[2] J.Verstuyft (2011) Selection and evaluation of the optimal wireless technology for a mobile network operator

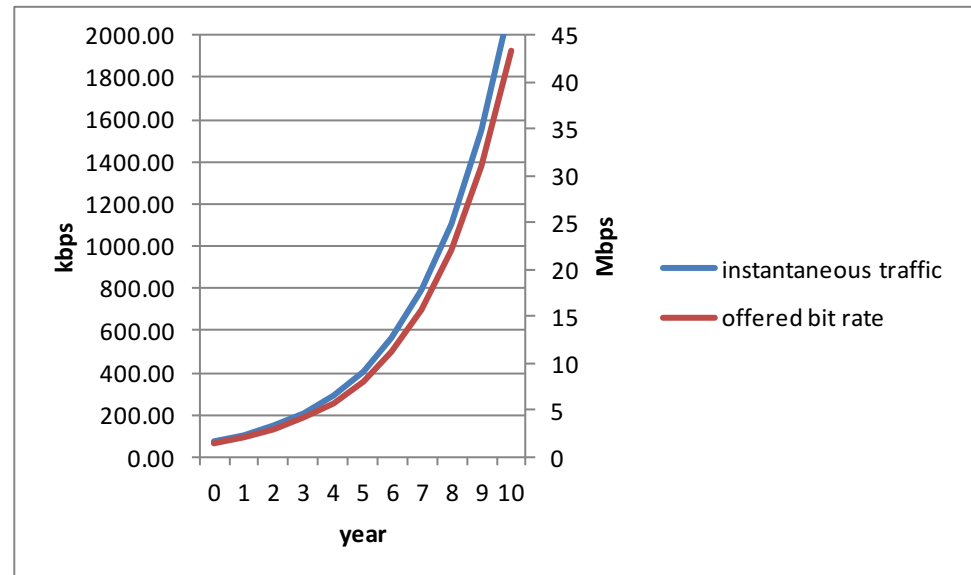
# Traffic model

indicates how many traffic we expect on the network

Initial bit rate offered	1,5 Mbps
Overbooking ratio	1:20
Expected traffic growth	40%

## Implications:

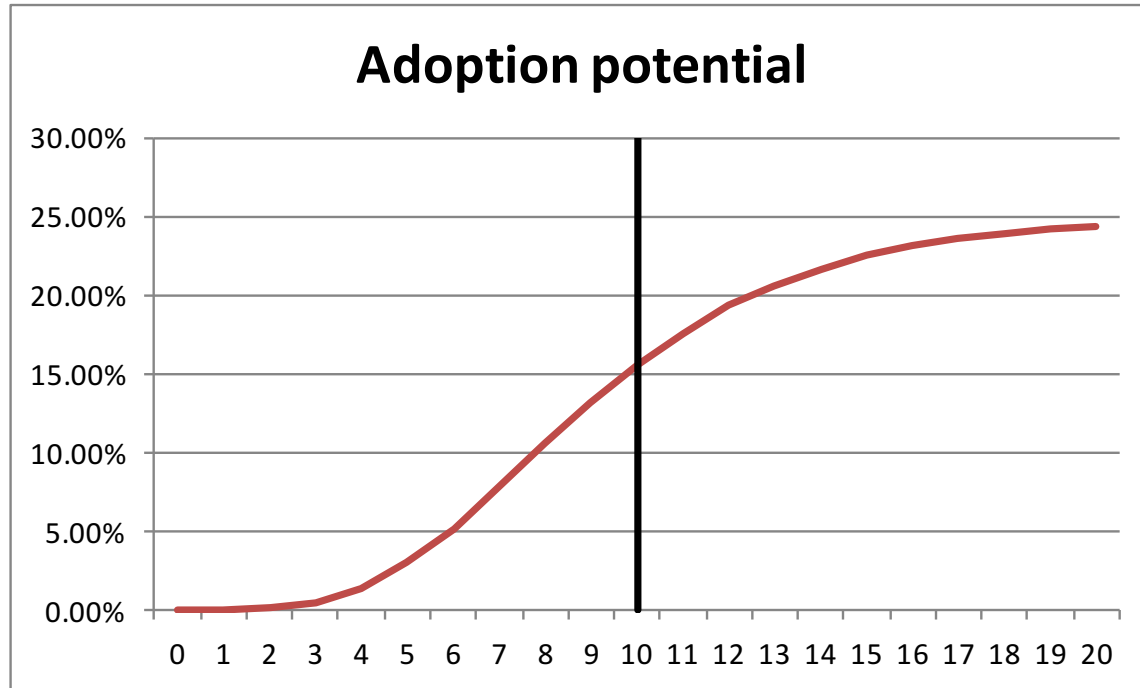
- Traffic growth will result in extra BS
- Fiber lease cost will grow with traffic



# Customer uptake

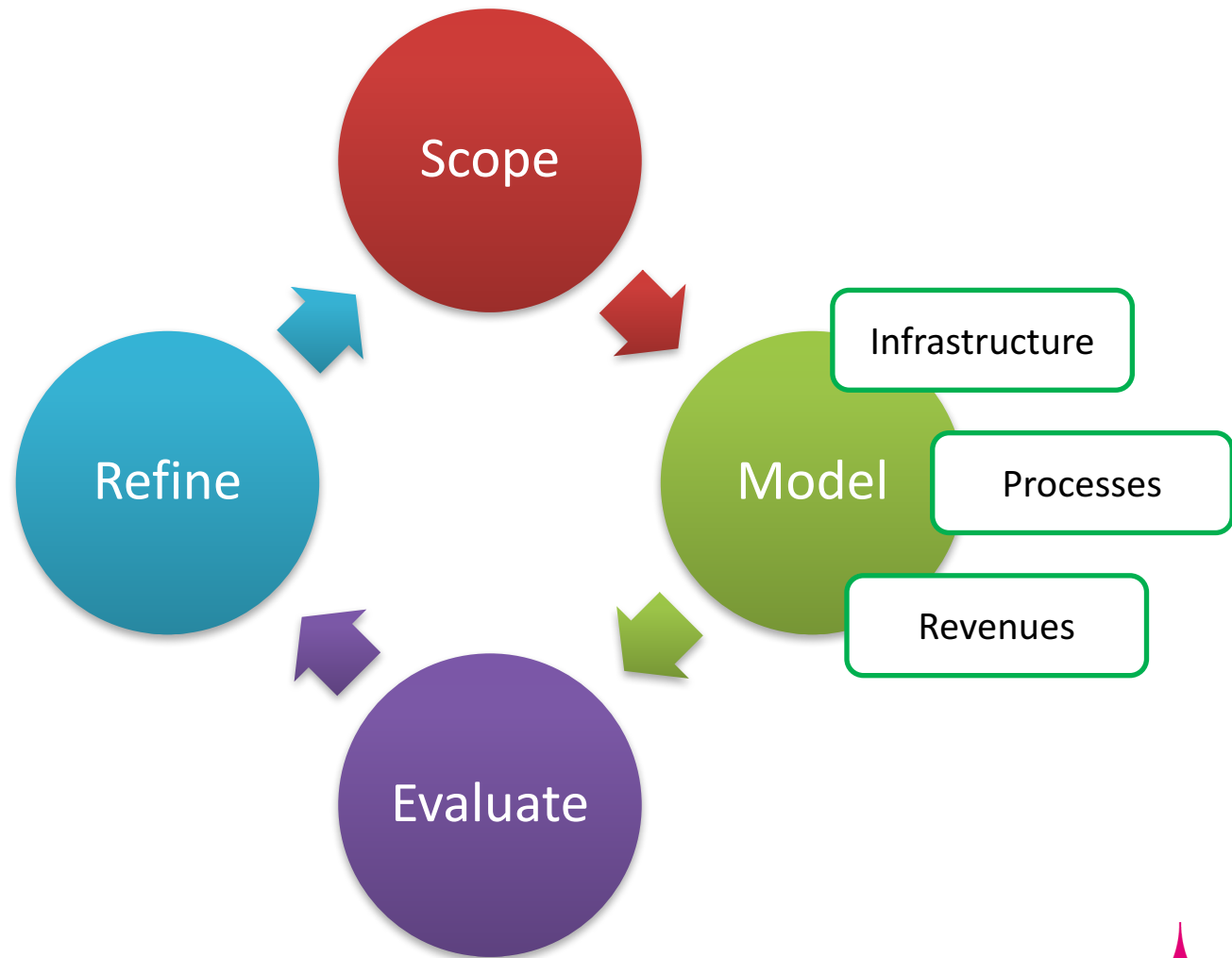
is modeled by Gompertz S-shaped adoption

ARPU - €20 per month



[3] [http://afr.com/p/business/technology/uptake\\_hanging\\_on\\_the\\_telephones\\_HhQoW6hT7Yy4sAnL6iOqWN](http://afr.com/p/business/technology/uptake_hanging_on_the_telephones_HhQoW6hT7Yy4sAnL6iOqWN)

# Model costs and revenues as a second step

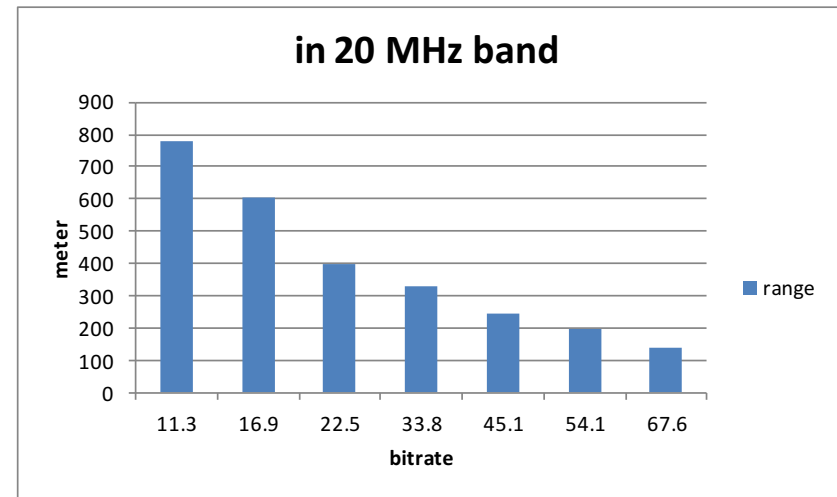
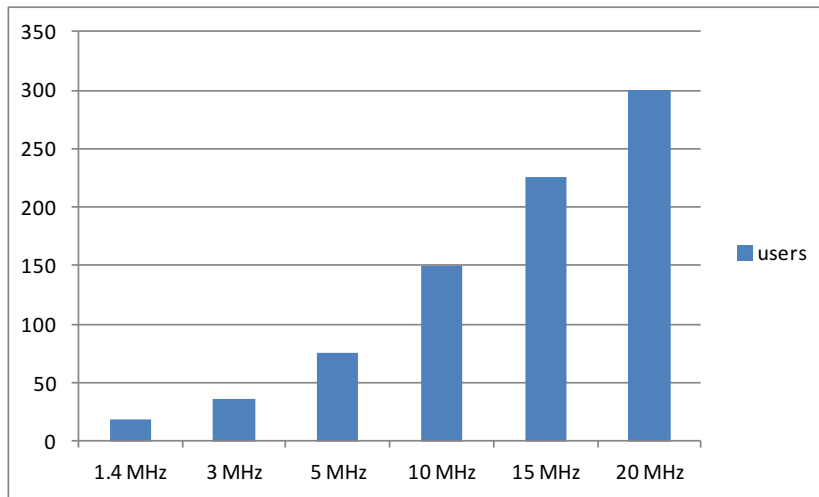


# Base station dimensioning

indicates # base stations depending on areas and # customers

Customer dependent

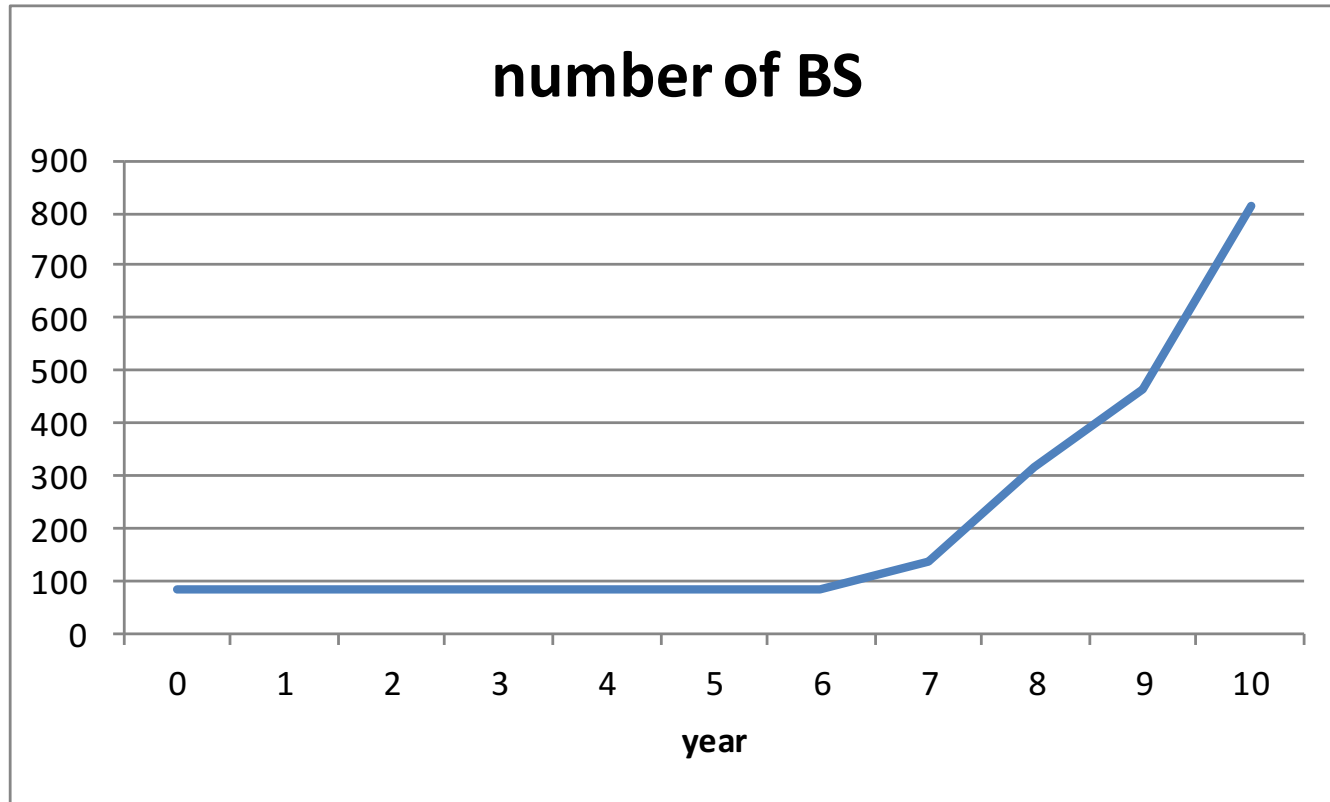
Area dependent



$$\# BS = \text{MAX} \left( \frac{\text{area}}{\text{range}_{BS}}, \frac{\text{customers}}{\text{customers}/BS} \right)$$

# Base station dimensioning

results in total number of base stations installed



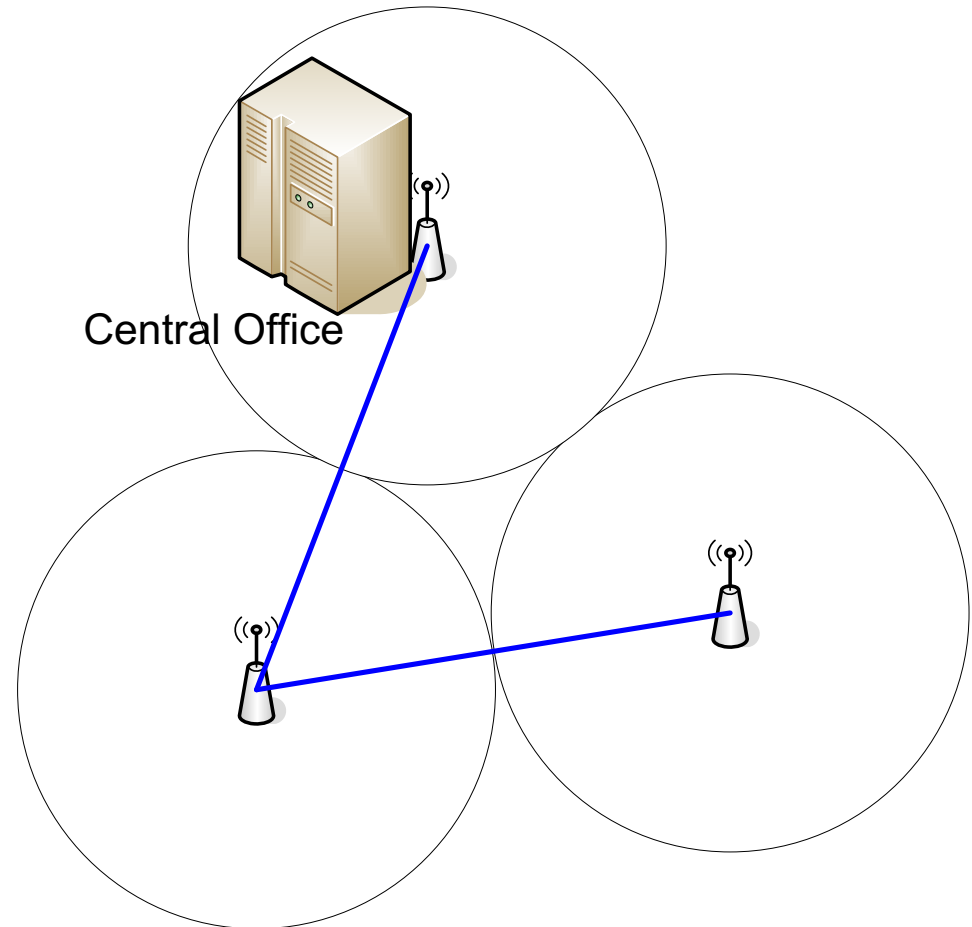


# Backhaul dimensioning

results in required backhaul fiber length

$$(\# BS - 1) * range_{BS} * 2$$

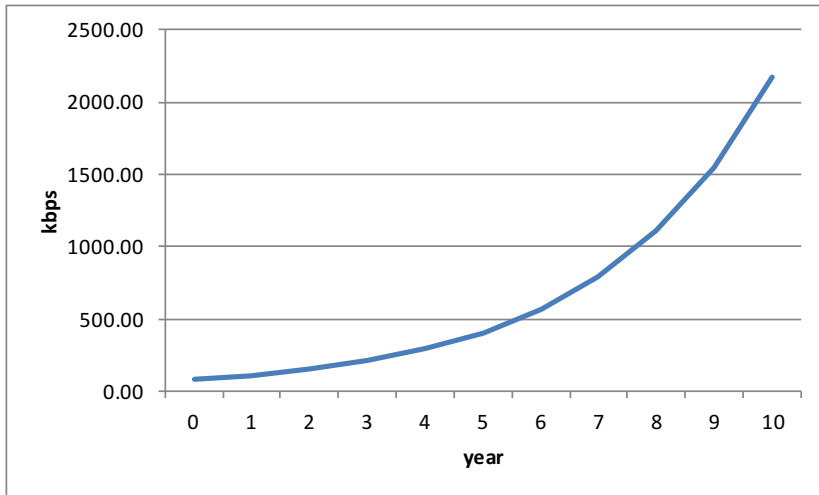
- CO located at BS
- Overhead length
- Lease cost
  - €1/Gbps/m/year



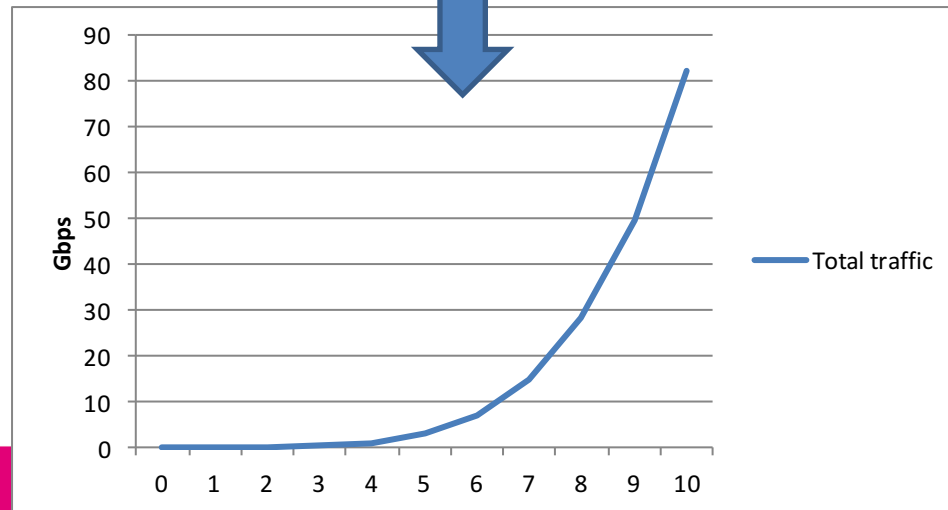
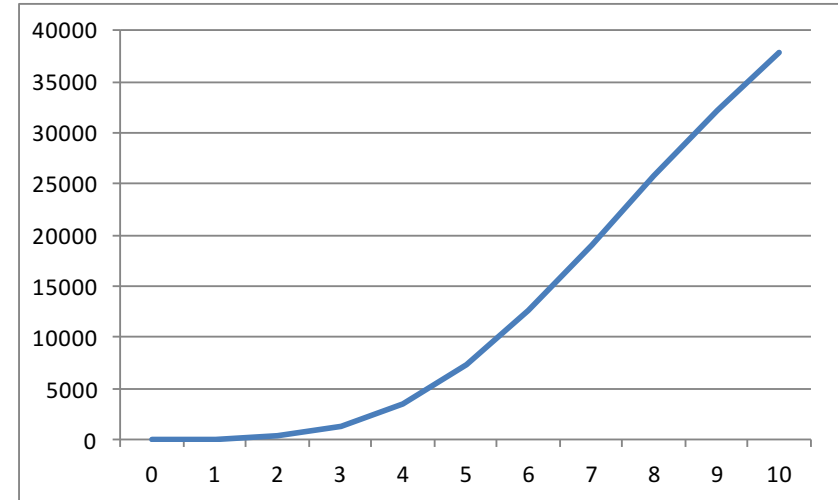
# Backhaul traffic

indicates required capacity over backhaul connections

Instantaneous traffic

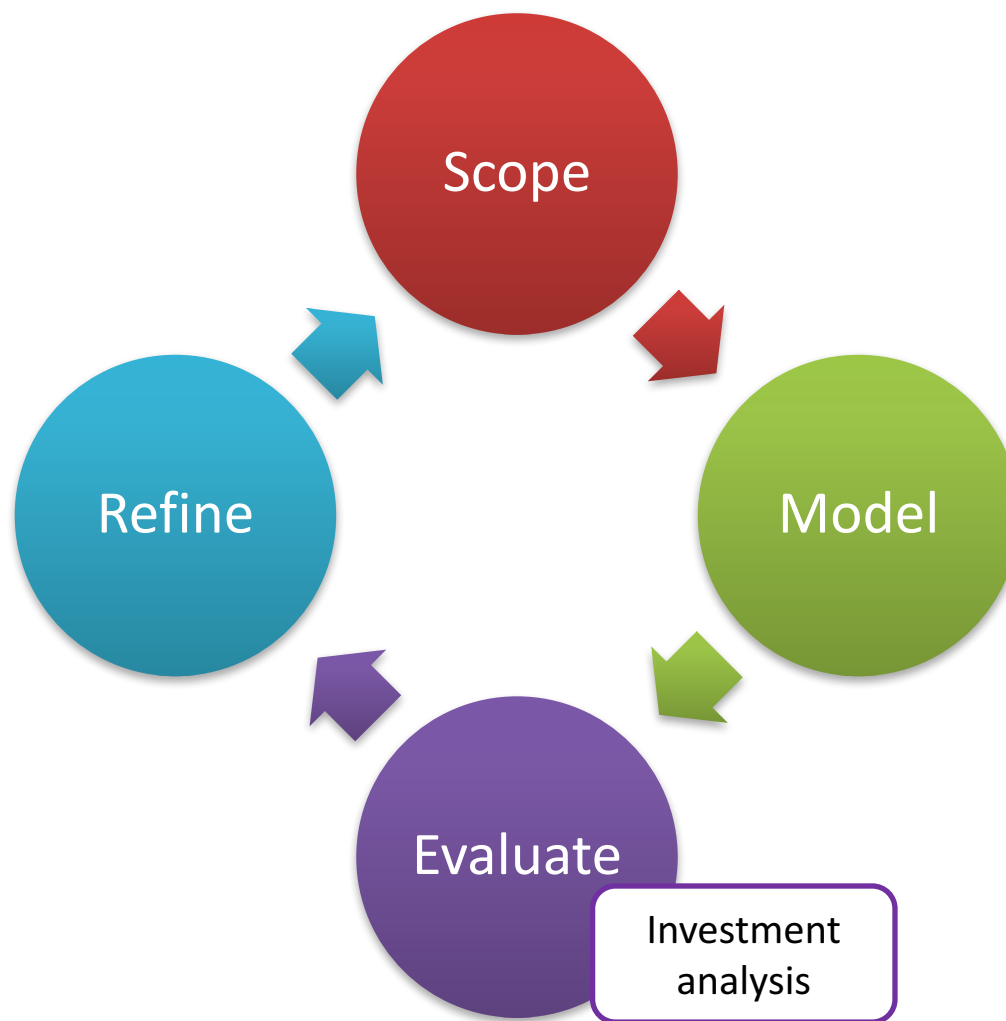


# customers



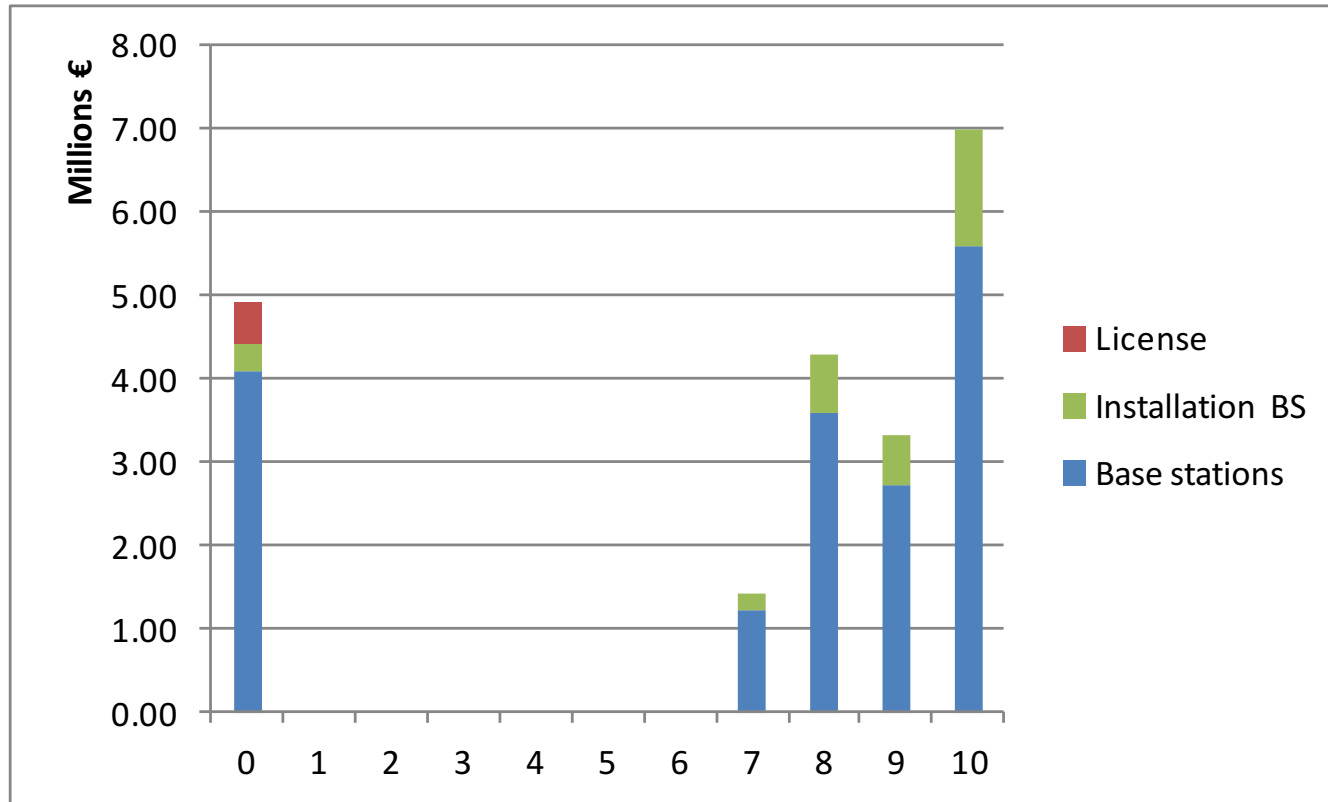
# Evaluate cost versus revenues

as a third step



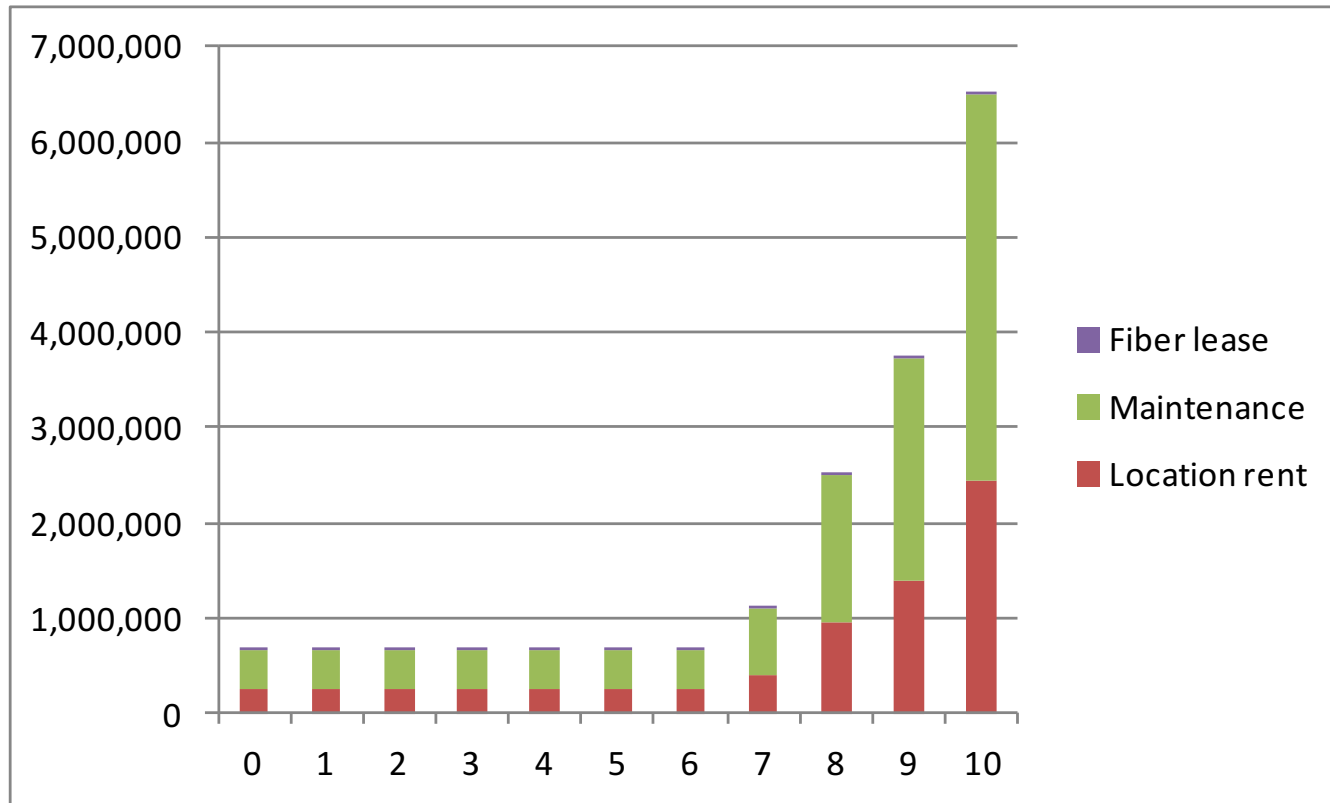
# Capital expenditures

indicate depreciable investment cost



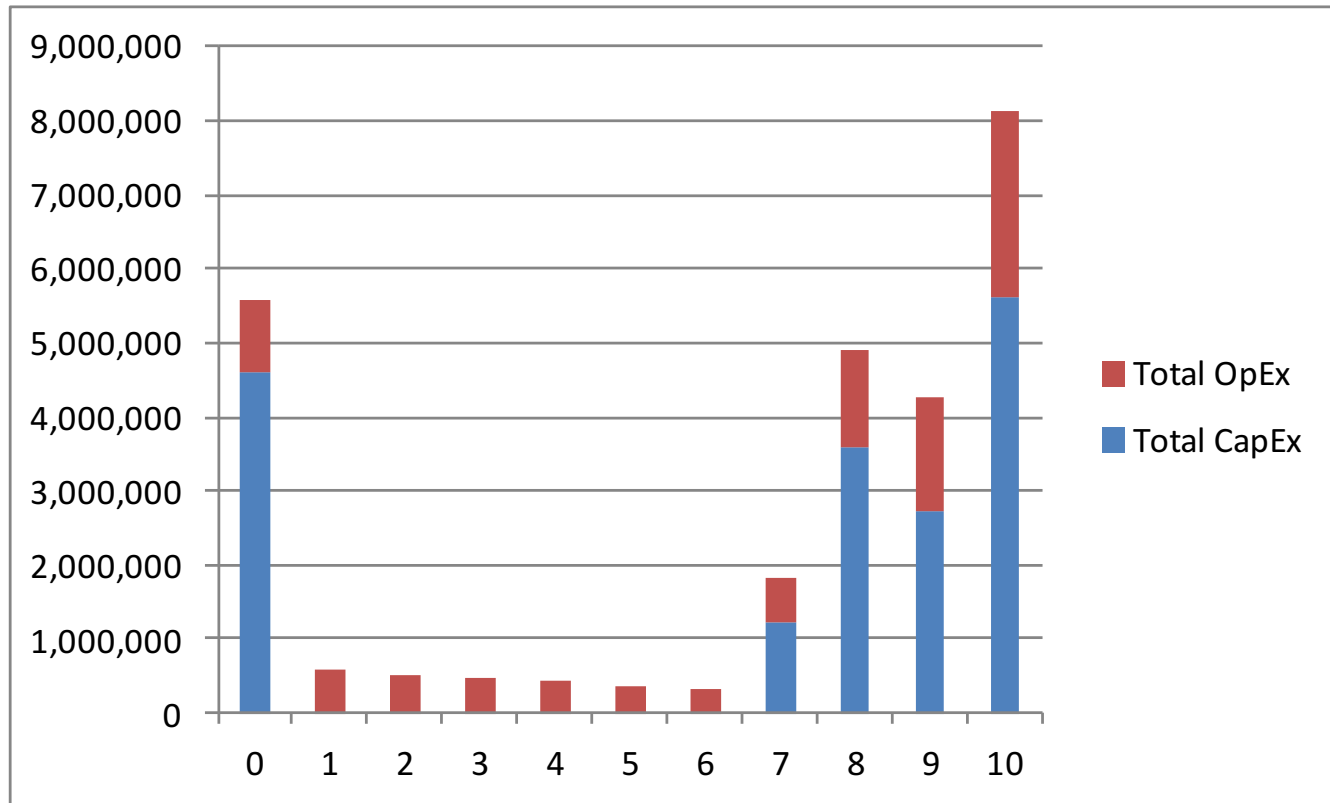
# Operational expenditures

indicate recurring costs



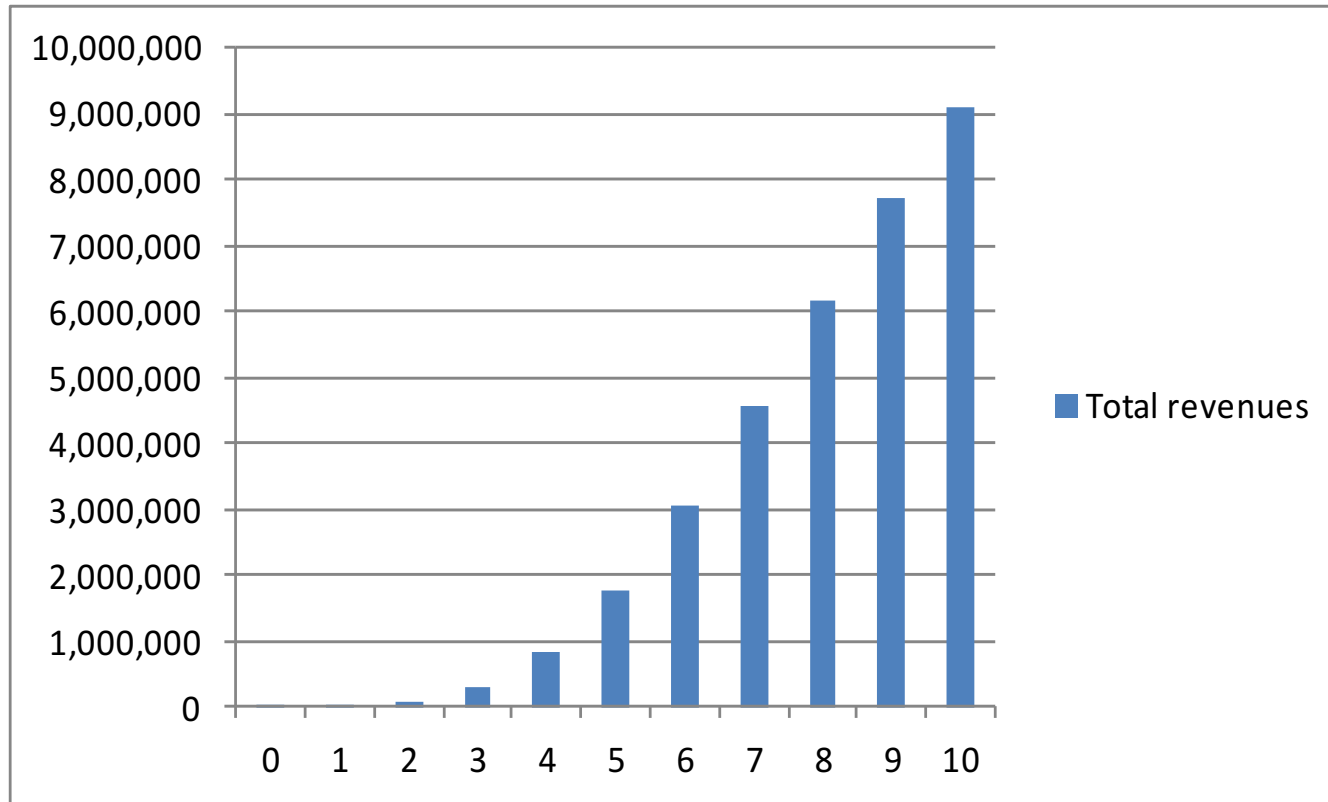
# Total cost

## sum CapEx and OpEx



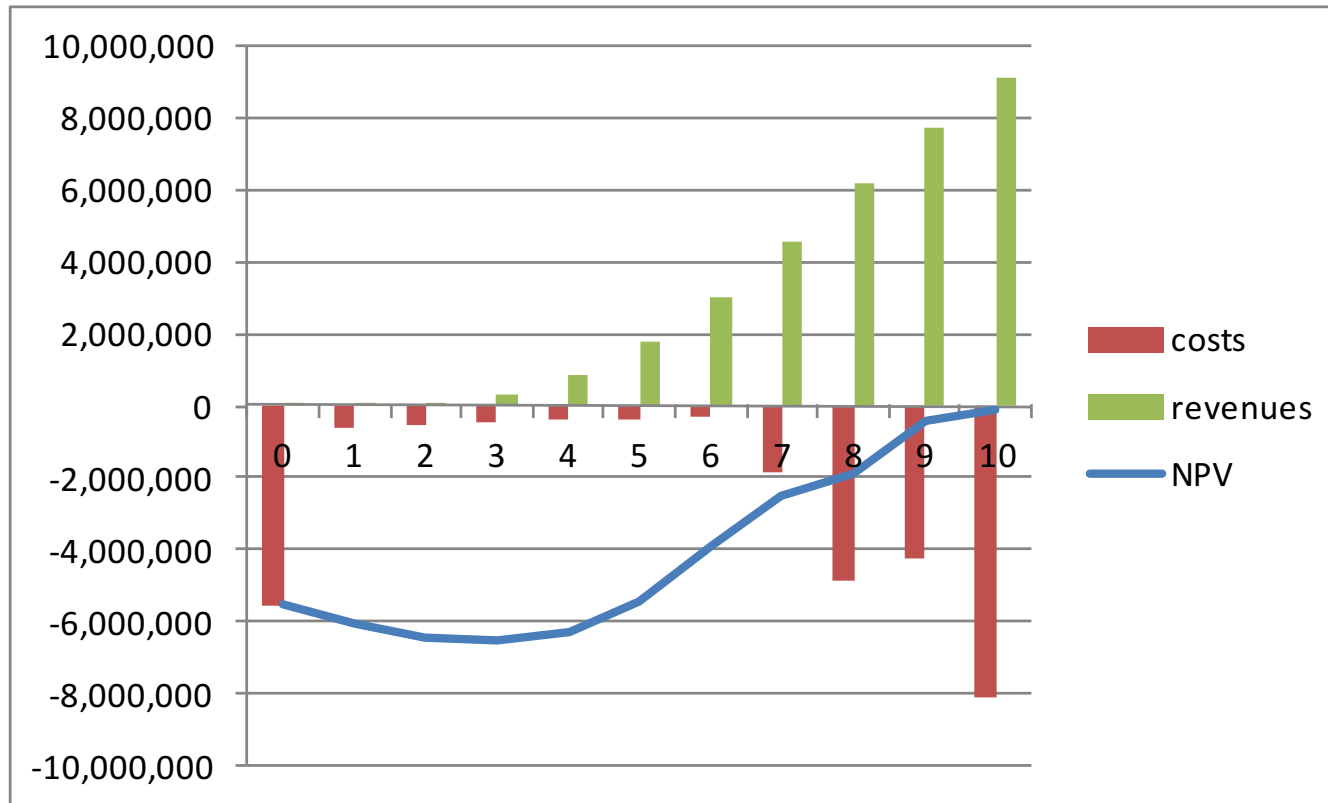
# Revenues

are related to the number of customers



# NPV analysis

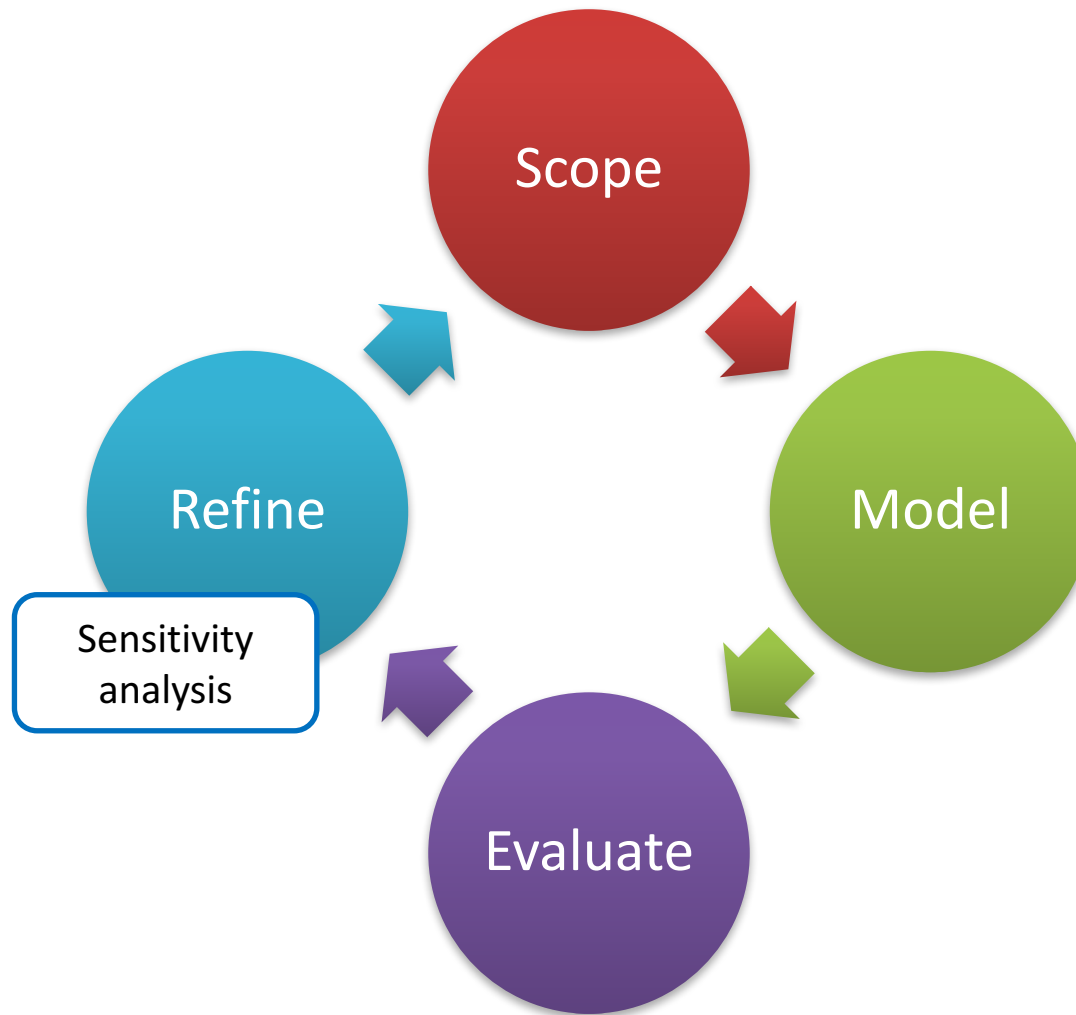
sums discounted cash flows



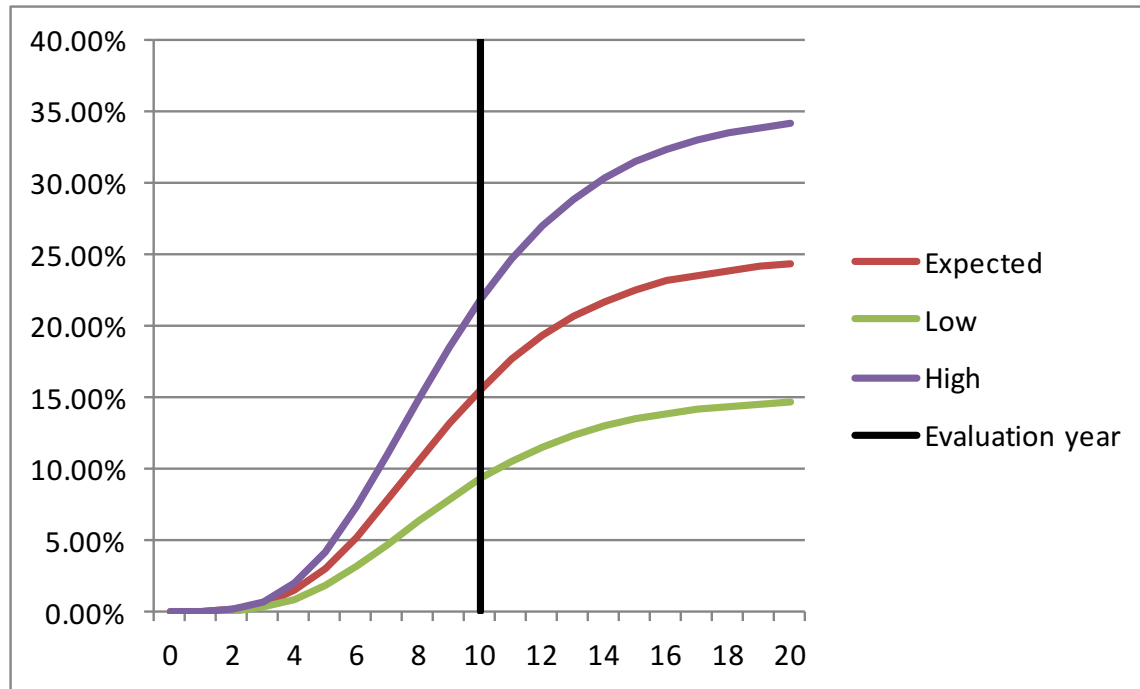
NPV at year 10 = €-84.999



# Refine the analysis as a fourth step



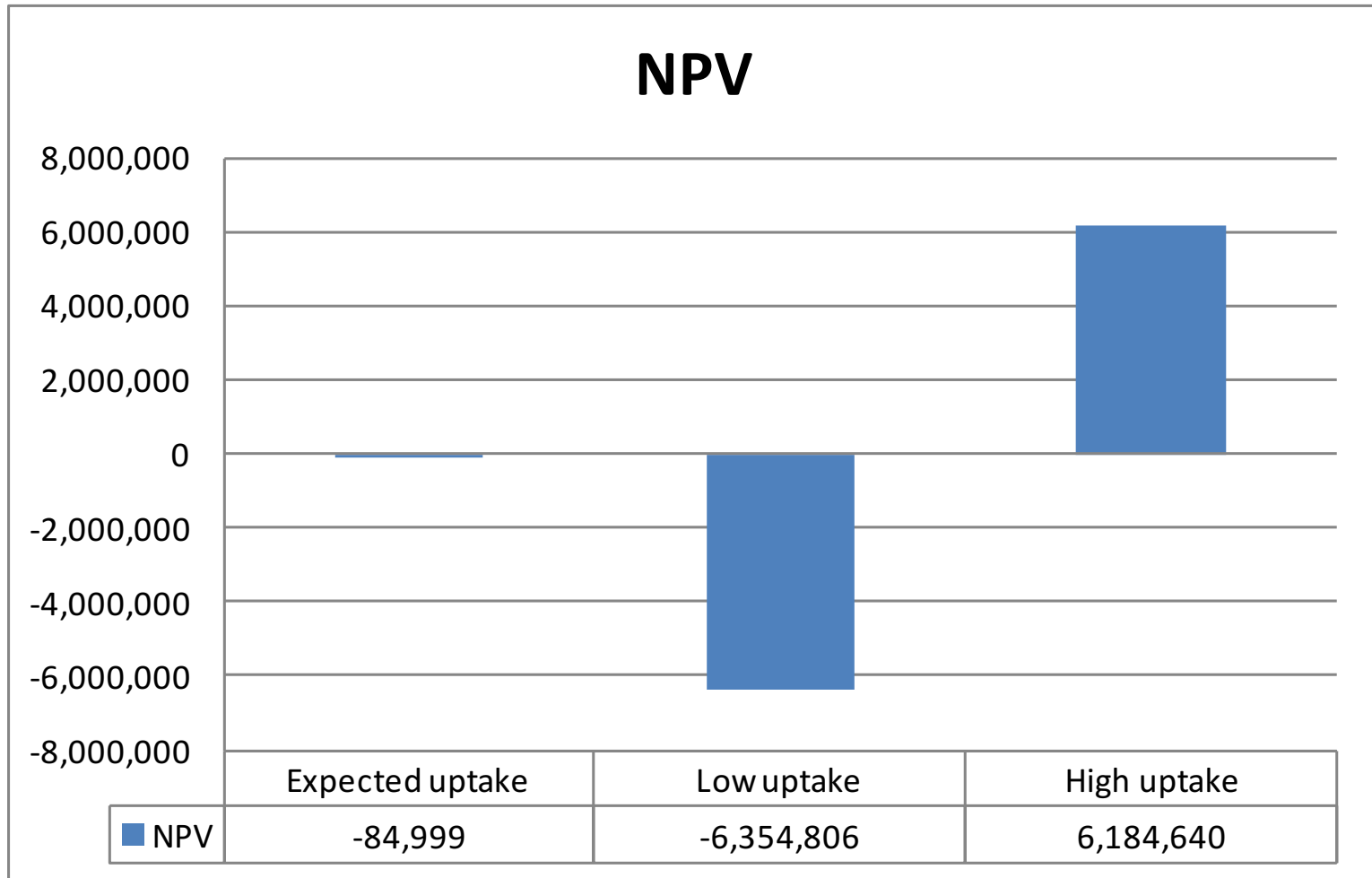
# Impact of uncertainty on expected market potential



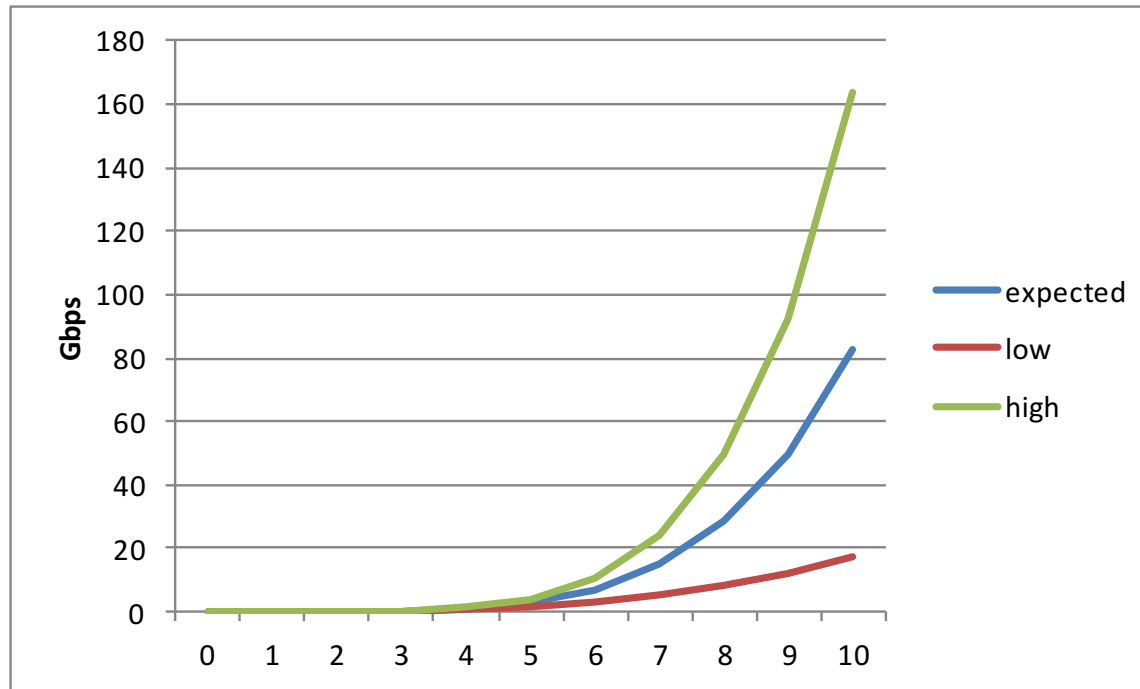
Impact on

- # BS
- Traffic → fiber lease cost

# Result can be very different under different uptake assumptions



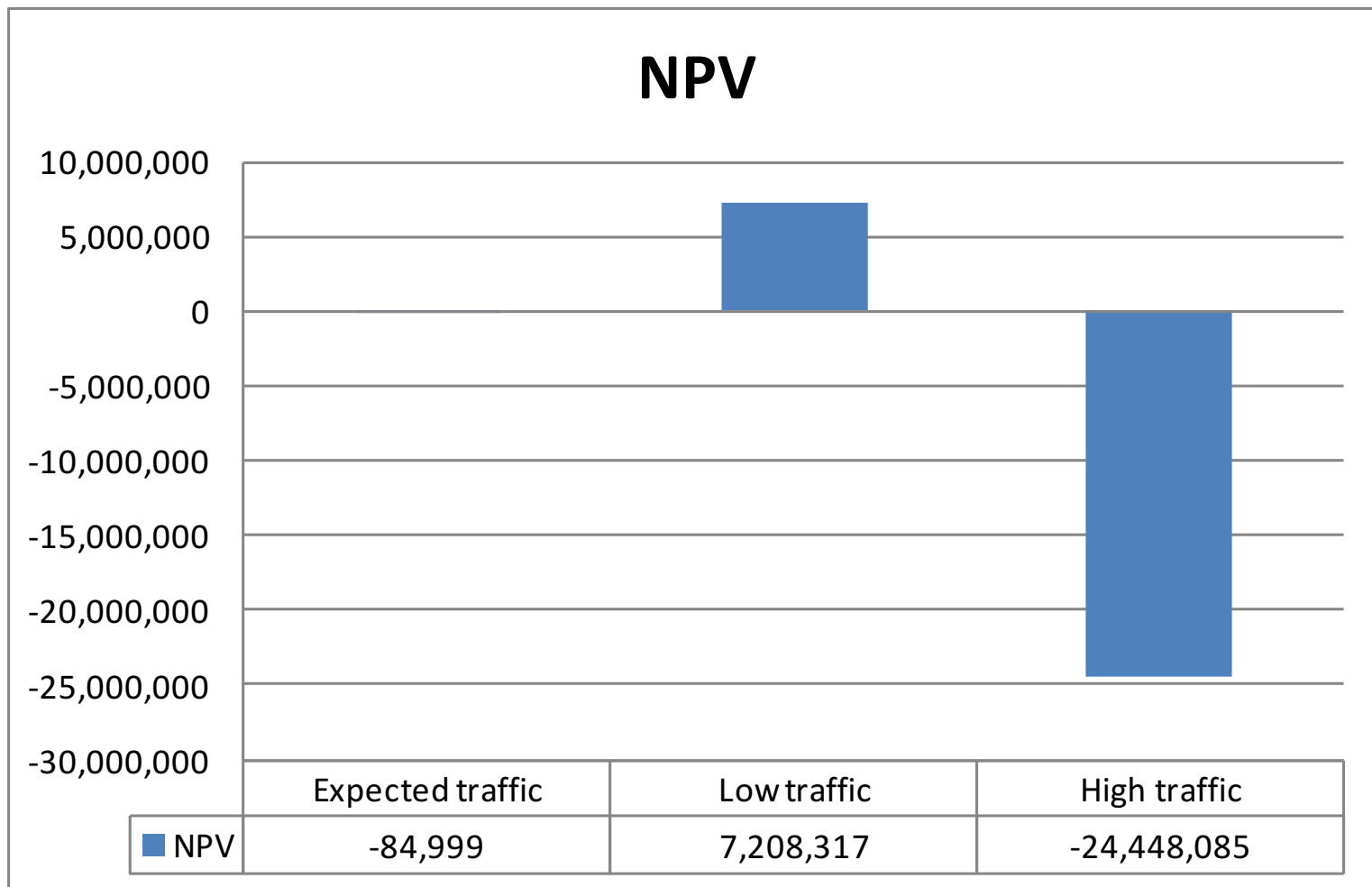
# Impact of uncertainty on expected traffic growth



Impact on

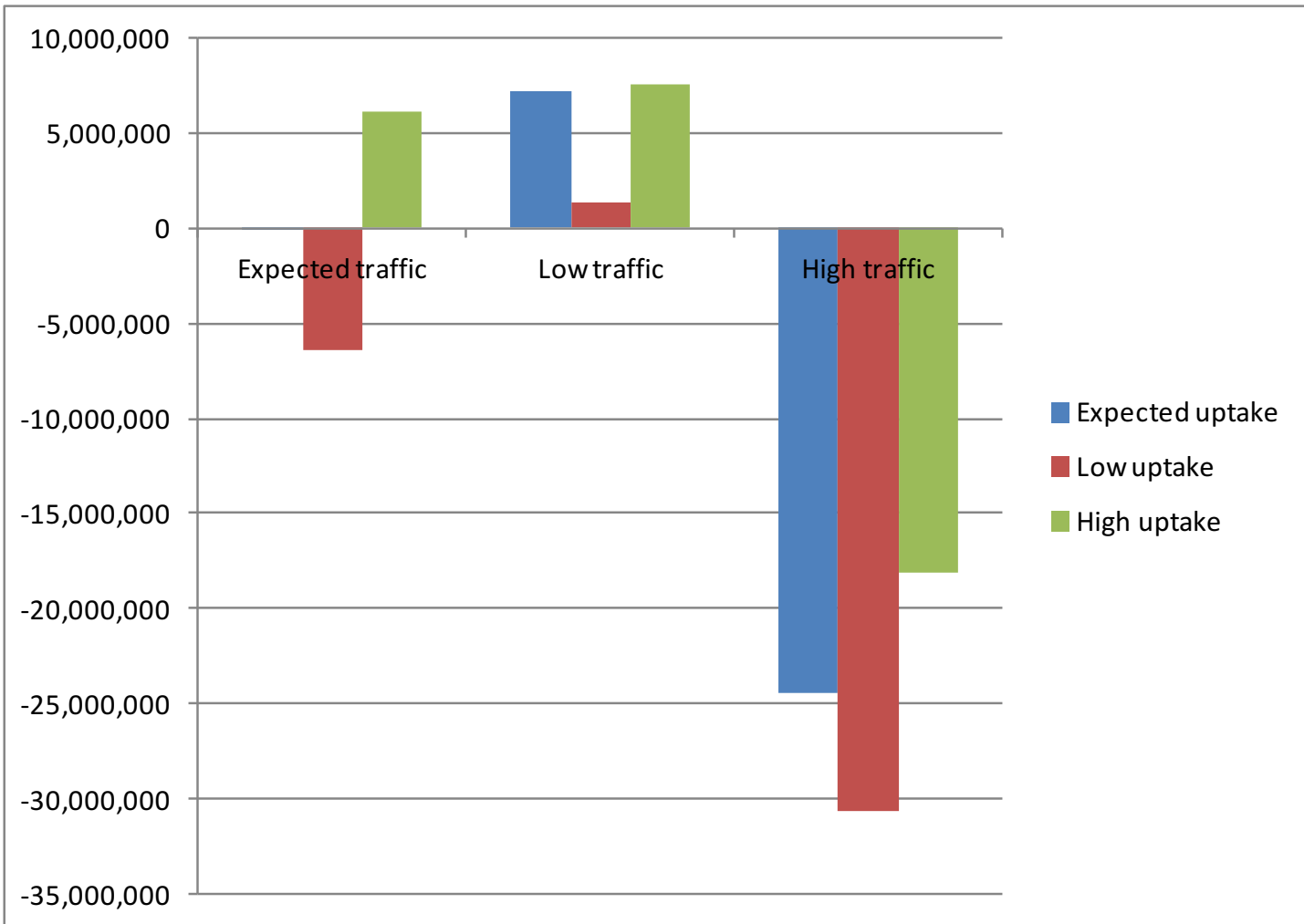
- # BS
- Fiber lease cost

# Result can be very different under different traffic growth assumptions

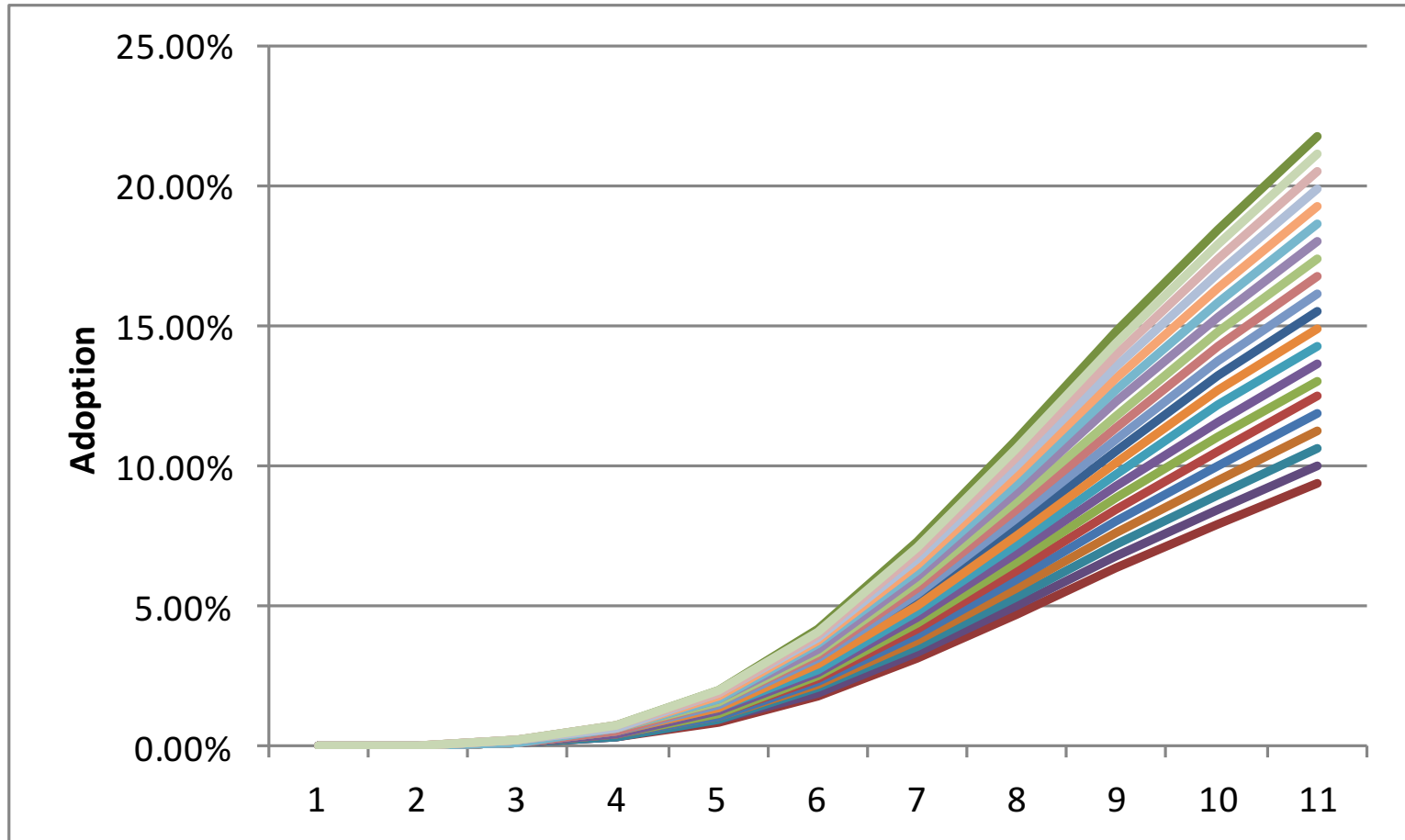


# Results are even more different

under combined market potential and traffic growth assumptions

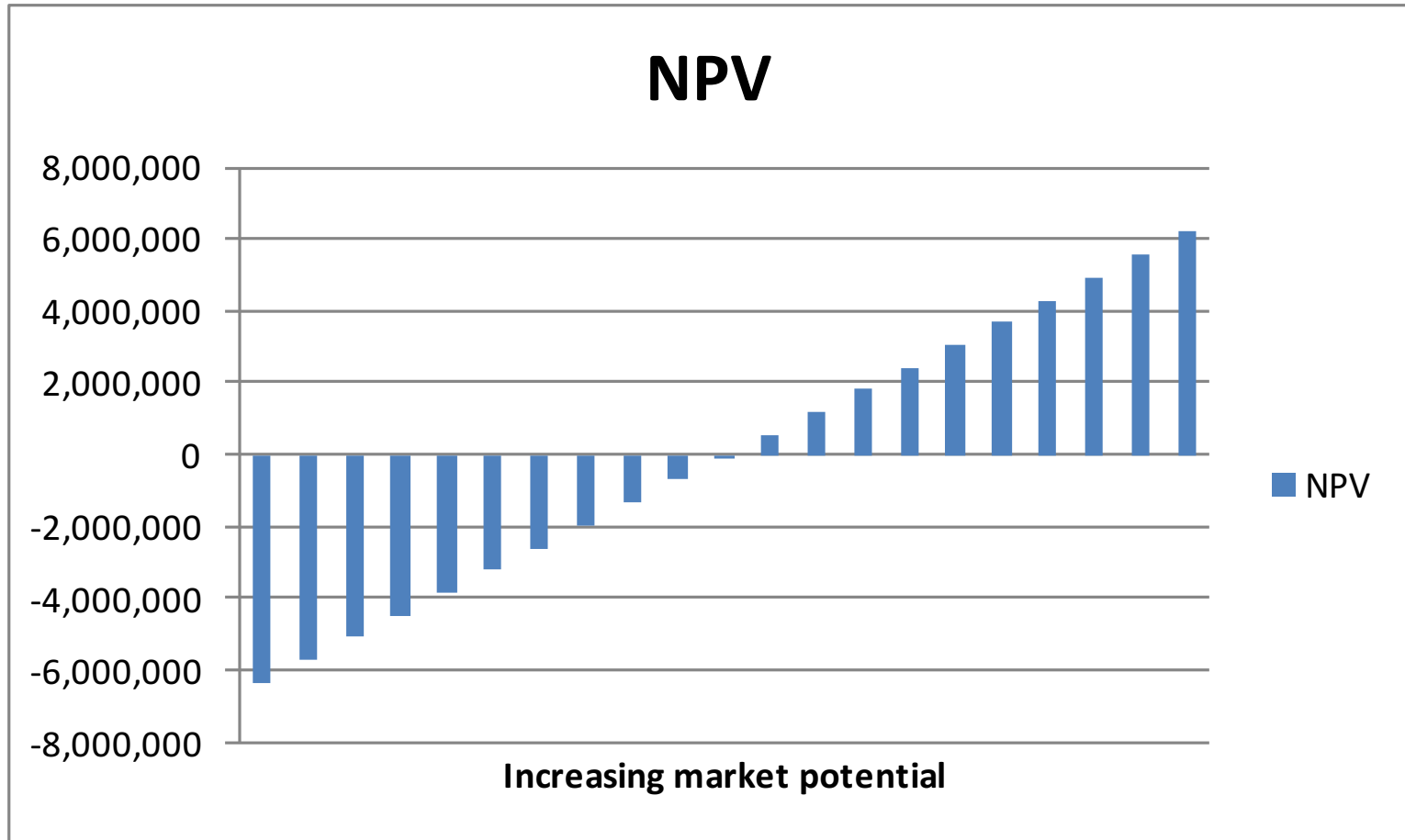


# From discrete to continuous uncertainty by adding big amount of scenarios



# From discrete to continuous uncertainty

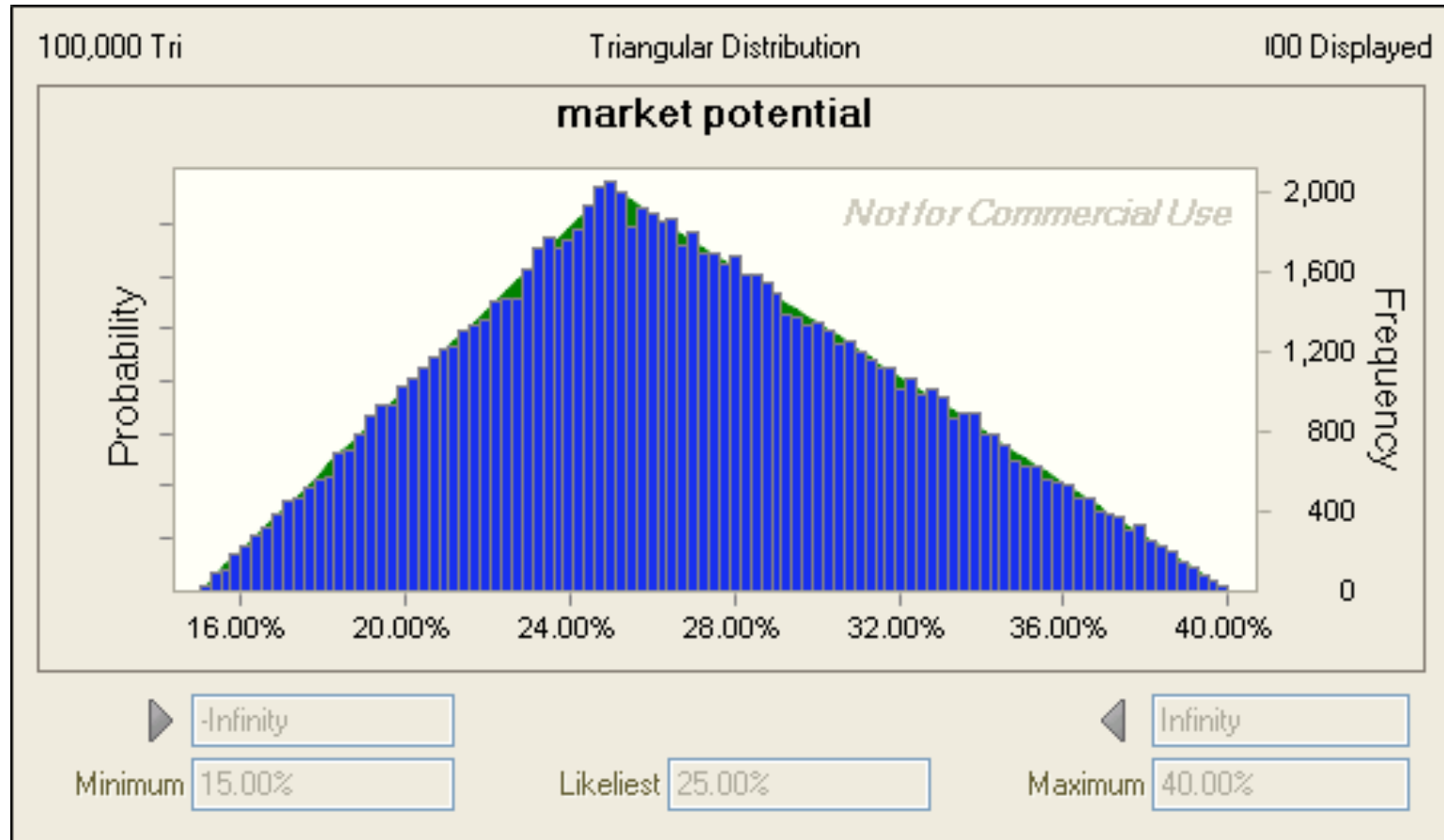
shows range of results, representing range of scenarios



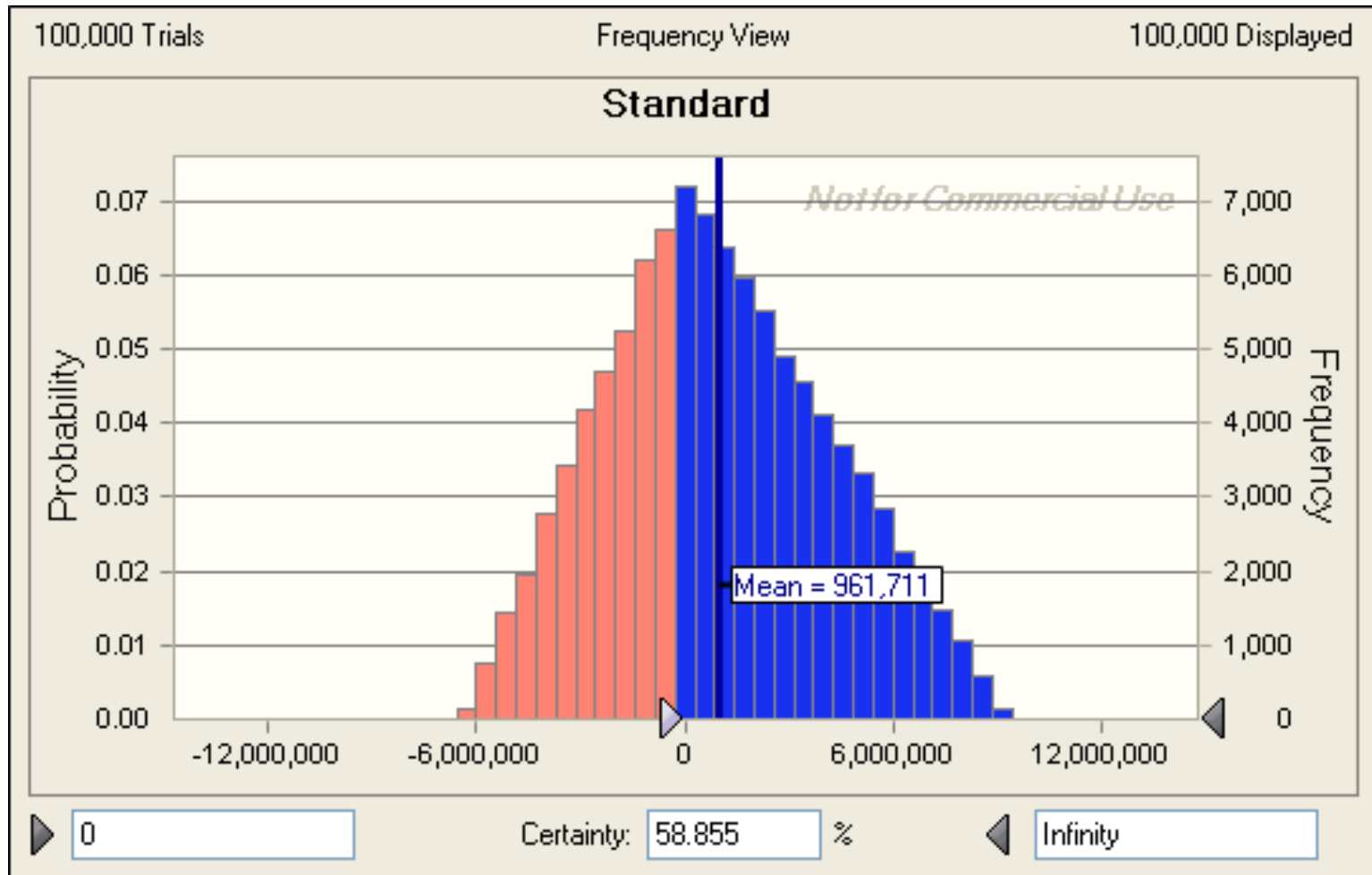


# Density distribution of results

indicates mean value and deviations

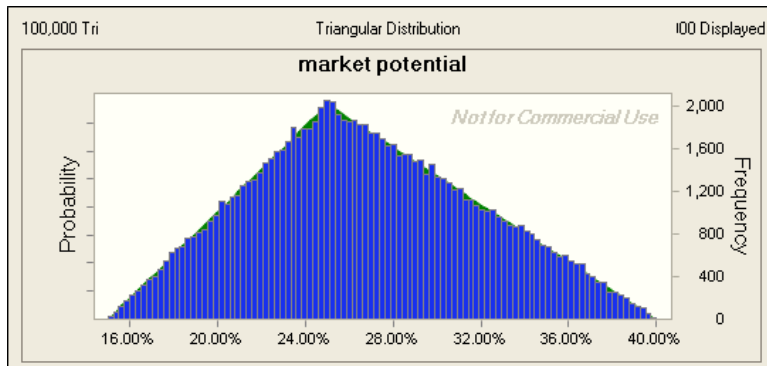


# Density distribution of results leads to helpful interpretations

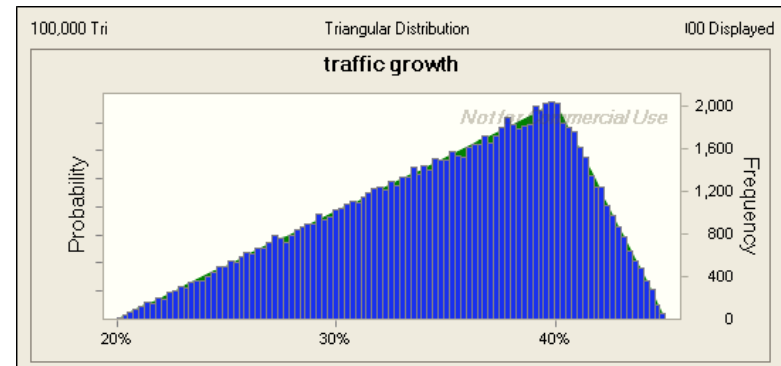


# Combined uncertainties on adoption and traffic growth..

## Adoption

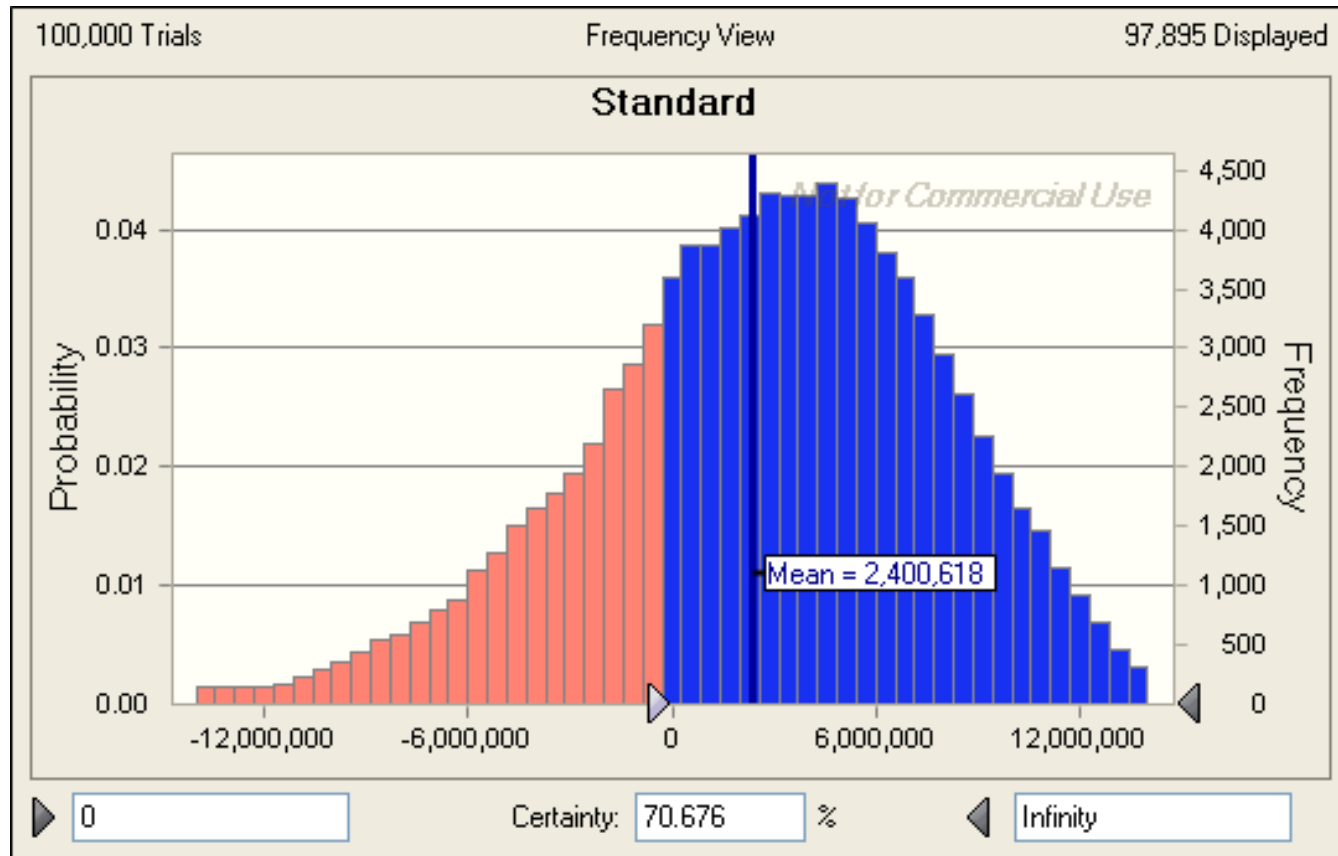


## Traffic growth



# Combined uncertainties

lead to combined impact on results..



# Conclusion

## on the use case of LTE deployment in Gent

The project is unprofitable

- Negative payoff under initial conditions
- Very sensitive to input

But the operator has flexibility

- Deploy network in another city
- Stop project if it turns out unprofitable
- Offer differentiated services
- Use other technology



*Should I deploy  
the network in  
other cities?*

*Is it worth more  
paying for a larger  
wireless license?*



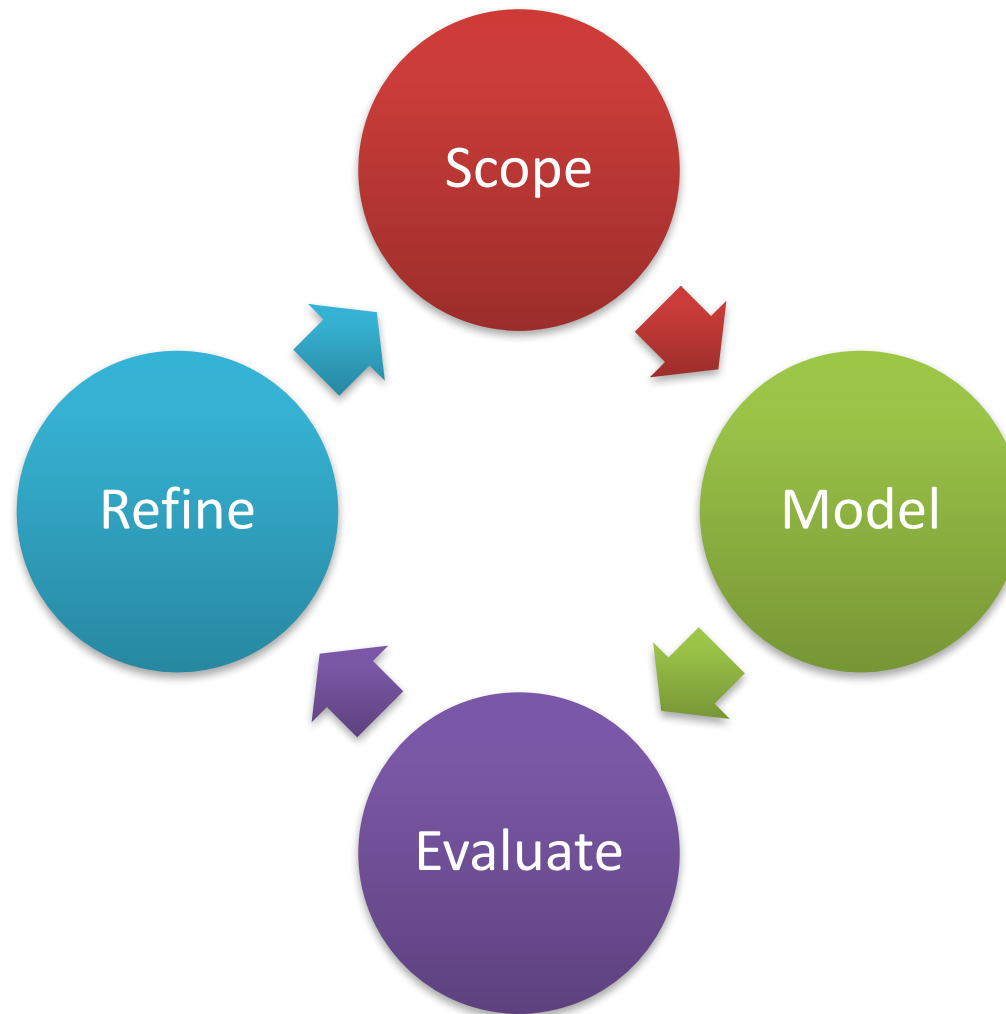
# Deploy in other cities

## in Antwerp

- 483.505 inhabitants
- 204.5 km<sup>2</sup>



# Following the same methodology

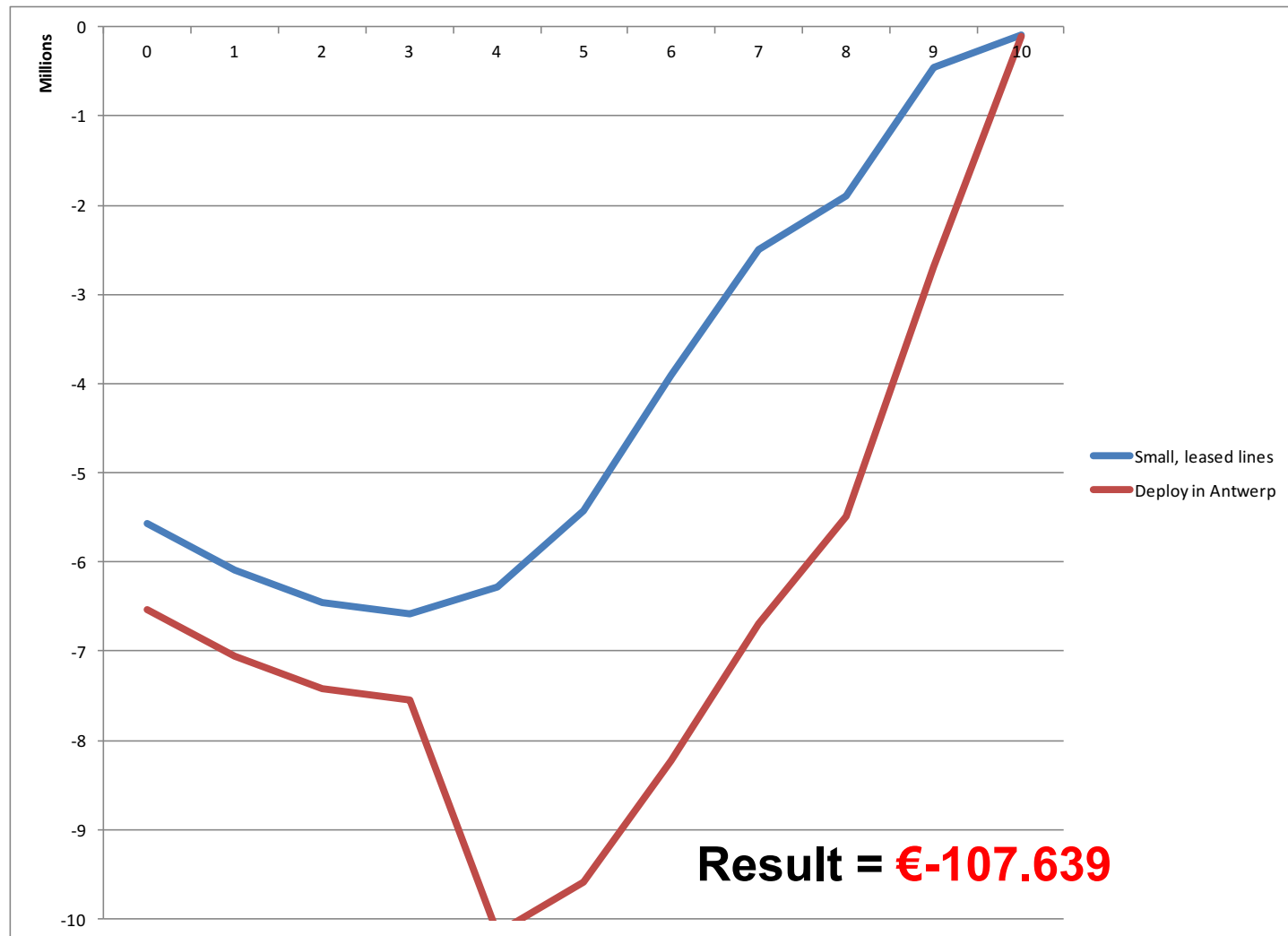




# Minor differences with previous case

- Deployment in Antwerp in year 4
  - Higher initial license cost
  - Extra CapEx and OpEx
- But also larger market
  - Higher potential revenues

# Result from deployment in other cities



# But what if operator has flexibility?

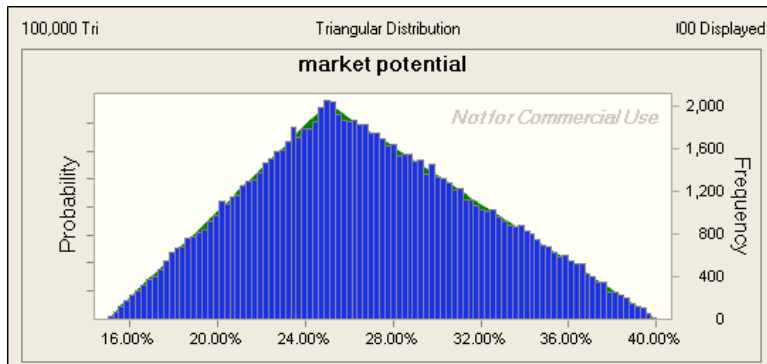
## 1. He can do an extra deployment/ expand the deployment

### Extra deployment only

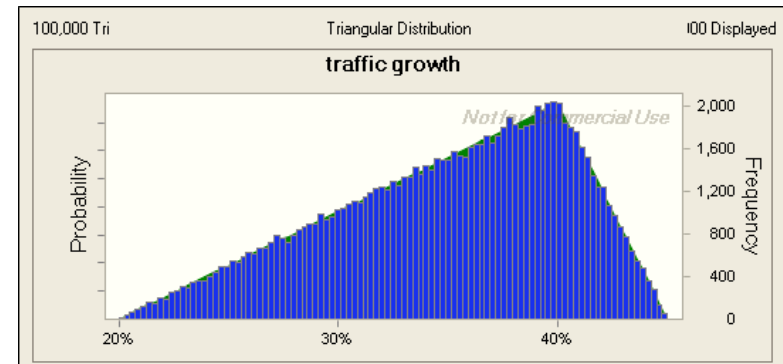
- If positive impact on case
- Impacted by uncertainty
  - Adoption
  - Traffic growth

# Uncertainties

## Adoption

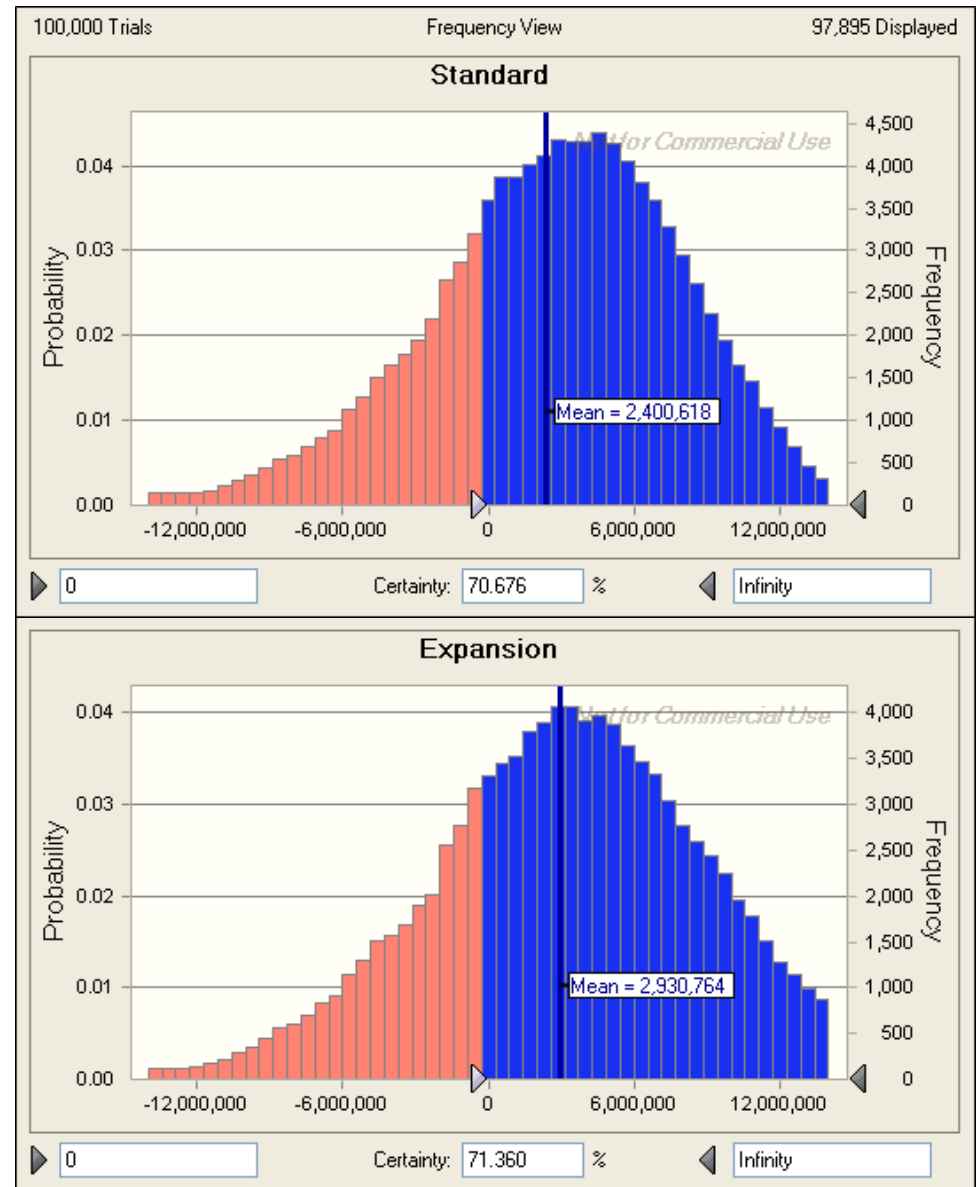


## Traffic growth

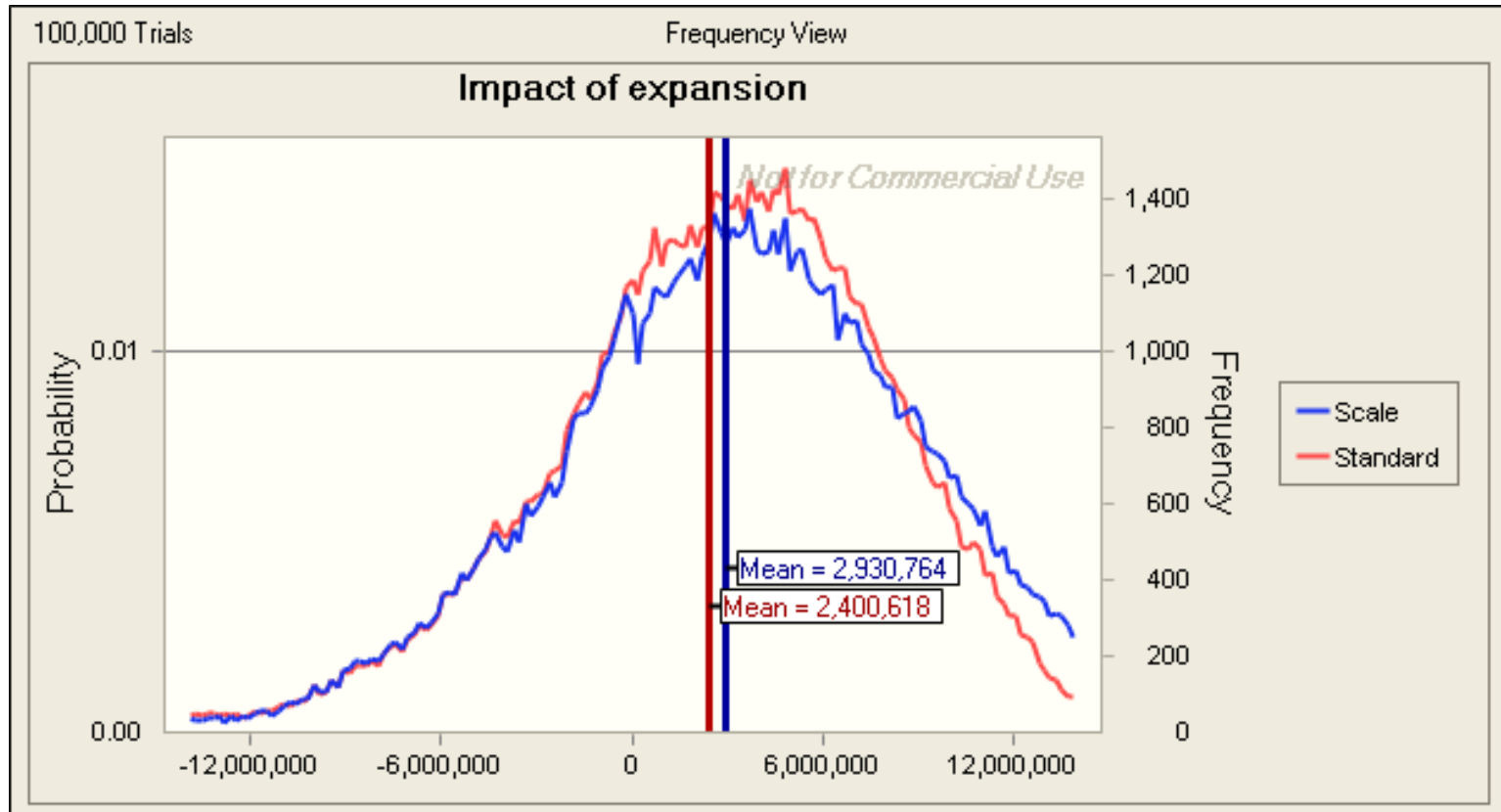


# Flexibility to expand has a positive impact

- Expected payoff
  - + 22%
- Risk
  - Higher probability of positive case +0.7%
  - Mean negative -3% (license cost)



# Flexibility to expand shows a shift to a more positive result



*Do I continue  
with the  
operation of the  
wireless  
network?*

*Do I stop and sell  
my license if it is not  
viable?*



# What if operator has flexibility?

## 2. He can abandon the project

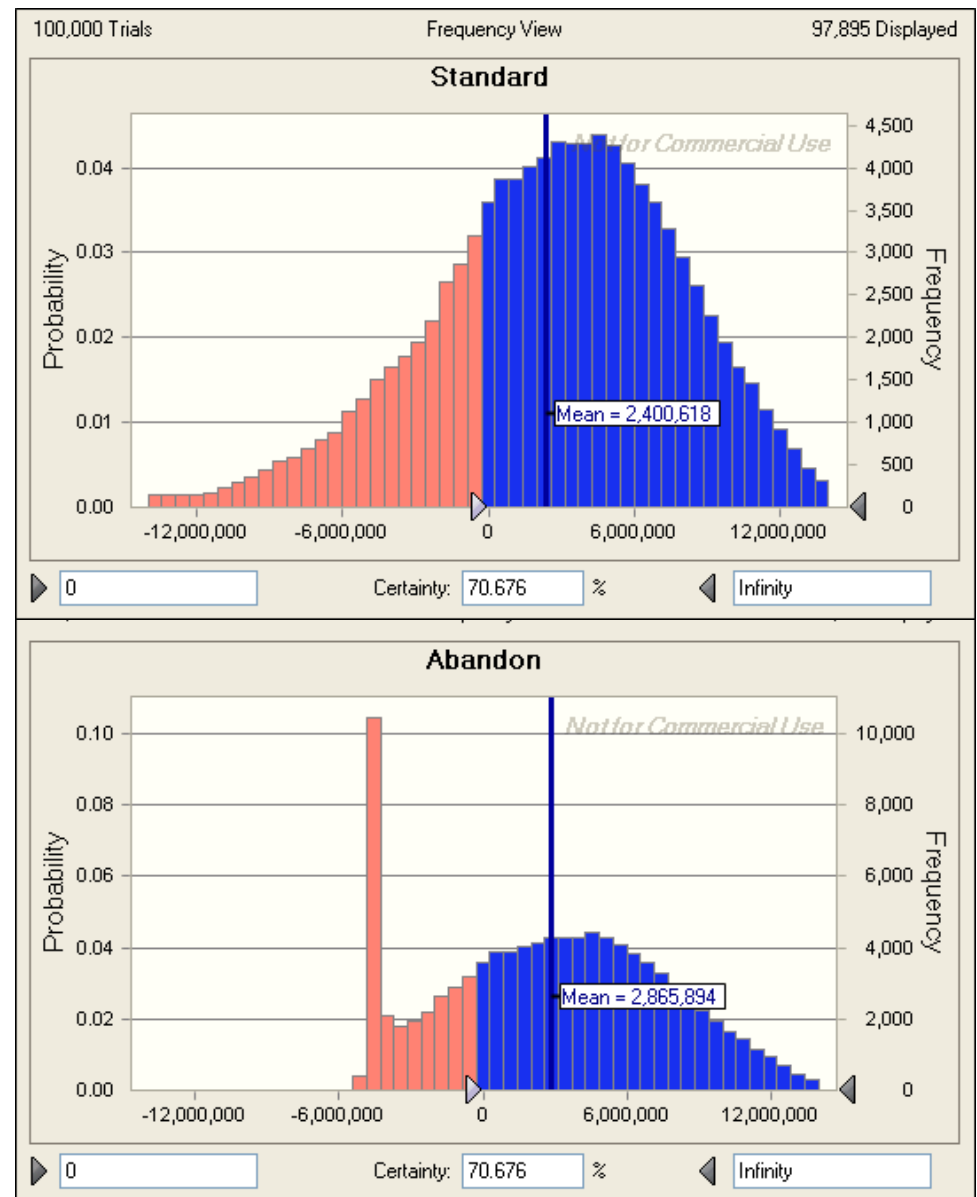
### If outlook is negative

- Abandon the project
- Cut losses
- Gain revenues from
  - License sale
  - Scrap value of equipment (50%)



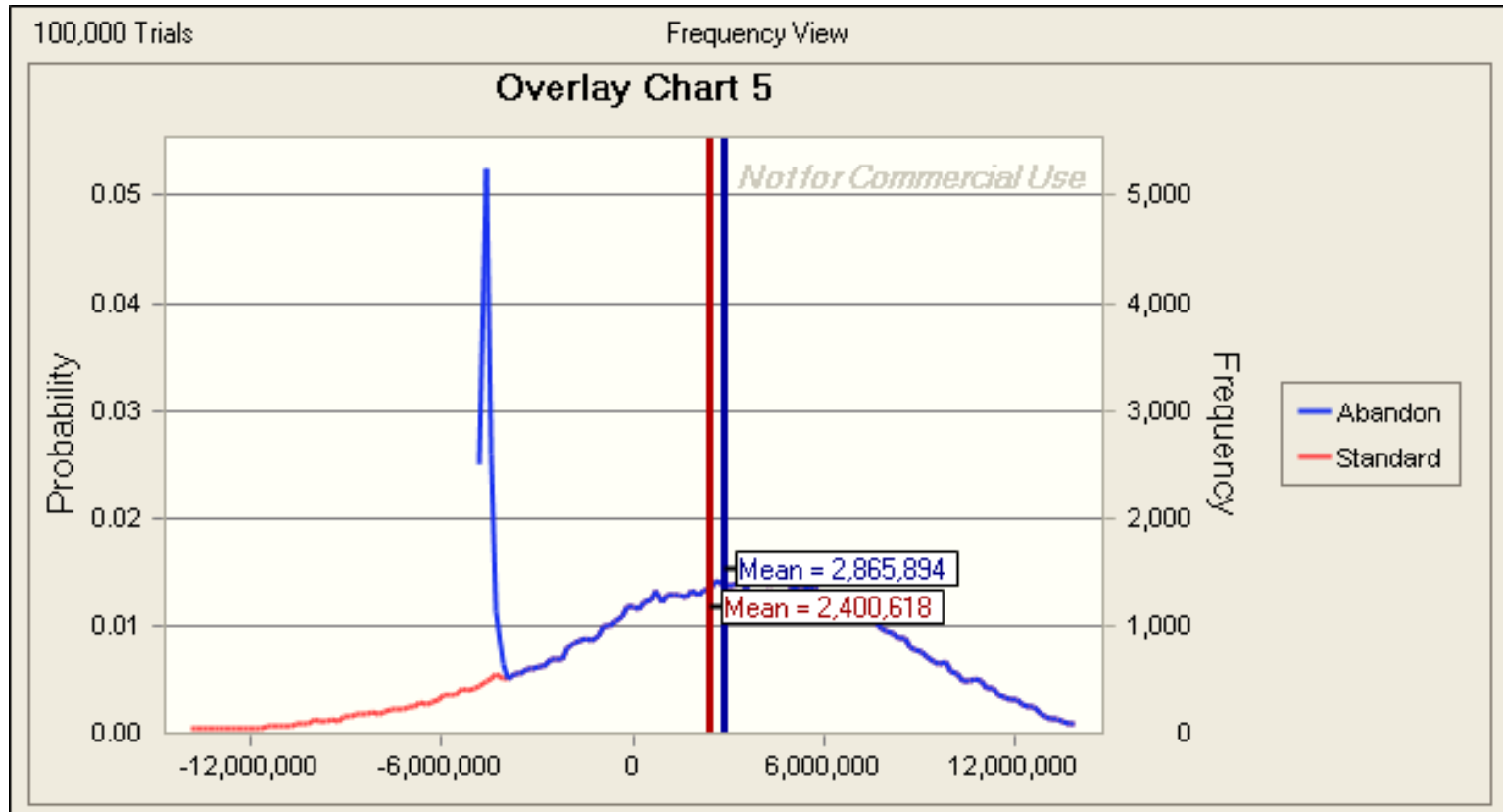
# Flexibility to abandon shows a dual effect on result

- Expected payoff
  - + 19%
- Risk
  - No impact on positive probability
  - Clear that tail is cut
  - Mean negative +20%



# Flexibility to abandon

shows a cut in the negative tail in the expected result



*Do I lease the  
backhaul  
capacity?*

*Is it more interesting  
to install my own  
fixed backhaul  
network?*



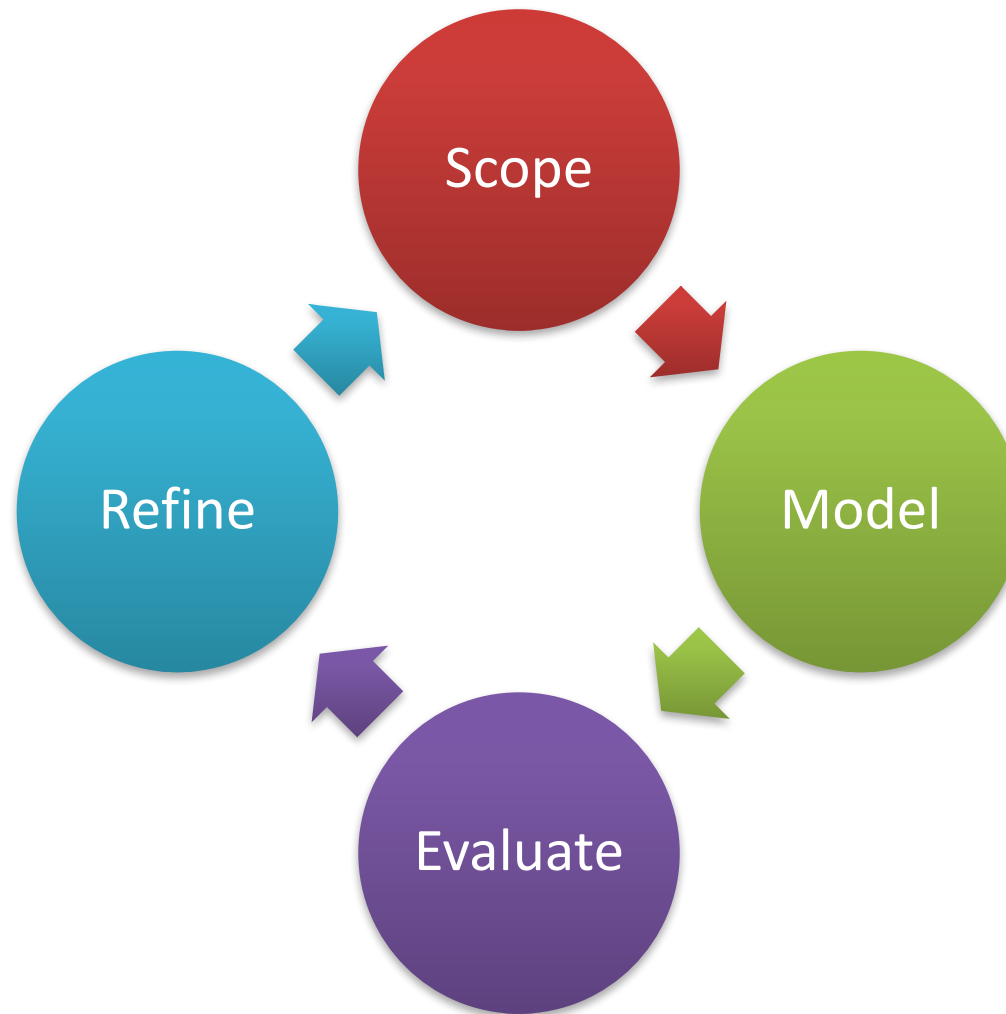
# But what if operator has flexibility?

## 3. He can install his own backhaul infrastructure

### Buy-or-lease decision

- Infrastructure installation is expensive
- Only interesting under large traffic volumes
  - High uptake
  - High traffic growth
- Requires fiber dimensioning
- Installation in Y4

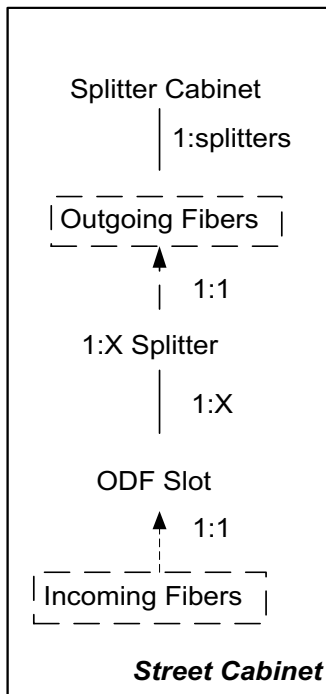
# Following the same methodology



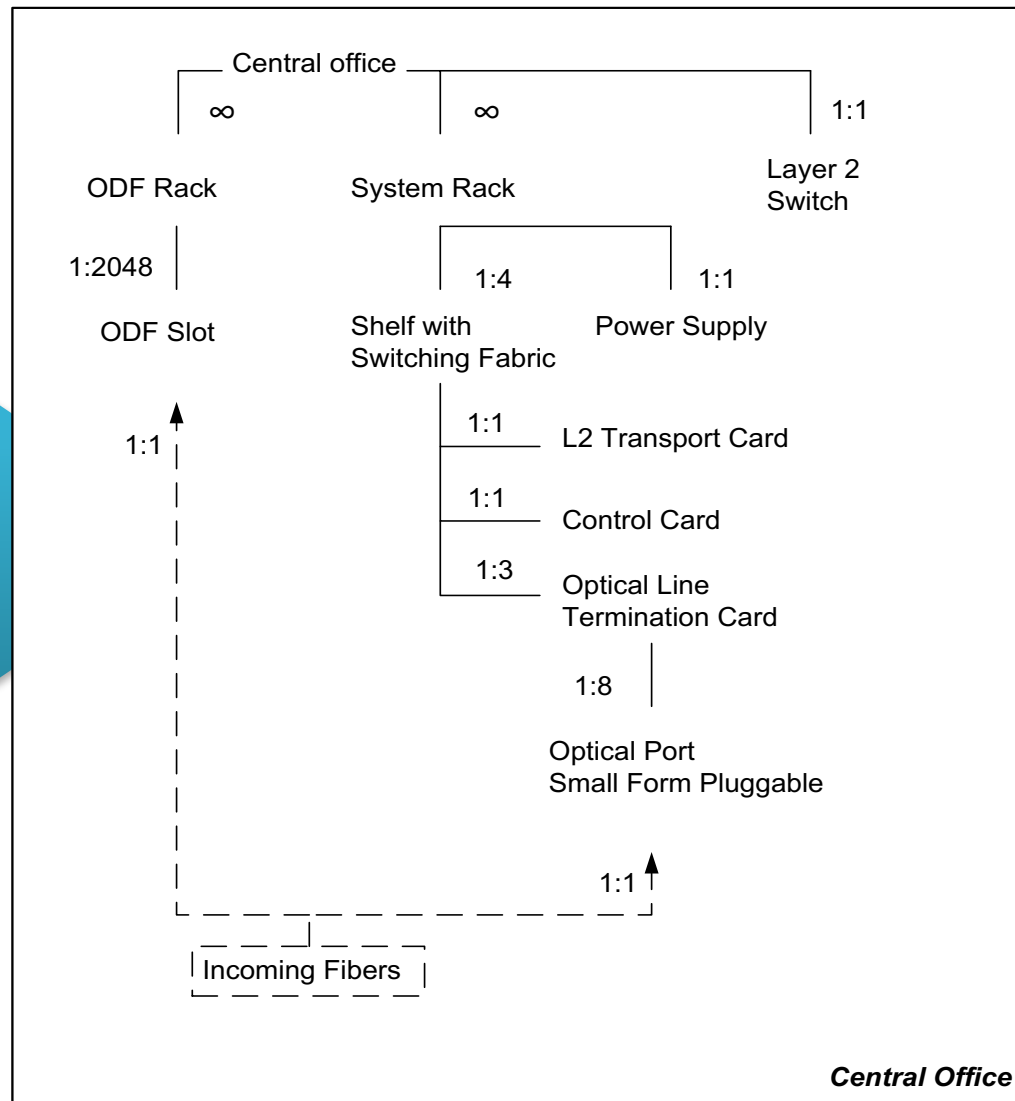
# Following the same methodology

Parameter	Cost	Unit
Fiber	€0.20	Per meter
1:32 splitter	€500	Per 32 fiber
L2 switch	€650	Per Central Office
Power supply	€700	Per Central Office
Optical port	€15	Per splitter
OLT card	€2.000	Per 8 ports
Shelf	€5.375	Per 3 cards
System rack	€600	Per 4 shelves
ODF slot	€20	Per splitter
ODF rack	€800	Per 2048 slots

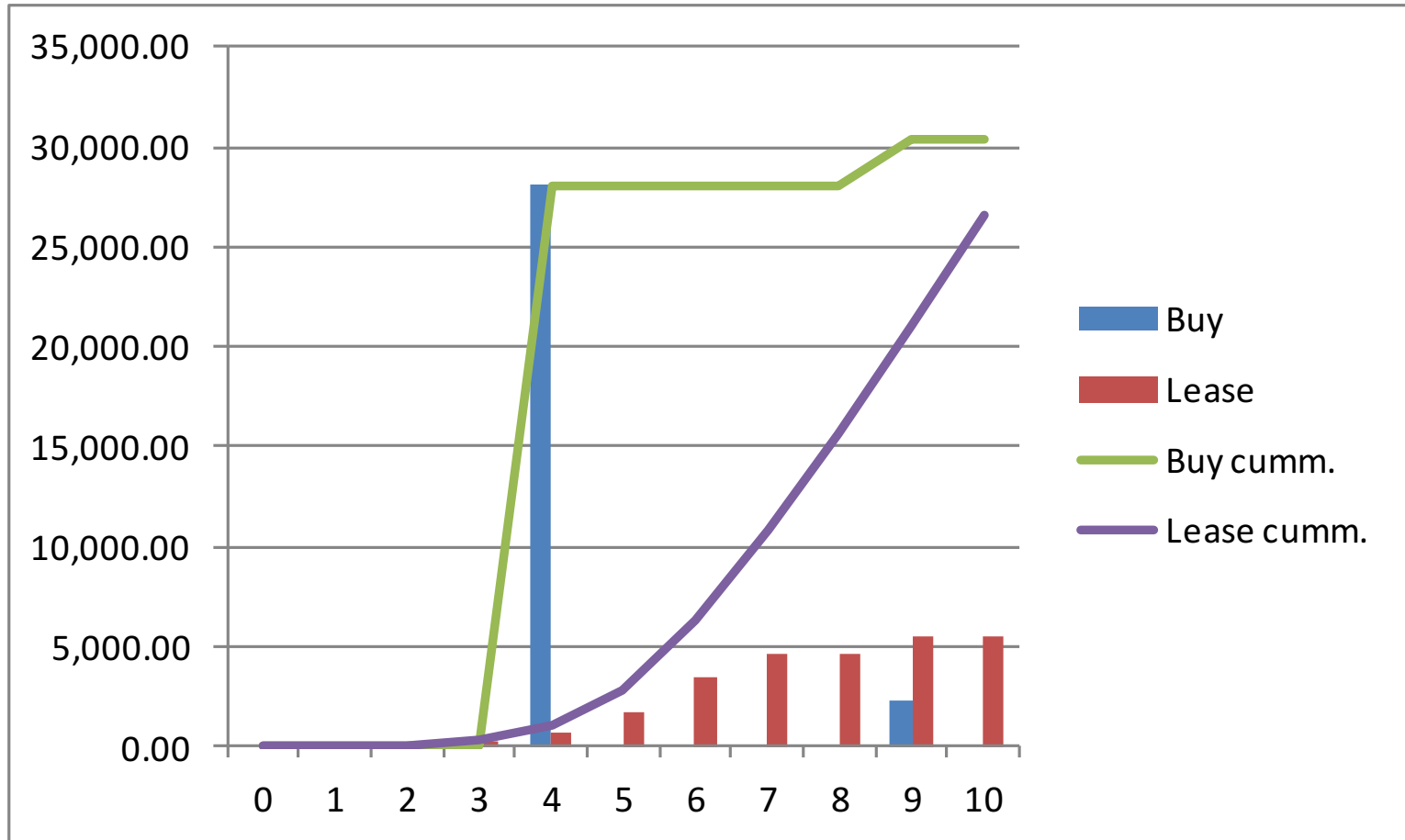
# Following the same methodology



efine



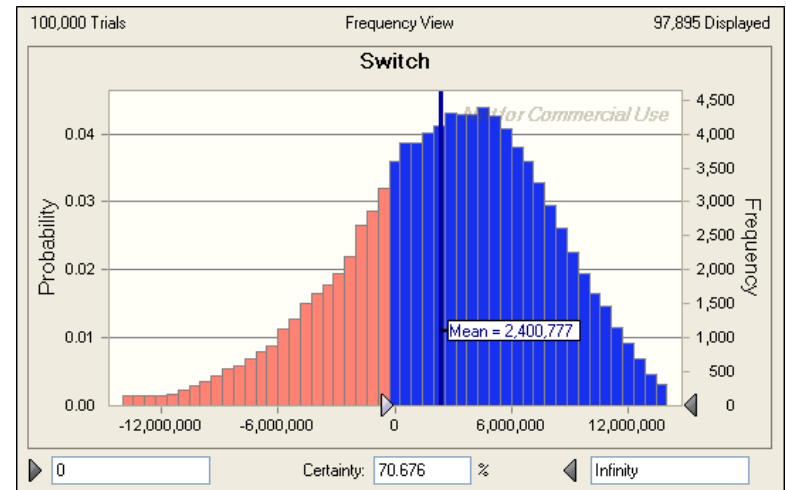
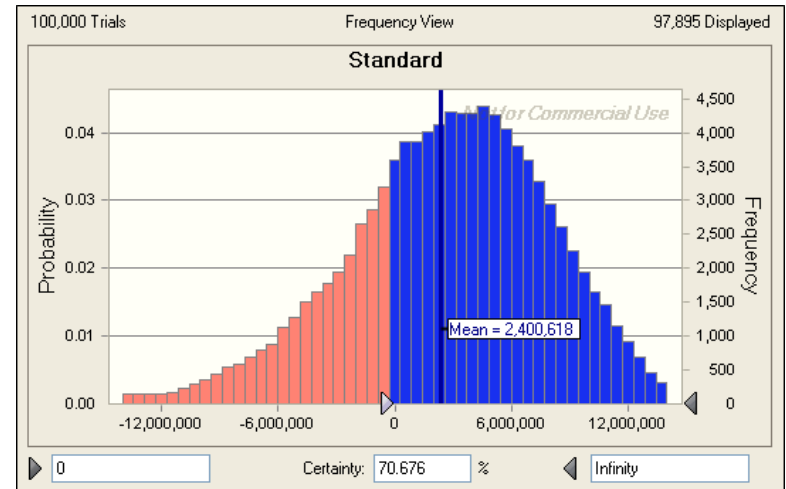
# Buy-or-lease decision





# Flexibility to deploy on own backhaul shows a negligible impact on result

- Expected payoff
  - + 0.007%
- Risk
  - No impact



*Are all  
customers  
buying the same  
service?*

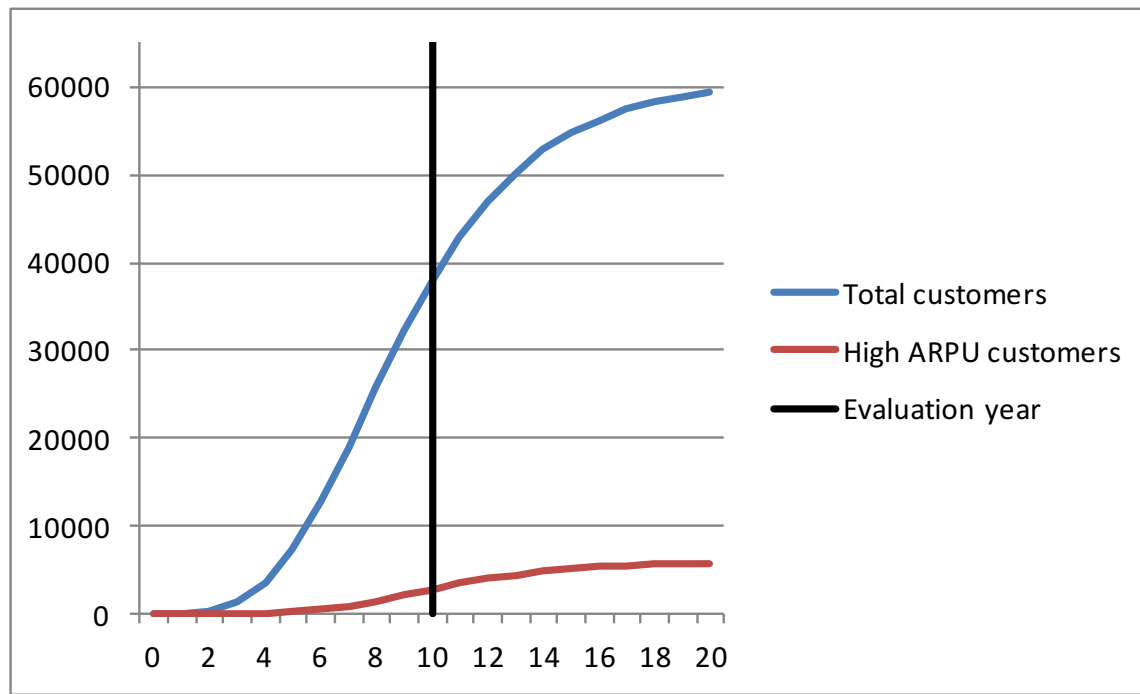
*Or can I differentiate,  
and sell different  
services?*



# But what if operator has flexibility?

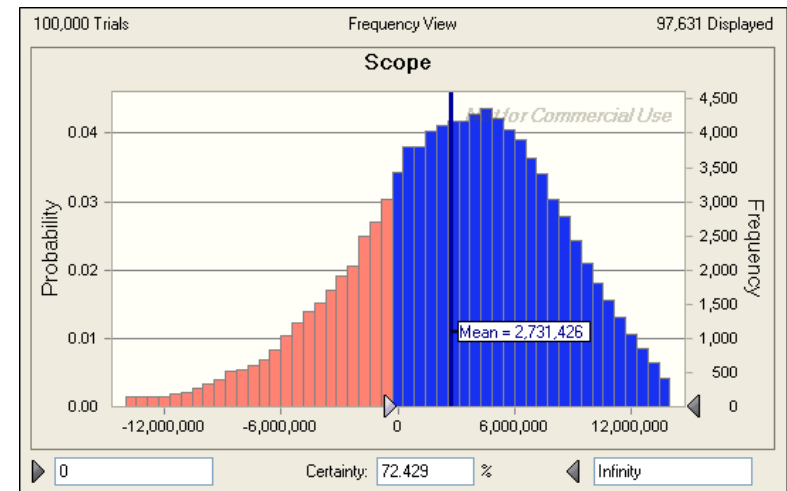
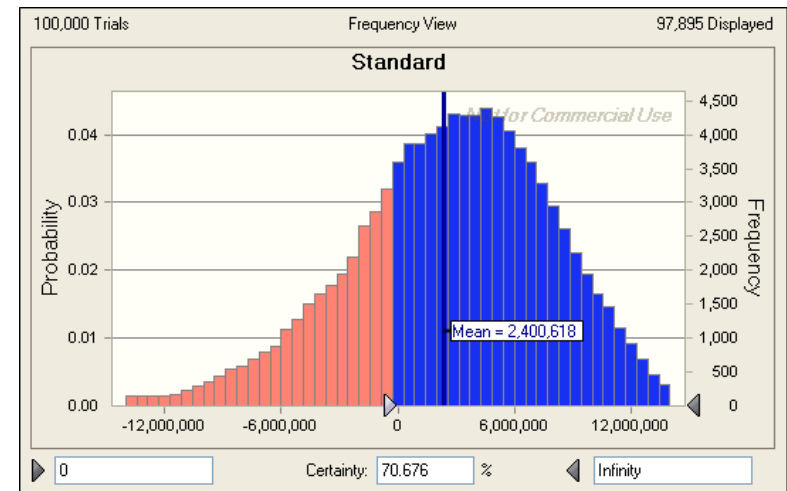
## 4. He can differentiate between customers

- Sell high-speed subscriptions
- Will require capacity upgrade
- Customers with higher ARPU
- Decide in Y4



# Flexibility to differentiate between customers shows a positive impact on the result

- Expected payoff
  - + 13.8%
- Risk
  - Higher probability of positive case (+1.8%)
  - No impact on mean negative (no option cost)



*Do I expand my network to a larger area?*

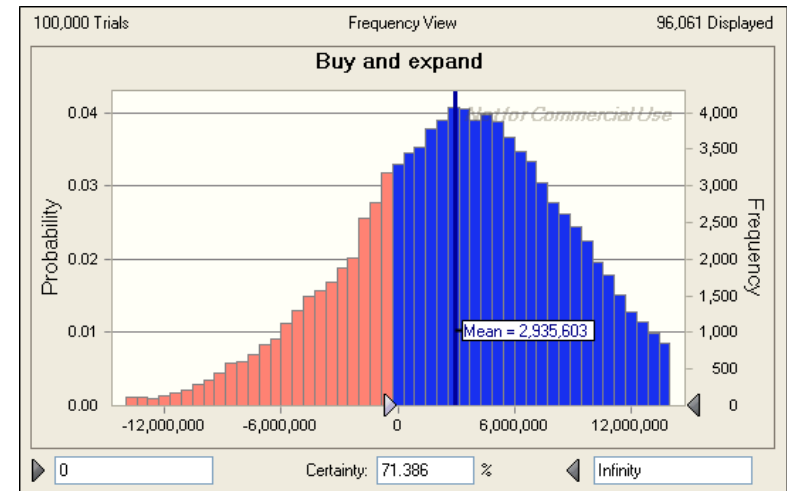
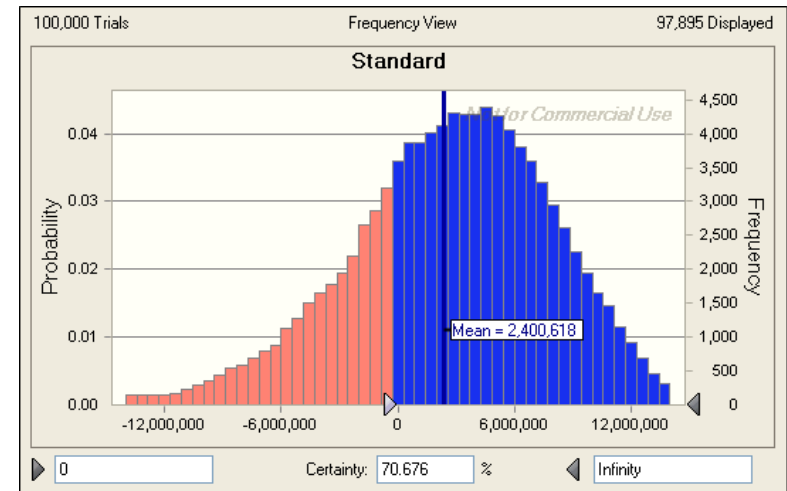
*Is installing my own backhaul capacity more interesting?*



# Combined flexibility

## to expand and switch to own backhaul

- Expected payoff
  - + 22.3%
  - Buying backhaul creates value
- Risk
  - Higher probability of positive case (+0.7%)
  - Mean negative -3% (license cost)



# Uncertainty and Flexibility

are typical in real investment problems

# Uncertainty in telecom planning: from case study

- Adoption
- Traffic growth



# Uncertainty in telecom planning: more examples

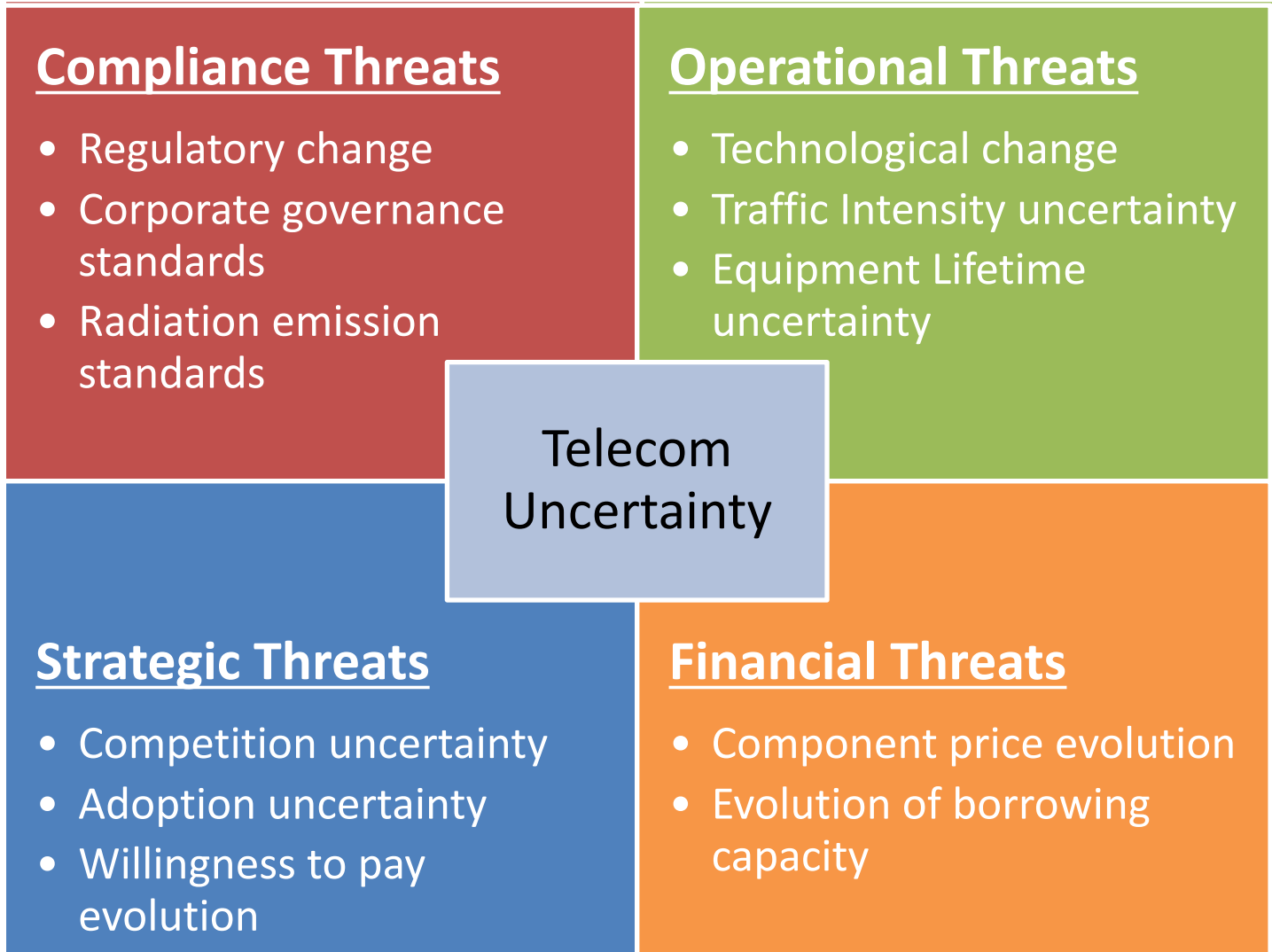
- Technological change
  - alternative technologies
  - improved standards
- Competition uncertainty
  - competitor entry
- Adoption uncertainty
  - potential
  - timing
  - speed
- Regulatory changes
  - Licensing
  - Radiation limits
  - corporate governance standards
  - forced network unbundling
- Component price evolution
  - resource price inflation
- Traffic intensity uncertainty
  - OTT services
  - geographical concentration of usage (events)
- Equipment lifetime uncertainty
- Borrowing capability
- Willingness to pay/ARPU evolution

# Sources of uncertainty in telecom planning



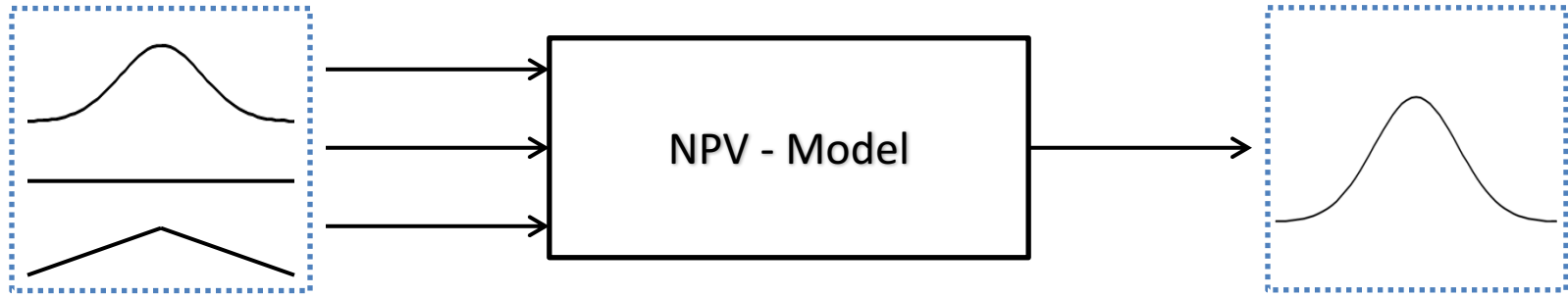
# Sources of uncertainty in telecom planning

allow to classify typical uncertain parameters



# Impact of uncertainty on decision making

when the input is uncertain, the output is uncertain as well

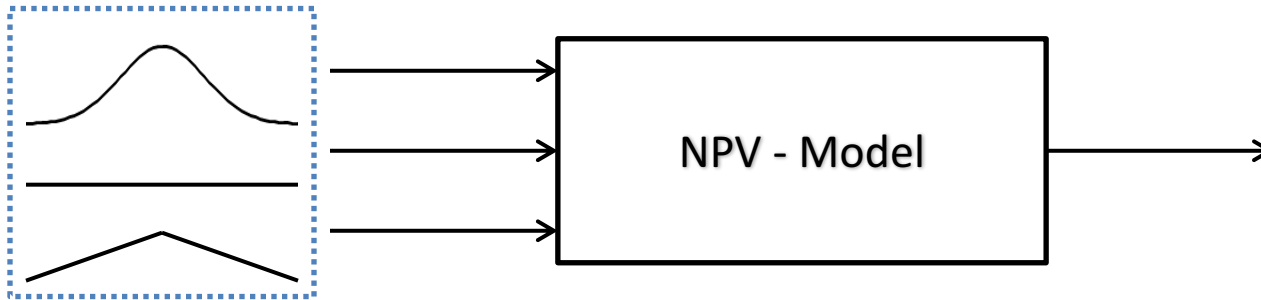


Input information is uncertain for different reasons

- Inherently
  - Aleatoric uncertainty
- Data unavailable
  - confidential
  - costly predictions
- Timing issues
  - Will become available at  $t > 0$

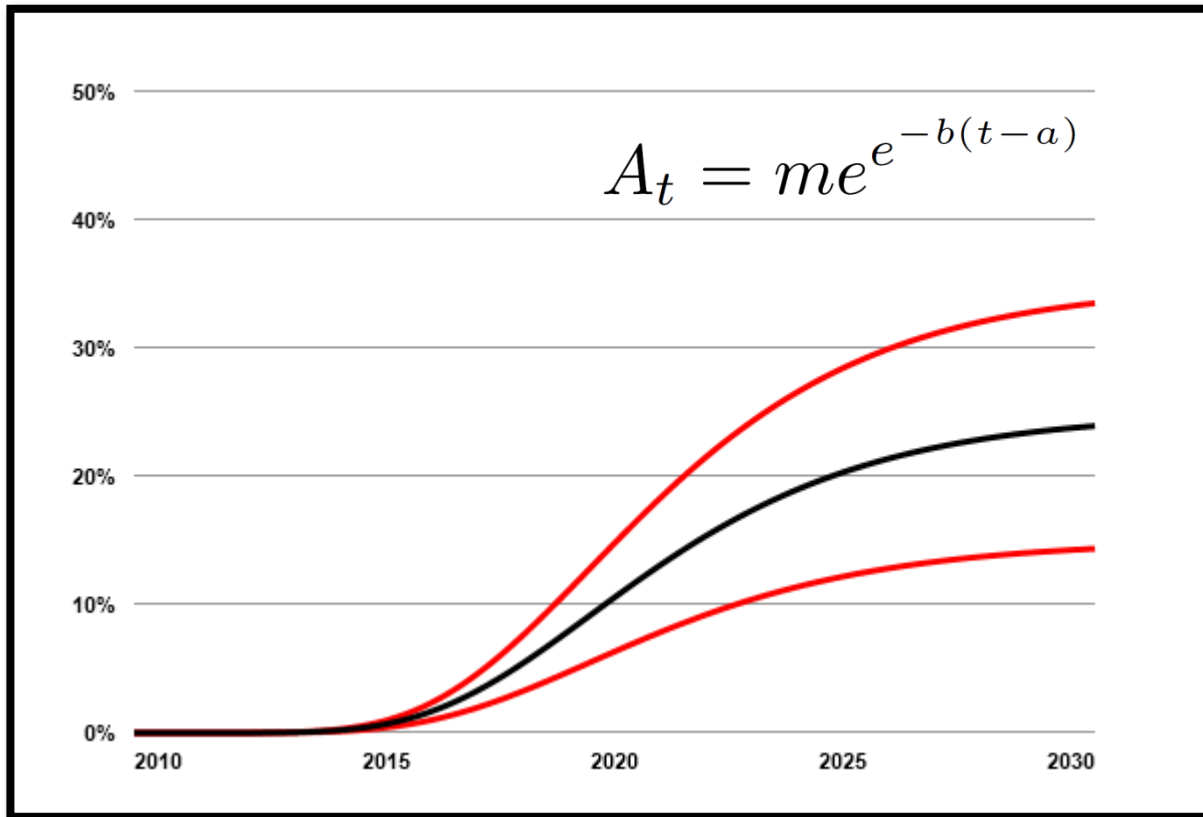
# Impact of uncertainty on decision making

when the input is uncertain, the output is uncertain as well



Different ways to model  
input uncertainty

# Sources of uncertainty, in the case estimated adoption between high and low extreme

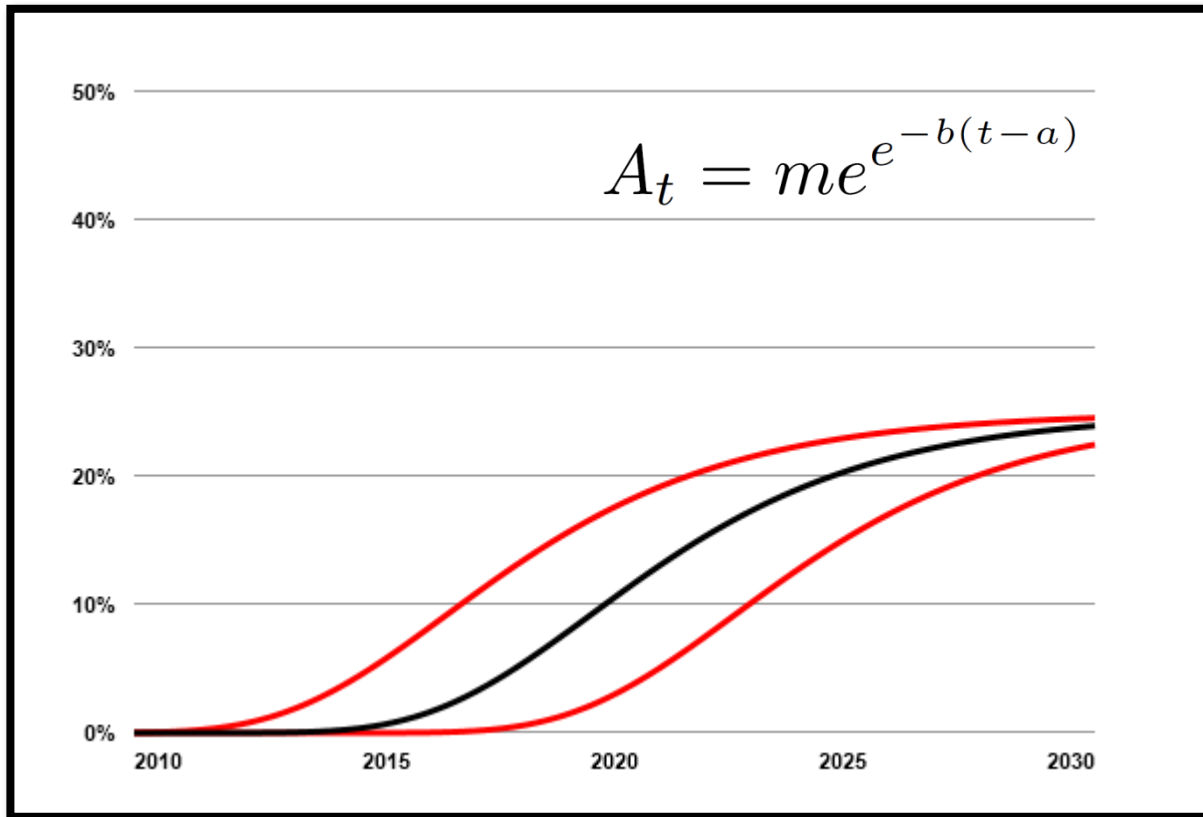


Gompertz Curve [1]:  
m: 0.15-0.35  
a: 2019,5  
b: 0.3

## ADOPTION POTENTIAL

# Sources of uncertainty, other possibilities

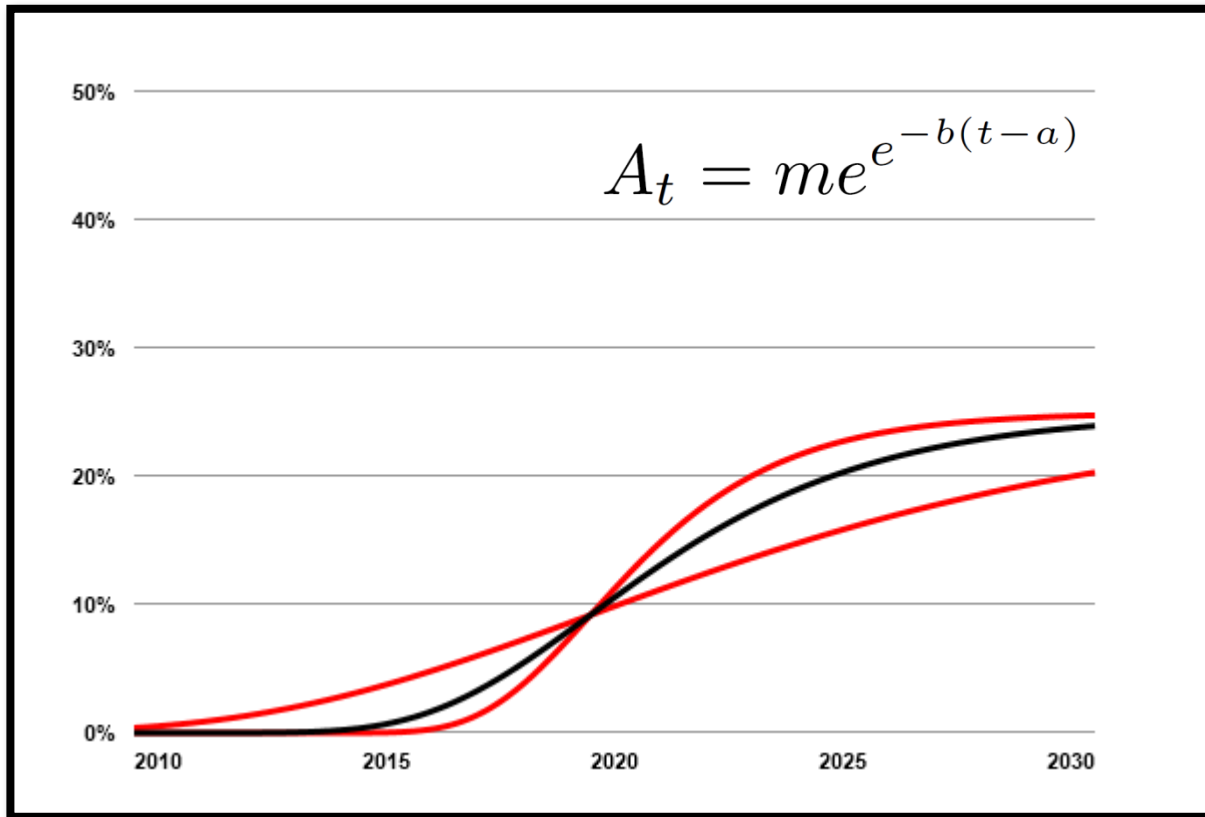
## timing of the adoption (position of inflection point)



m:	0.25
a:	2017,5 – 2021,5
b:	0.3

ADOPTION TIMING

# Sources of uncertainty, other possibilities adoption rate (steepness of the curve)

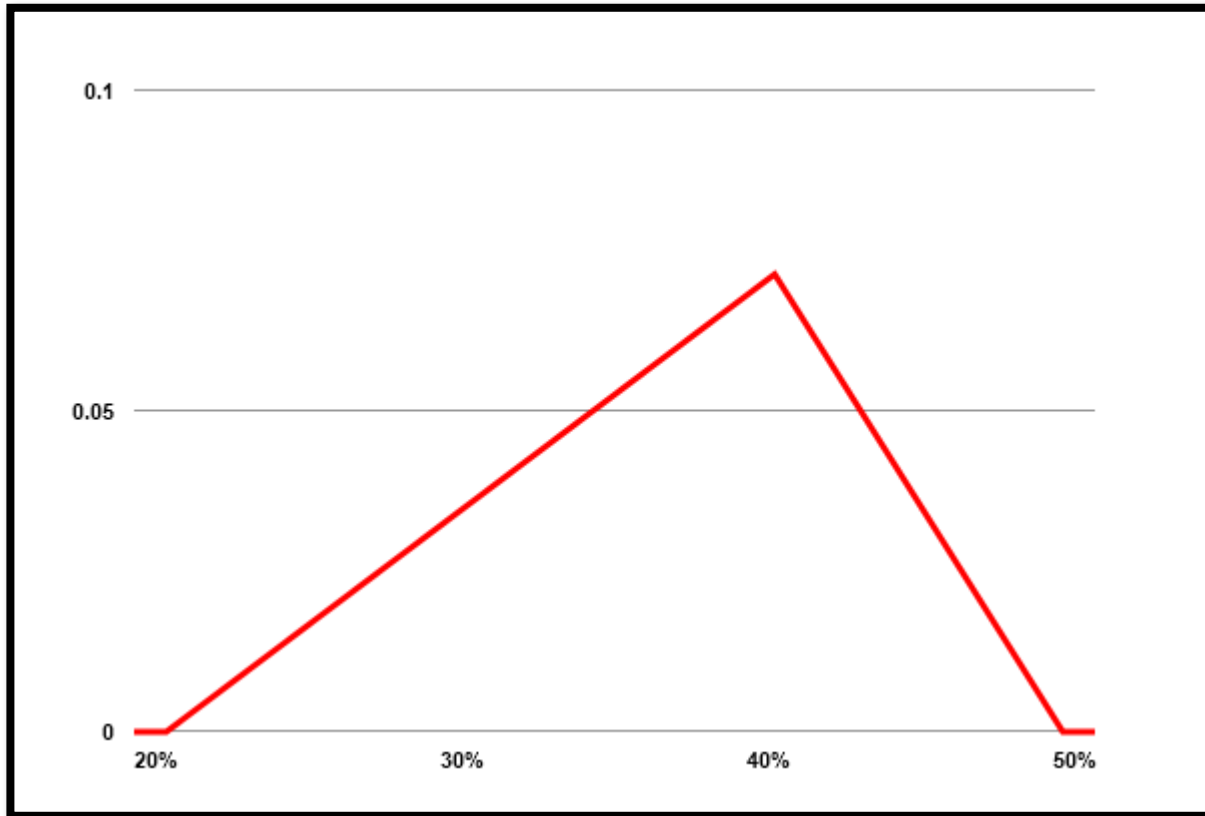


<b>m:</b>	<b>0.25</b>
<b>a:</b>	<b>2019,5</b>
<b>b:</b>	<b>0.15 – 0.45</b>

**ADOPTION RATE**

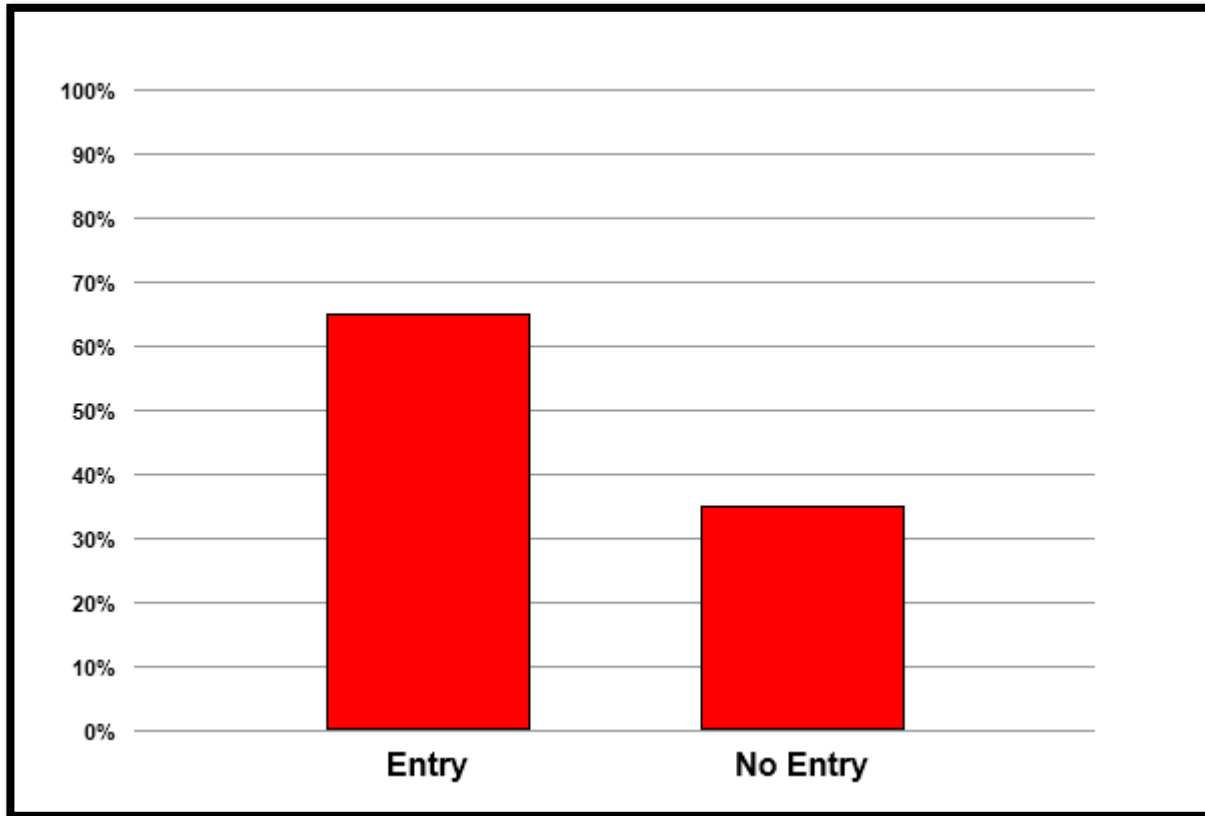


# Sources of uncertainty, in the case triangular between high and low extreme



**TRAFFIC GROWTH**

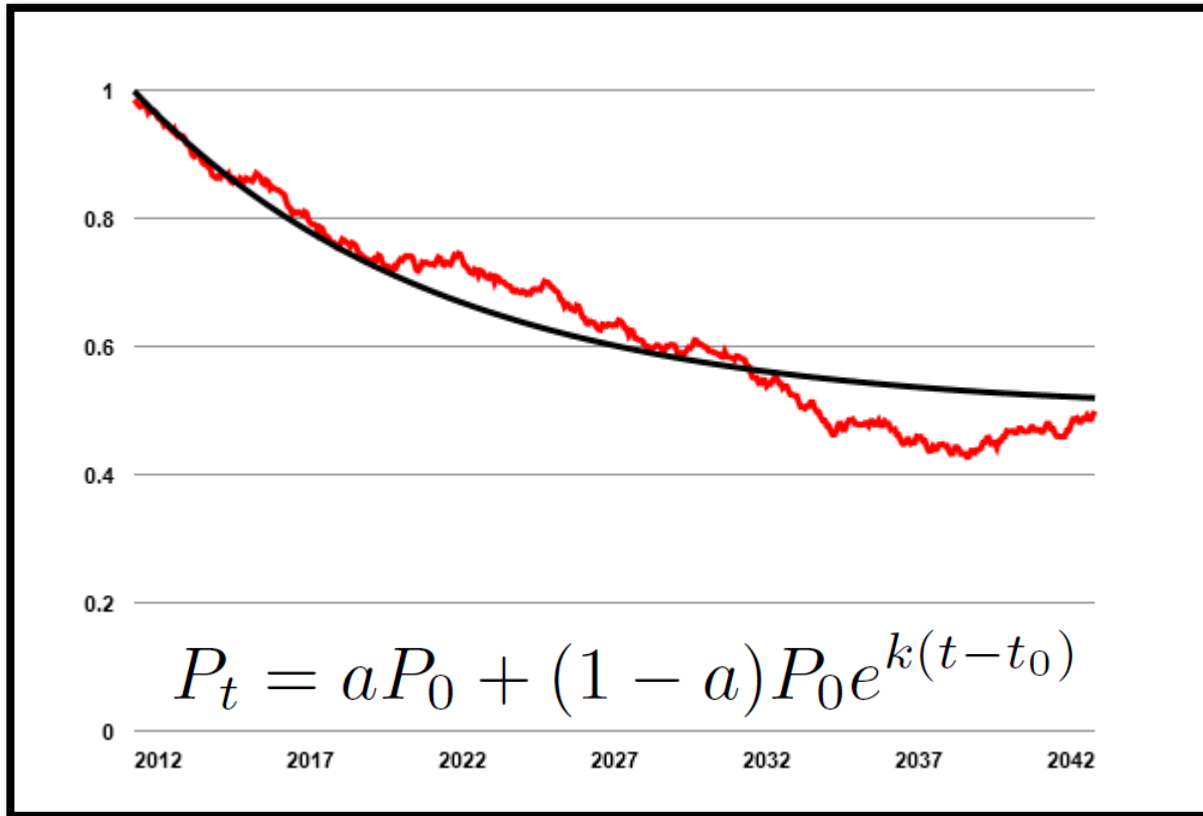
# Sources of uncertainty, other possibilities changes in competitive setting



**COMPETITOR ENTRY**

# Sources of uncertainty, other possibilities

## cost erosion over time



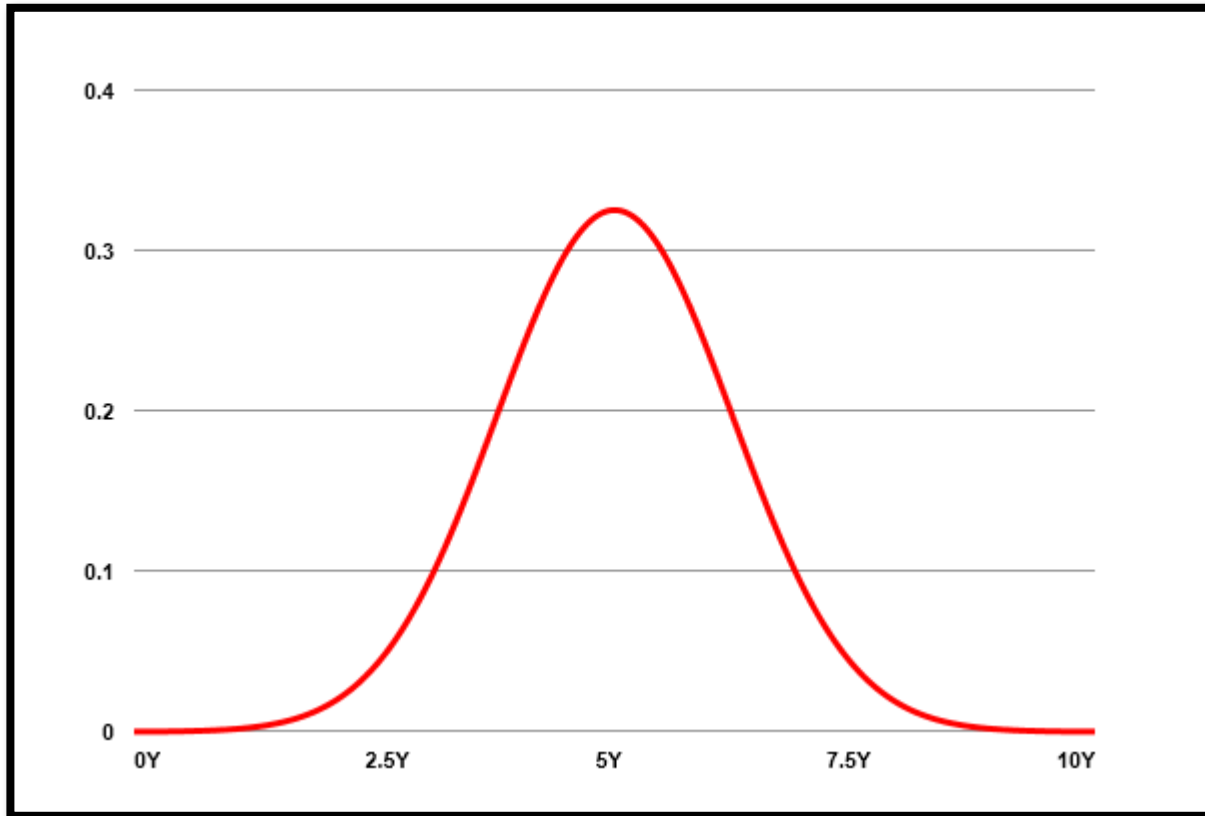
Simplified version of learning curve [1] with exponential decay:

P_0:	1
T_0:	2012
a:	0.5
k:	-0.1

**BASE STATION PRICE EVOLUTION**

# Sources of uncertainty, other possibilities

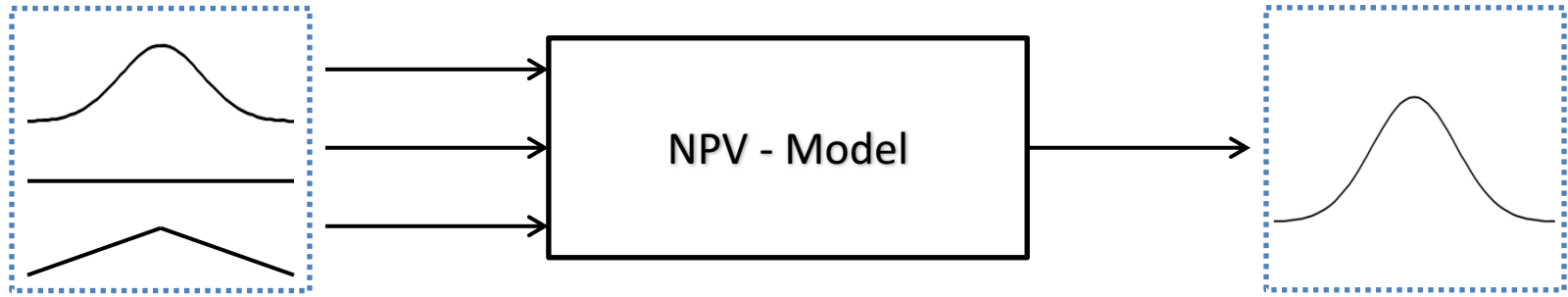
Gaussian distribution around mean expected lifetime



**BASE STATION LIFETIME**

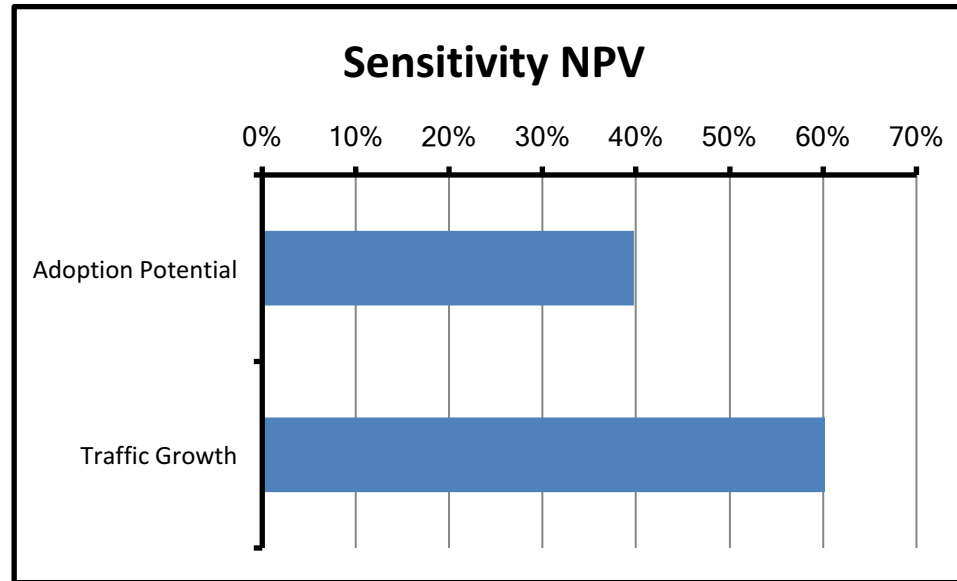
# Impact of uncertainty on decision making

when the input is uncertain, the output is uncertain as well



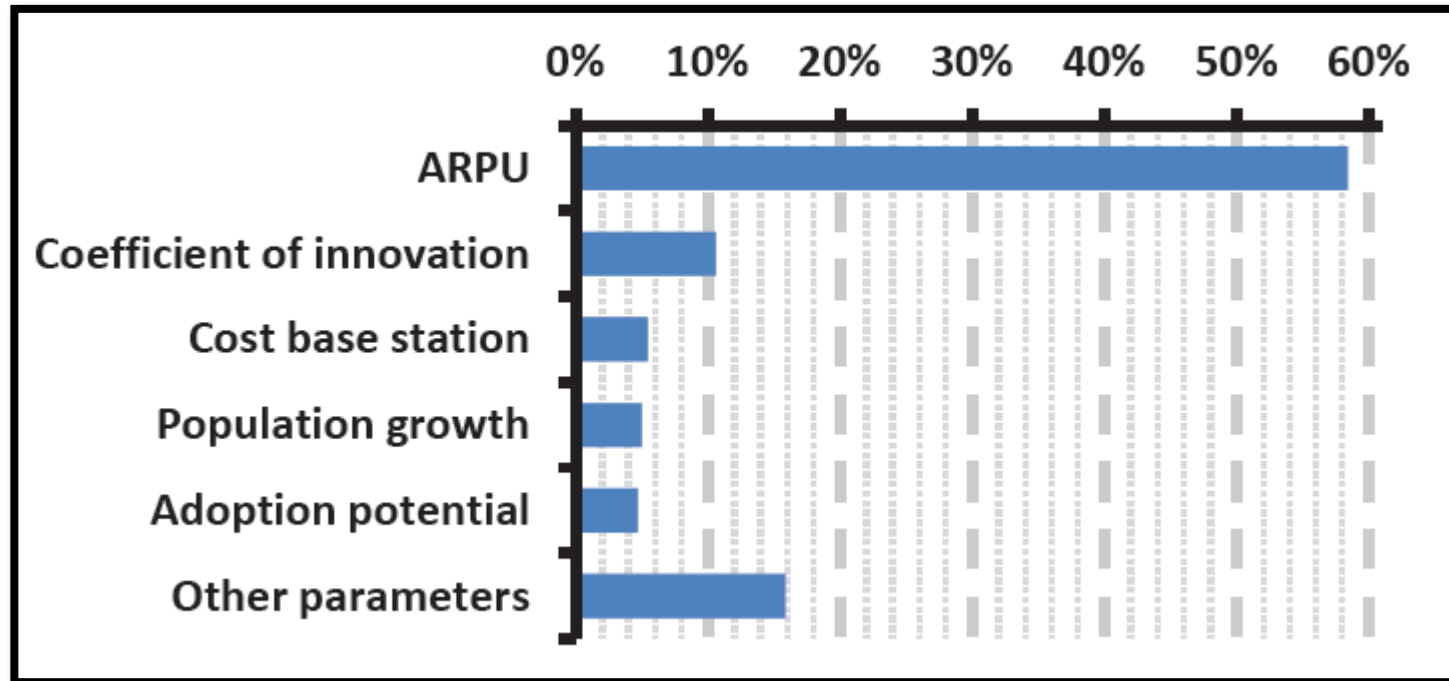
Ways to represent  
impact of input  
uncertainty in output

# Impact of uncertainty of input parameters on output values



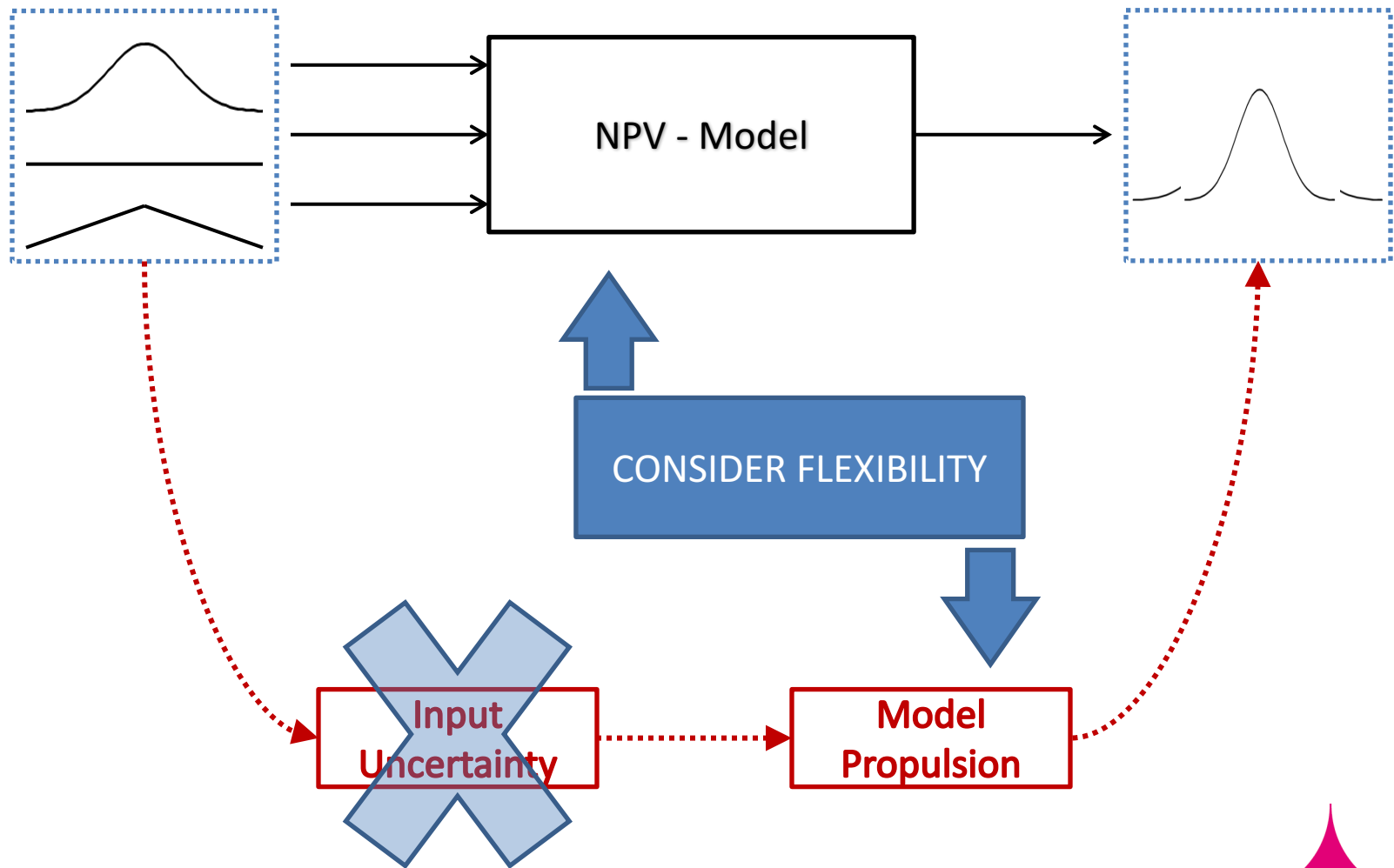
**Sample case**

# Impact of uncertainty of input parameters on output values



Crowdsourced Wi-Fi project Ghent

# Flexibility during the project course can help to reduce the effect of the uncertainty





# Types of flexibility

## ACT

### INVEST

- Expand geographic coverage
- Upgrade production capacity
- Improve product portfolio

### DISINVEST

- Decrease geographic coverage
- Disinvest in production capacity
- Withdraw from market

## LEARN

Postpone decision

Trial project

Market research

# Real Options

Indicate flexible options in real investment projects

# Origin of Real Options

## is in financial options



An option gives the buyer the **right** to buy or sell an **asset** for a **predetermined exercise price** over a **limited time period**.

A real option gives the manager the possibility to change the course of the project at a certain cost during the project's lifetime.

# What are Real Options?

## Real options

- Investment project over longer period
- Uncertain future
- Capture the value of managerial flexibility

# Real options as an extension of NPV

## Example

2 projects having the same NPV

Intuitively choose the project which gives the most possibilities later on

## Weak aspect of NPV evaluation

Assumes strict planning, with no flexibility

## Real projects

Anticipate on changing market circumstances

# Categories of real options based on the 7S framework

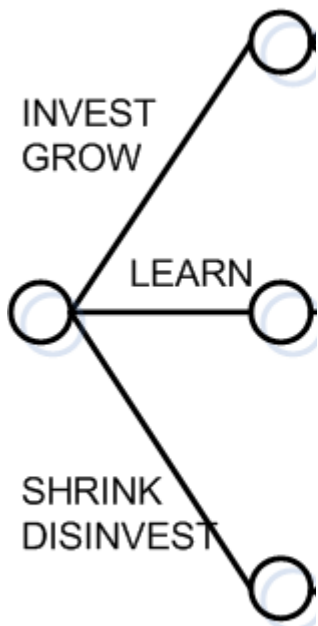
## LTE deployment case study

Roll-out in additional city

Deploy own backbone infrastructure

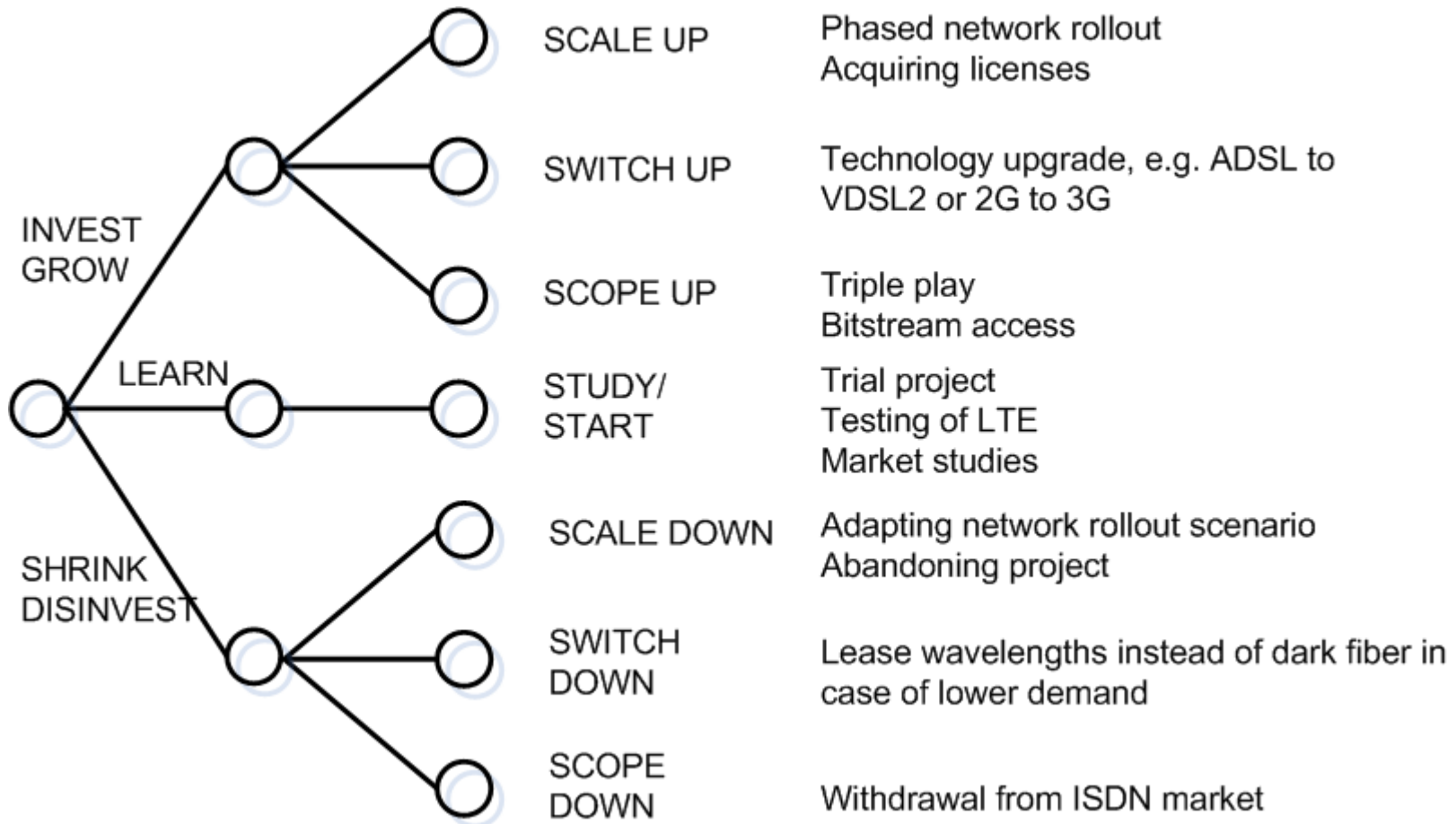
Differentiate between customers

Stop and sell off license



# Real Options in Telecom

## Telecom examples

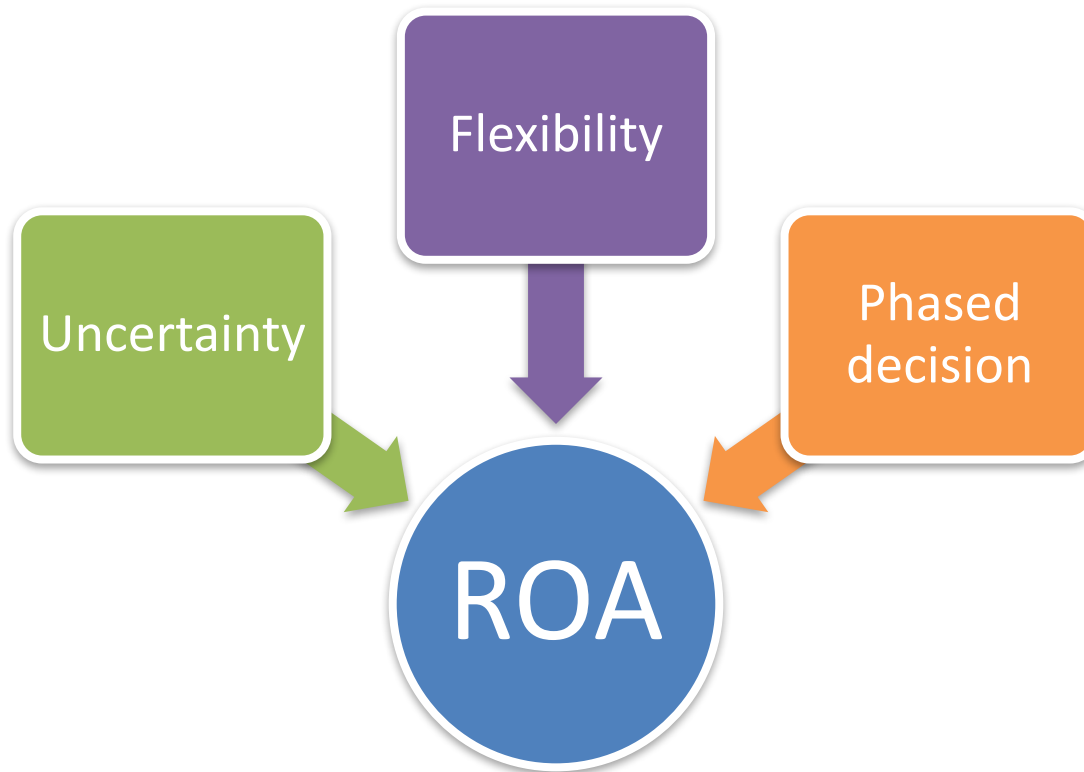


(Source: Copeland and Keenan, 1998)

Real Option Category	Real Option Type	Description	Telco examples
Invest/ grow	Scale up	Cost-effective sequential investments as market grows	Expand area of wireless coverage from cities to semi-urban areas
	Switch up	Switch products given a shift in underlying price/demand	Start offering dedicated wavelengths using DWDM in case of equipment price drops
	Scope up	Enter another industry cost-effectively	Start offering IPTV next to Internet connectivity
Defer/ learn	Study/start	Delay investment until more info/skill is acquired	Wait till competitor strategy is more clear
Disinvest/ shrink	Scale down	Shrink or shut down project as new info changes expected payoffs	Abandon one region if competitor drops prices there
	Switch down	Switch to more cost-effective and flexible assets as new info is obtained	Lease wavelengths instead of dark fiber in some regions of lower demand
	Scope down	Abandon operations in related industry if there is no further potential	Stop offering hot spot services if market does not take off



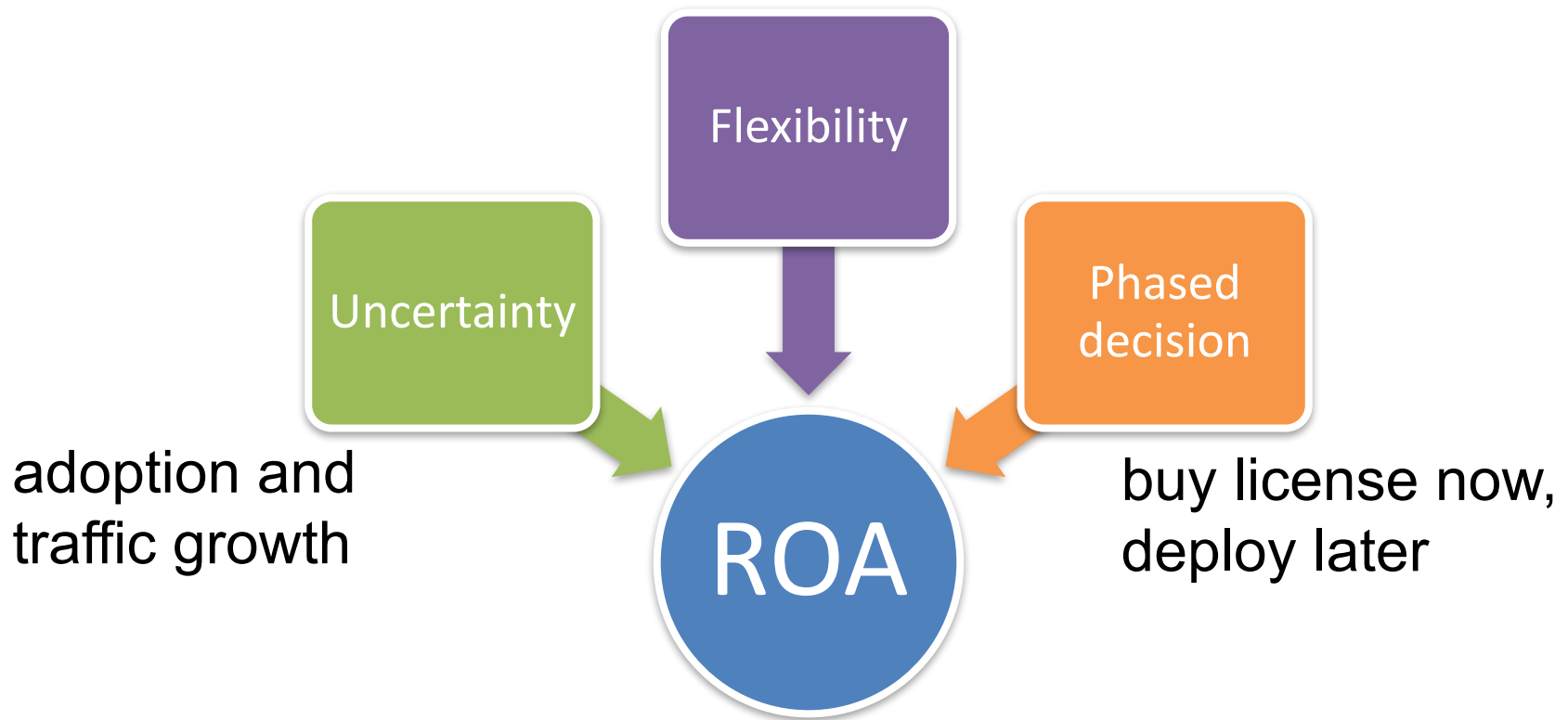
# Three conditions for a ROA



# Three conditions for a ROA

as illustrated for the case of LTE deployment in Gent

move to bigger city

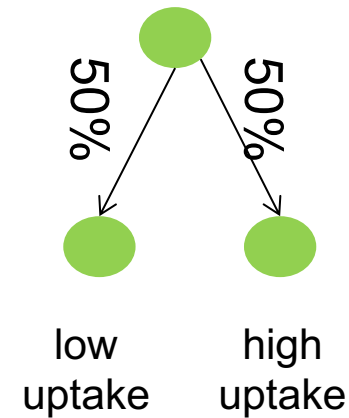


# Condition 1: uncertainty

## Uncertainty concerning initial assumptions

- Customer uptake
- Price evolutions
- ...

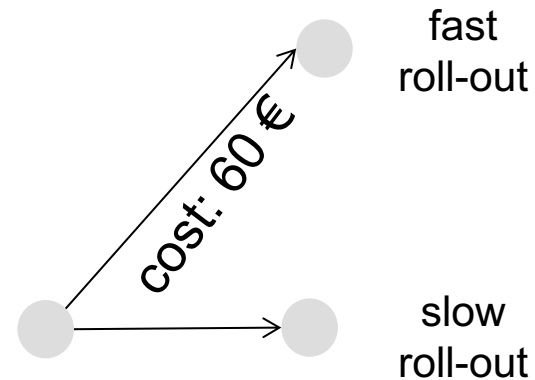
uncertain user uptake



# Condition 2: Flexibility

## Flexibility in decision

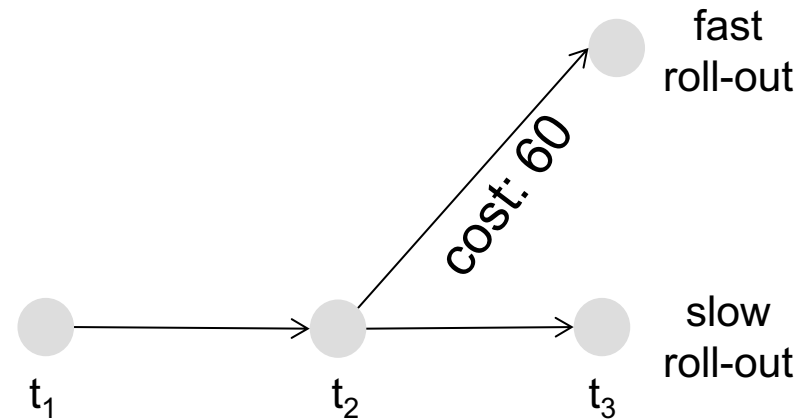
- According to the 7S framework
- Different paths available
- Example: fast or slow rollout



# Condition 3: Timing

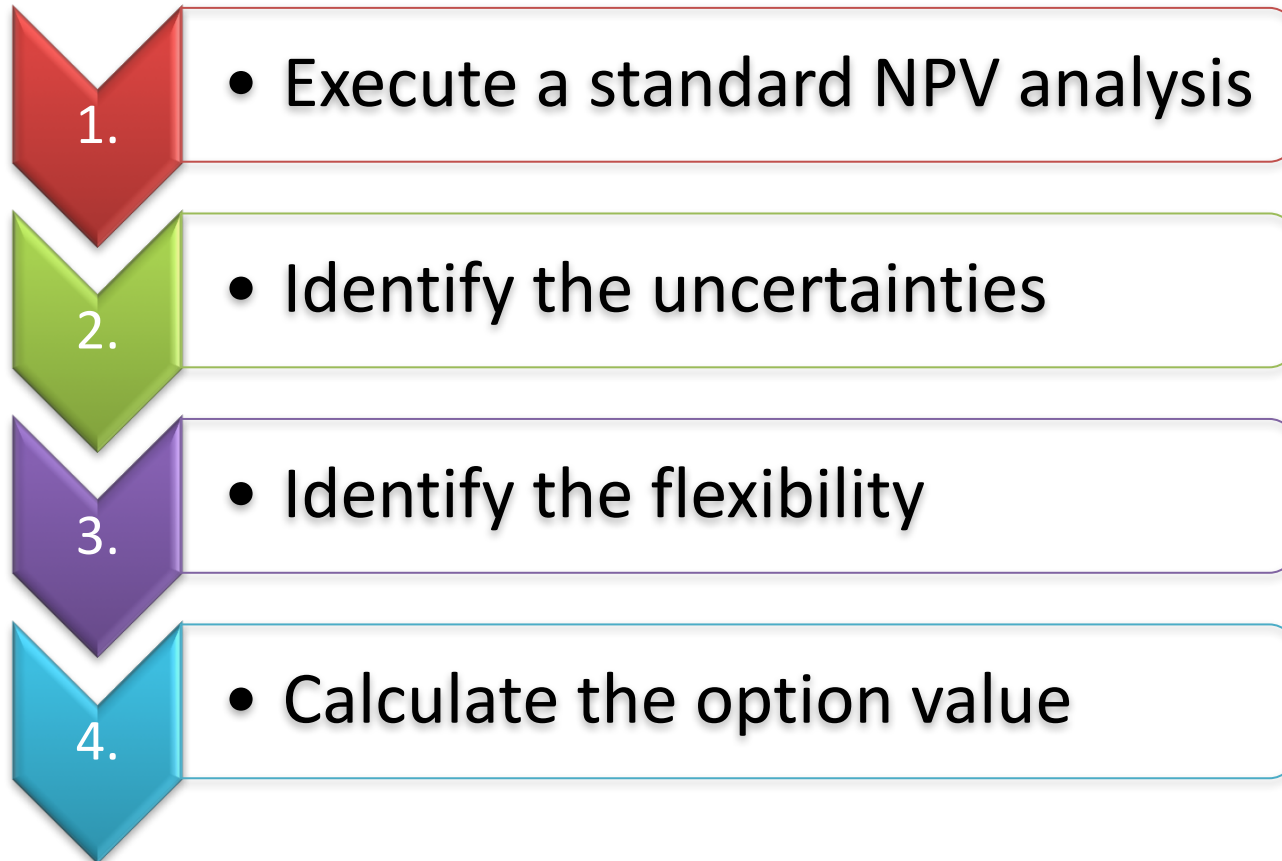
## Phased investment

Decisions to be made in future stages



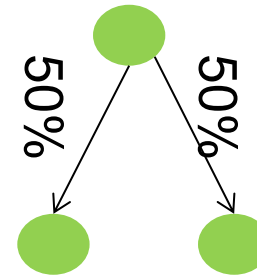
# Methodology for calculating option value

is starting from traditional static analysis



# 1. Execute standard NPV analysis

uncertain user uptake



low uptake

high uptake

● fast roll-out  
(cost 60 €)

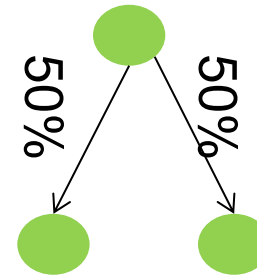
● slow roll-out  
 $t_3$

100€	400€
50€	150€

expected revenue

# 1. Execute standard NPV analysis

uncertain user uptake



low uptake      high uptake

● fast roll-out

● slow roll-out  
 $t_3$

40 €	340 €
50 €	150 €

NPV per scenario

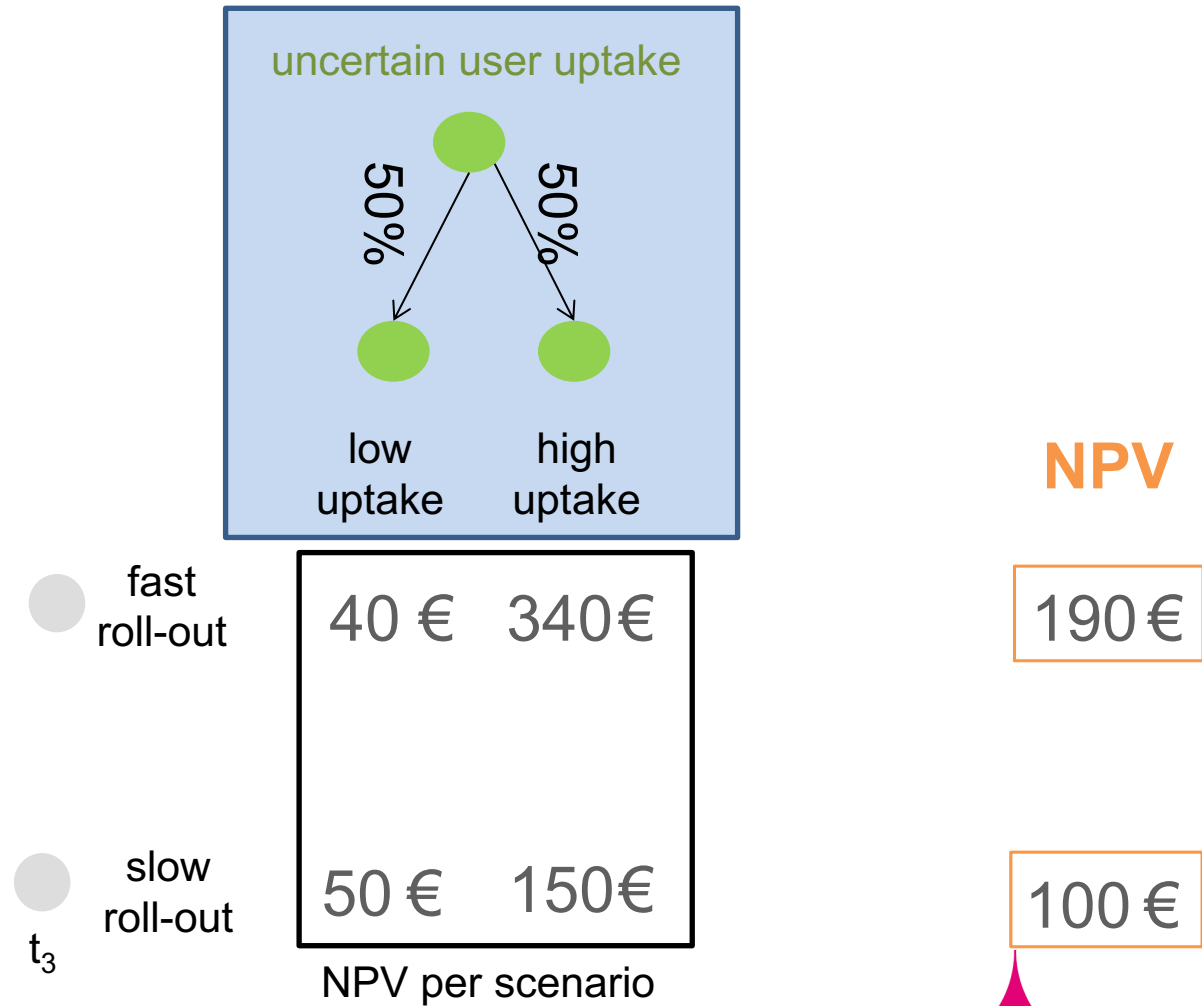
**NPV**

190 €

100 €

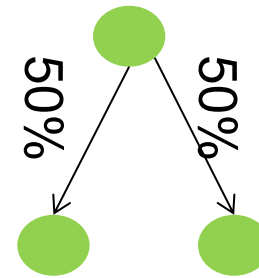


## 2. Identify the uncertainties

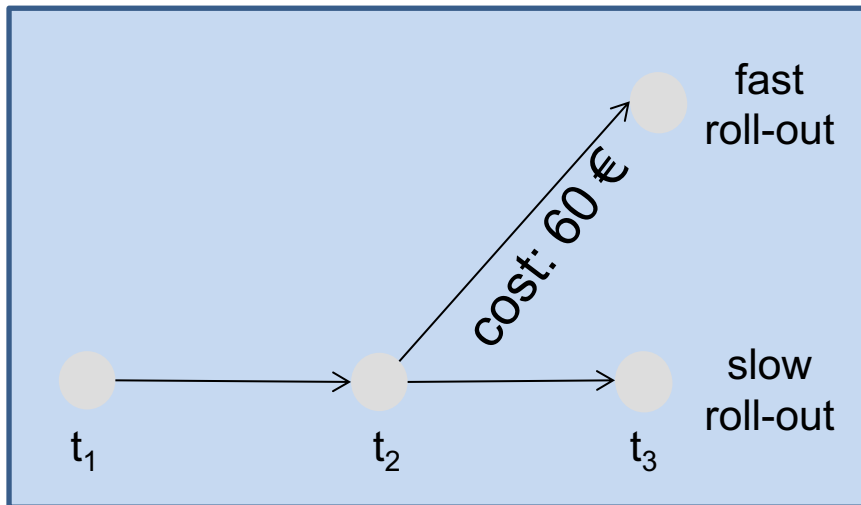


# 3. Identify the flexibility

uncertain user uptake



low uptake      high uptake



40 €	340€
50 €	150€

NPV per scenario

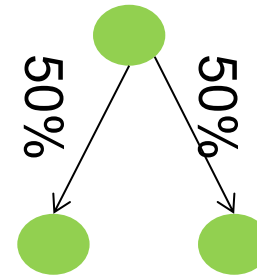
**NPV**

190 €

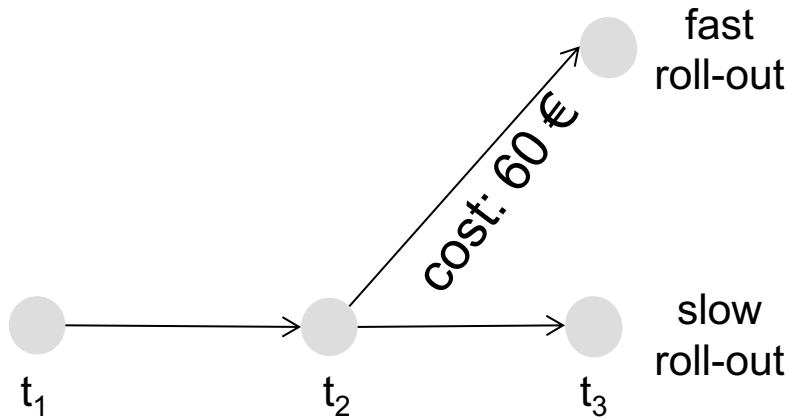
100 €

# 4. Calculate the option value

uncertain user uptake



low uptake      high uptake



<del>40 €</del>	340 €
50 €	150 €

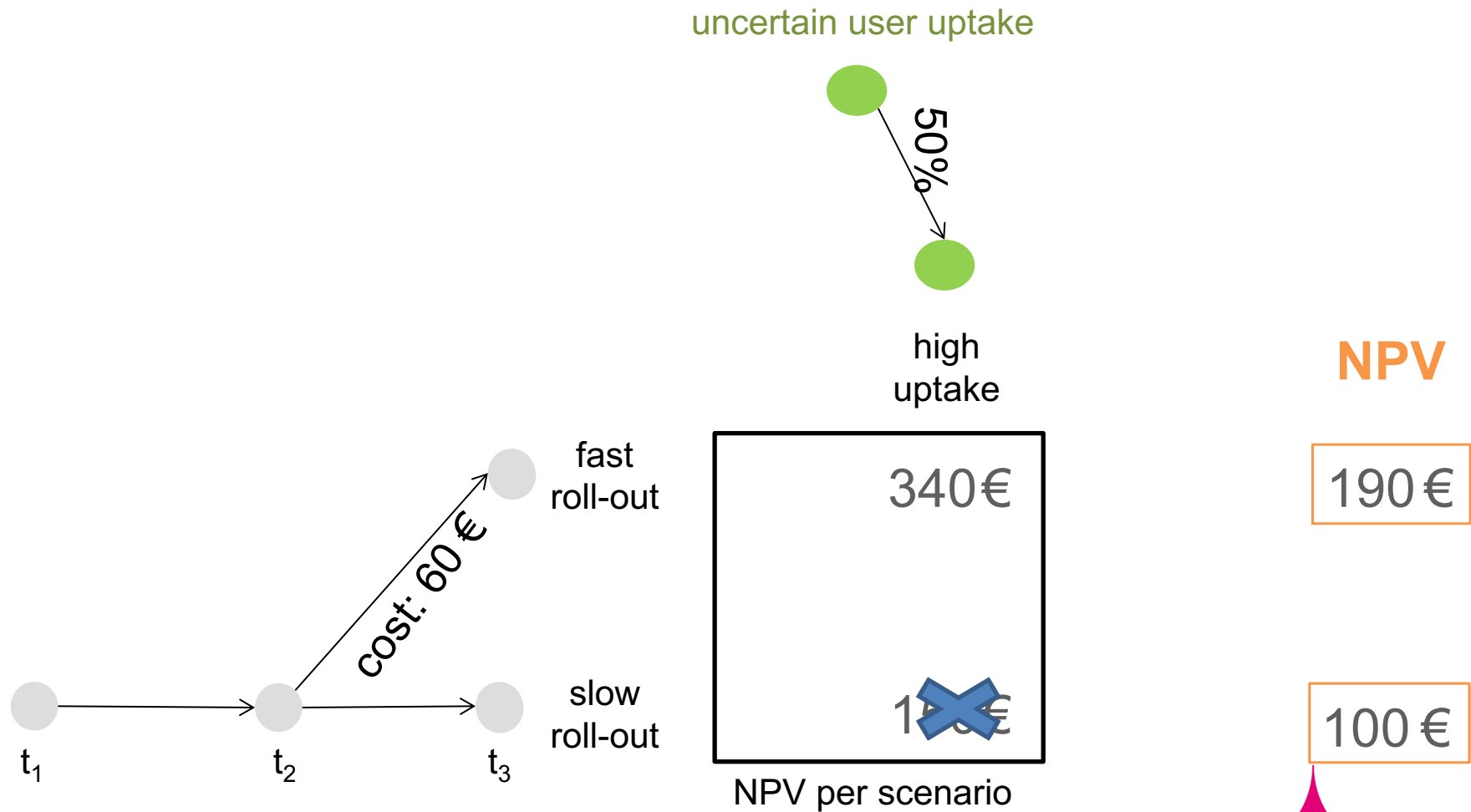
NPV per scenario

**NPV**

190 €

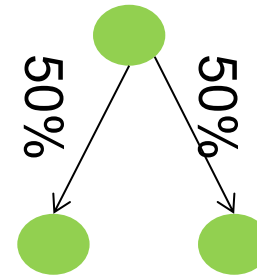
100 €

# 4. Calculate the option value

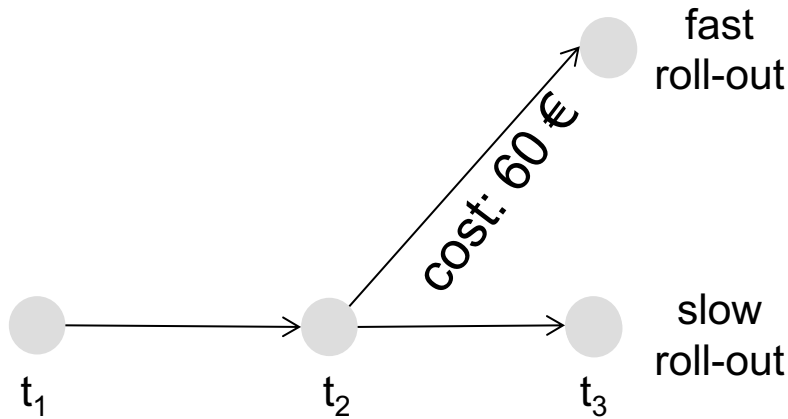


# 4. Calculate the option value

uncertain user uptake



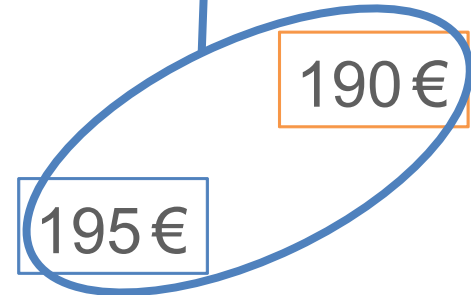
5€: value of option to wait compared to static fast case



	low uptake	high uptake
NPV per scenario	340€	100€
	50€	

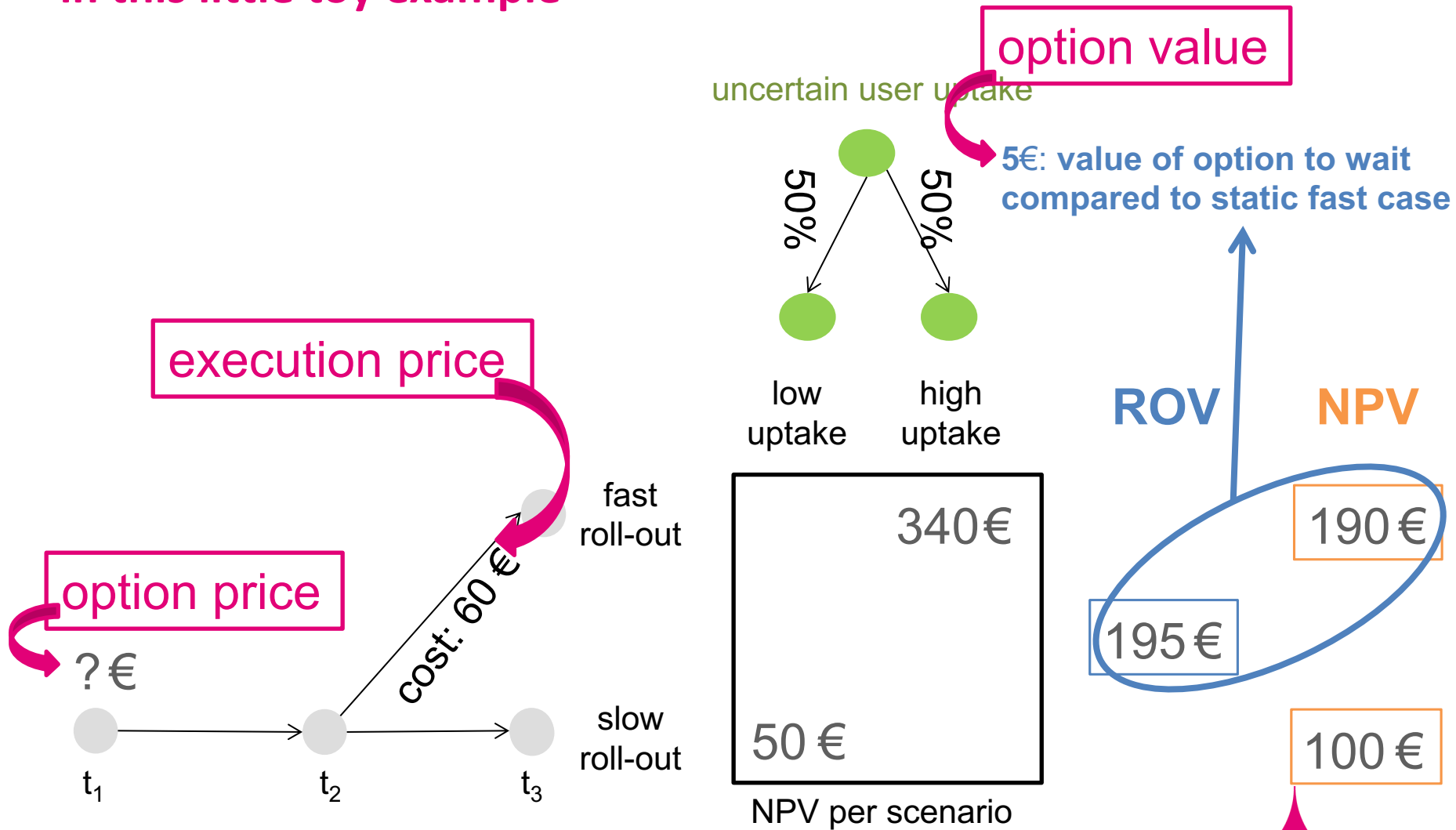
ROV

NPV



# Some options terminology

in this little toy example



# Some options terminology

## applied to the use case of LTE in Gent

option value

= what do you get by executing the option?

*e.g. revenues for Antwerp*

execution price

= what does it cost to execute the option once you have it?  
*e.g. deployment cost for Antwerp*

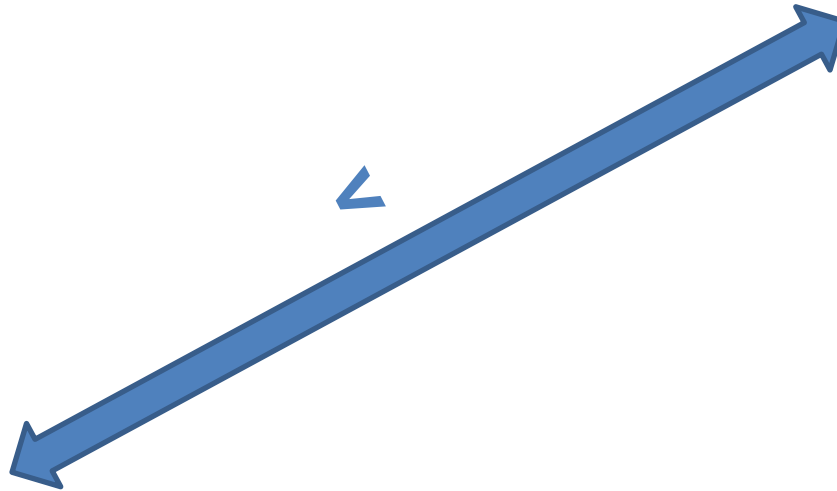
option price

= what does it cost to obtain the option?  
*e.g. bigger license for Antwerp*

# Evaluation a project with flexibility boils down to comparing option value to option price

option value

= what do you get by executing the option?  
*e.g. revenues for Antwerp*



option price

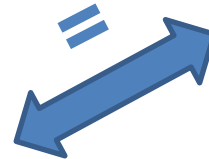
= what does it cost to obtain the option?  
*e.g. bigger license for Antwerp*



# Determining the value of an option

by comparing execution price with real project value

$$\text{Max}(0, \text{Project value} - \text{execution price})$$



option value

= what do you get by executing the option?

*e.g. revenues for Antwerp*

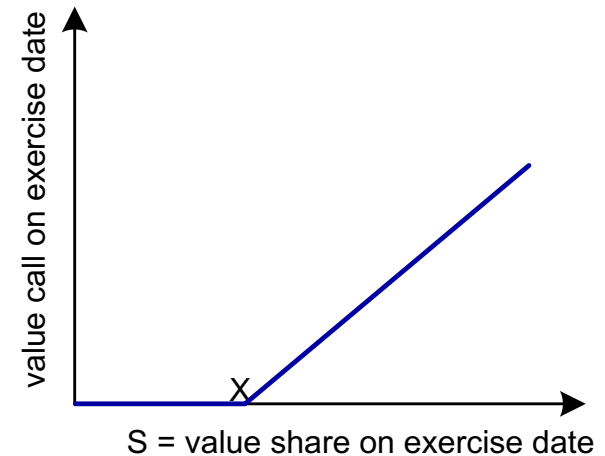
# Determining the value of a call option by comparing option price to stock value

- Call option = right to buy (a stock)

- Predetermined exercise price:  $X$
- Market value of the stock on exercise date:  $S$

- Value on exercise date

- $\text{MAX}(0, S - X)$
- always positive value



- Value of option = end value + time value

- End value = value if today was exercise date
- Time value
  - Grows with a growing time to maturity
  - Grows with volatility of share value
  - Small when difference between  $S$  and  $X$  is big

# Some more terminology originating from financial options

## European option

can only be exercised on the exercise date

## American option

can be exercised *till* the exercise date

## Call option

option holder has right to *buy* the asset

## Put option

option holder has right to *sell* the asset

## Option price = option premium

Price to acquire the option, price to acquire to right

## Exercise price = strike price

Price for which option holder can exercise the option (fixed)

# Several calculation methods

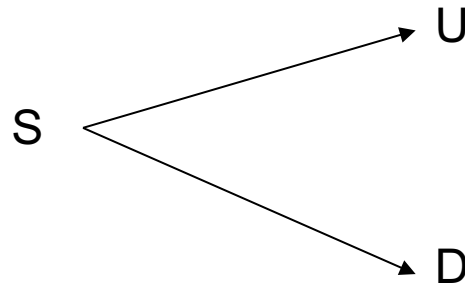
for option values can be found in literature

- Binomial tree model
  - Only discrete values for input
  - See toy example before
- Black and Scholes model
  - From financial options
  - Mathematical model
- Monte Carlo Analysis
  - Simulation based method
  - Spreadsheet approach
  - See demo in a minute

# Binomial tree option valuation

is the most intuitive method

- For European call option
- Assumes 2 possible end values



- Can be expanded for more time periods
  - software needed

# Black and Scholes option valuation

is not intuitive at all

Formula for European call option

$$C = SN(d1) - Xe^{-rt} N(d2)$$

$$d1 = \frac{\ln(S/X) + rt + \sigma^2 t / 2}{\sigma \sqrt{t}}$$

$$d2 = \frac{\ln(S/X) + rt - \sigma^2 t / 2}{\sigma \sqrt{t}}$$

N(d) = cumulative normal distribution

X = exercise price of the option

S = current value of the share

$\sigma^2$  = variance of the return of the share per time period

r = risk free interest rate

## Assumptions

arbitrage-free pricing: financial transactions that make immediate profit without any risk do not exist (there is a general economic equilibrium)

stock prices  $S$  follow Brownian motion (random walk)

$$dS = \mu S dt + \sigma S dw$$

# Parameters used in Black and Scholes formula for financial versus real options

	<b>Stock option</b>	<b>Real option</b>
$X$	exercise price of the option	investments required to carry out the project
$S$	value of the underlying stock	NPV of the cash flows generated by the investment project
$\sigma$	volatility of the stock	risk grade of the project
$r$	the risk-free interest rate	risk-free interest rate
$t$	life time of the option	time period where company has the opportunity to invest in the project

# Monte Carlo analysis for option valuation

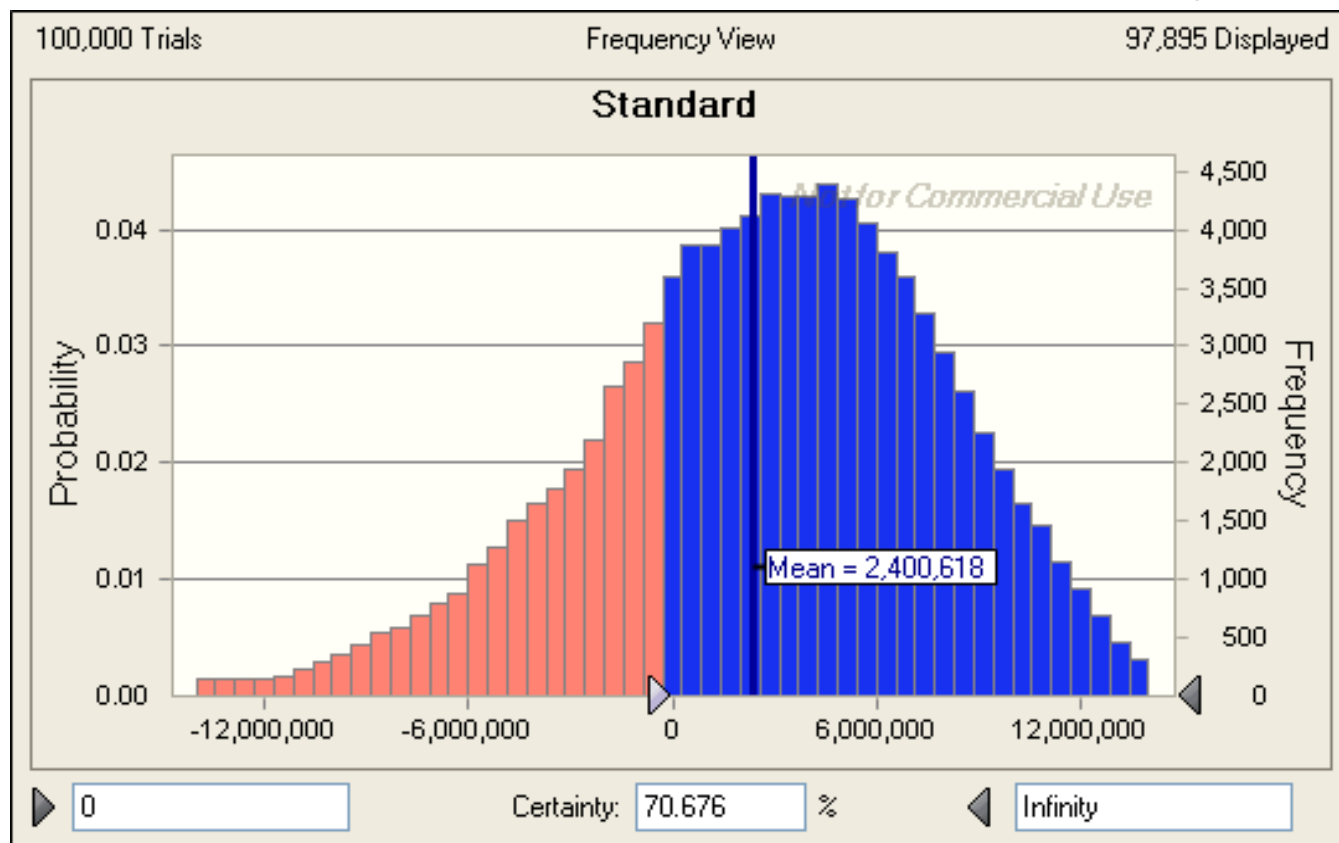
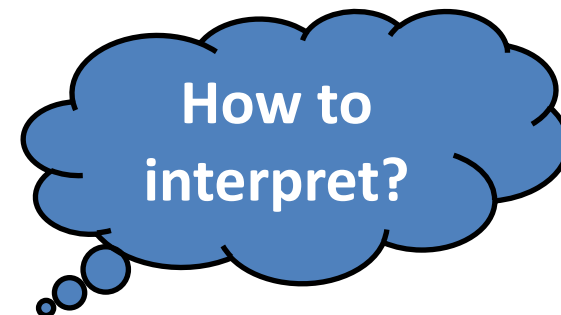
demonstrated in demo



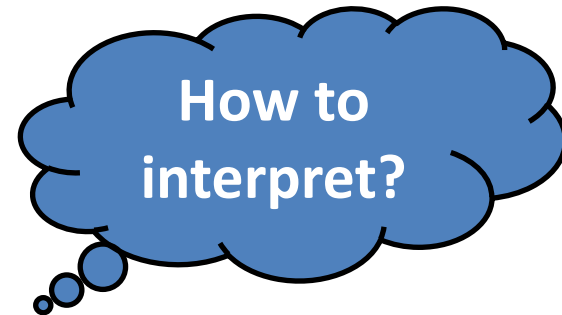
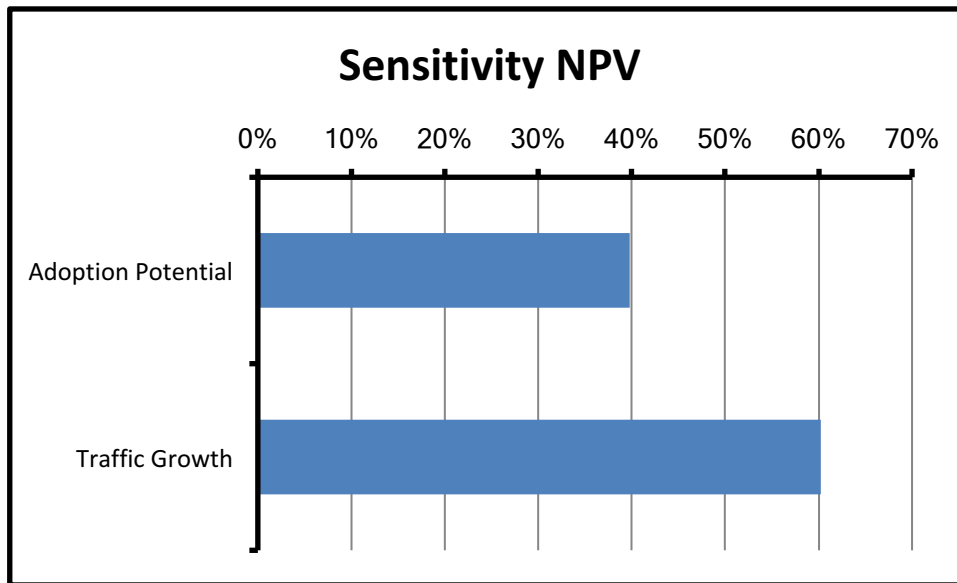
# Sensitivity and Uncertainty Analysis

How do we measure the impact of uncertainty and flexibility?

# Histograms

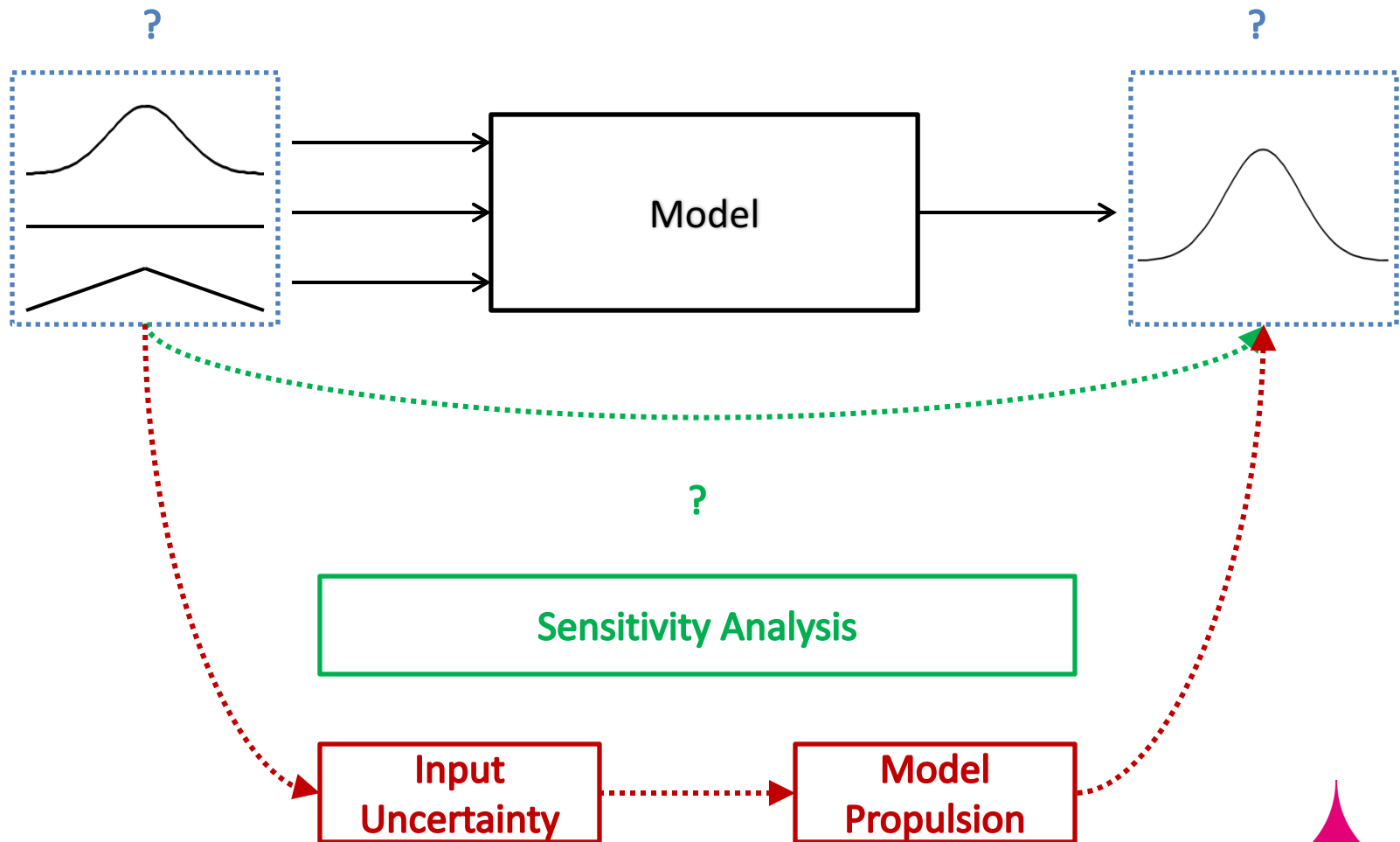


# Tornado charts



# Uncertainty analysis

## and the meaning of sensitivity analysis in there



# Comparison

## UNCERTAINTY ANALYSIS

- OBJECTIVE: **Quantify** and describe uncertainty.

- USES: **Descriptive Statistics** from Monte Carlo analyses
  - Expected Value
  - Variance
  - Higher order moments
- → **Histograms**

## SENSITIVITY ANALYSIS

- OBJECTIVE: **Relate** input and output uncertainty
  - Research prioritization
  - Model simplification
  - Factor mapping

- USES: **Sensitivity Indices** from Monte Carlo analyses
  - Based on Rank Cor.
  - Based on variance
  - Based on MC Filtering
  - Based on Lin.Reggression
  - → **Tornado charts**

# Relevance to ROA? Measure flexibility impact

- Using: **Expected value of model's output**
  - measures: **global profitability**
  - One would expect that adding ROA to the business model would increase the model's expected NPV since it allows the manager to steer away from scenario's depleting NPV
- Using: **Variance of model's output**
  - measures: **global uncertainty**
  - We would expect that the total variance of the project would have dropped since the manager can steer away from extreme outcomes.

# Relevance to ROA? Measure flexibility impact

- Using: **Conditional Variance and Mean Value**
  - measures: **Risk**
  - What is my expected loss in the worst case scenario?
  - What is the confidence interval around this estimate?
- Using: **First Order sensitivity Indices**
  - measures: **Relative importance inputs**
  - Rank correlation based (Crystal Ball)
  - We would expect that the relative importance of some uncertainty sources has switched. Against some you can react against others you can't.

# Let's return to our case: what did we expect?

## ↓ Variance NPV

- Lower overall uncertainty

## ↑ Expected value NPV

- Global profitability increases
- Positive option value

## ↓ Conditional Var & EV in negative scenario

- Lower overall risk

## → Truncated distribution

- Exit option



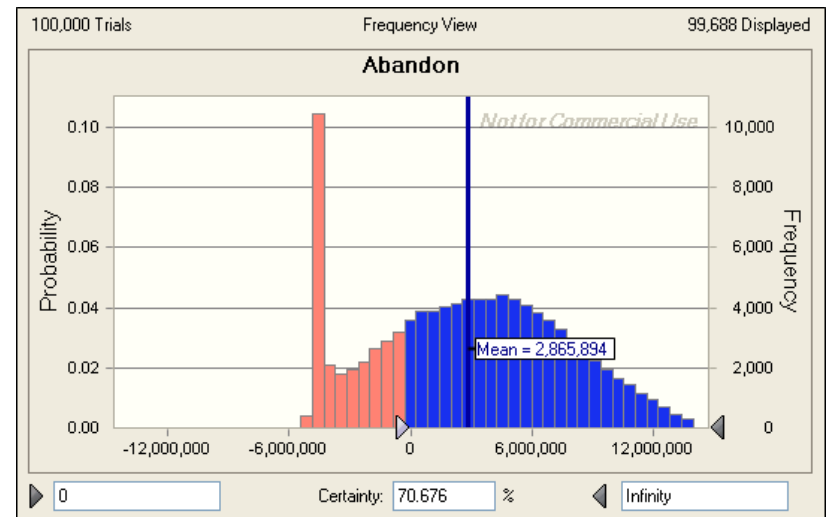
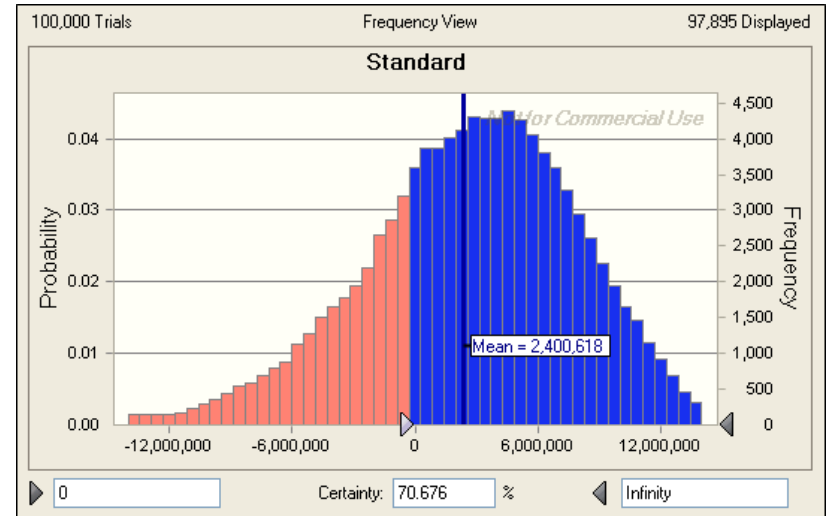
# Let's return to our case: evaluation

## No option:

- Expected NPV: 2.4m
- S.E. NPV: 5.8m

## Abandon option:

- Expected NPV: 2.9m **(+19%)**
- S.E. NPV: 4.7m **(-19%)**
- Truncated distribution **(visual)**
- Expected negative NPV **(+20%)**



# Let's return to our case: what did we expect?

## ↓ Sensitivity Indexes

- Certain input uncertainty is made less important

## → Switch in relative importance of uncertainty

- Flexibility has more effect on certain types of uncertainty

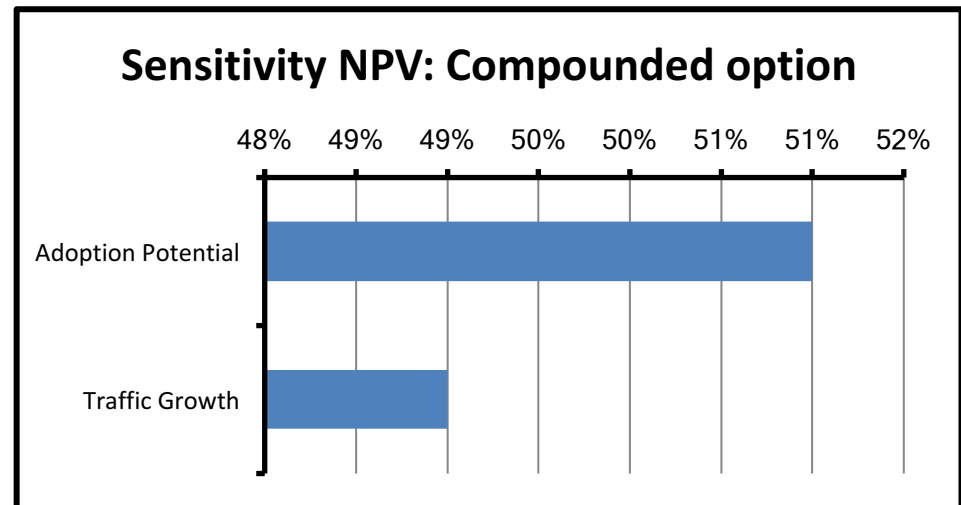
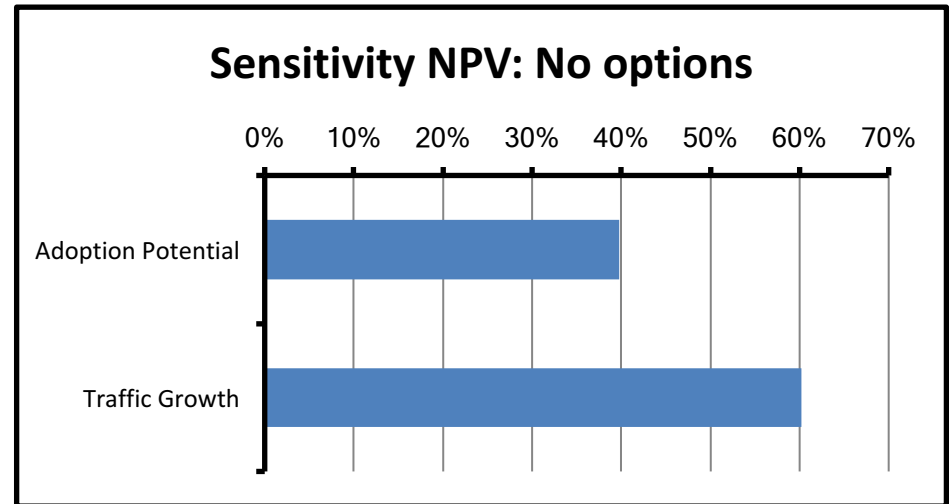
# Let's return to our case: evaluation

## No option:

- Adoption potential: 39%
- Traffic Growth: 61%

## Compounded option:

- Adoption potential: 51%
- Traffic Growth: 49%



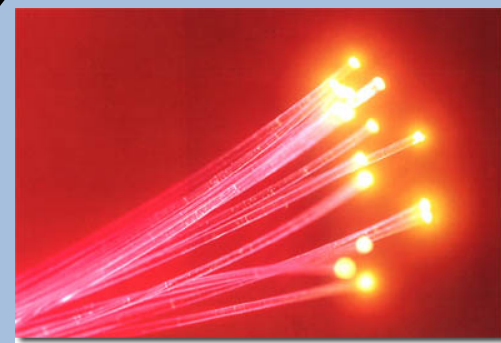
# Different case studies

What cases can RO be applied to?

# Case study overview

where we applied ROA before

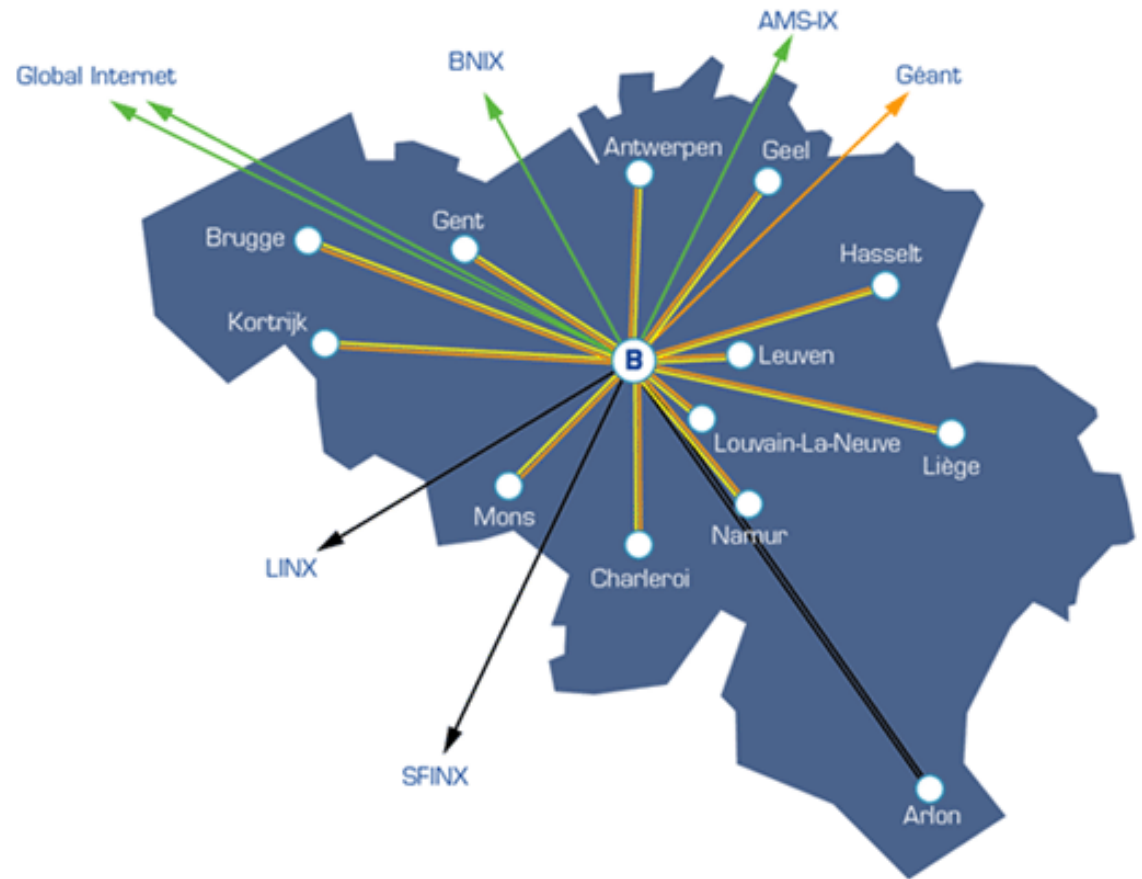
1. Make or lease fiber network?
2. Which areas to deploy wireless sensor network?
3. Optimal cabinet size for FTTcab roll-out?



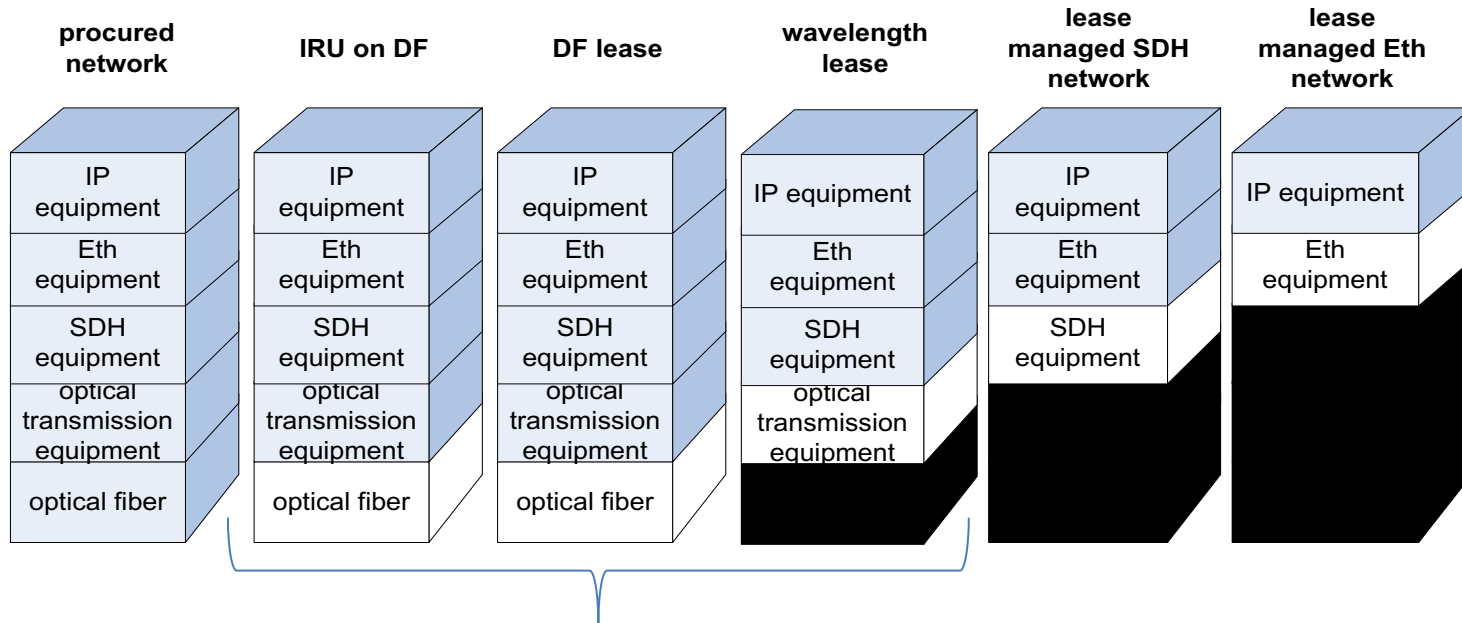
Do I install my own backhaul or do I lease dark fiber?

# Belgian network

where a fiber topology is needed



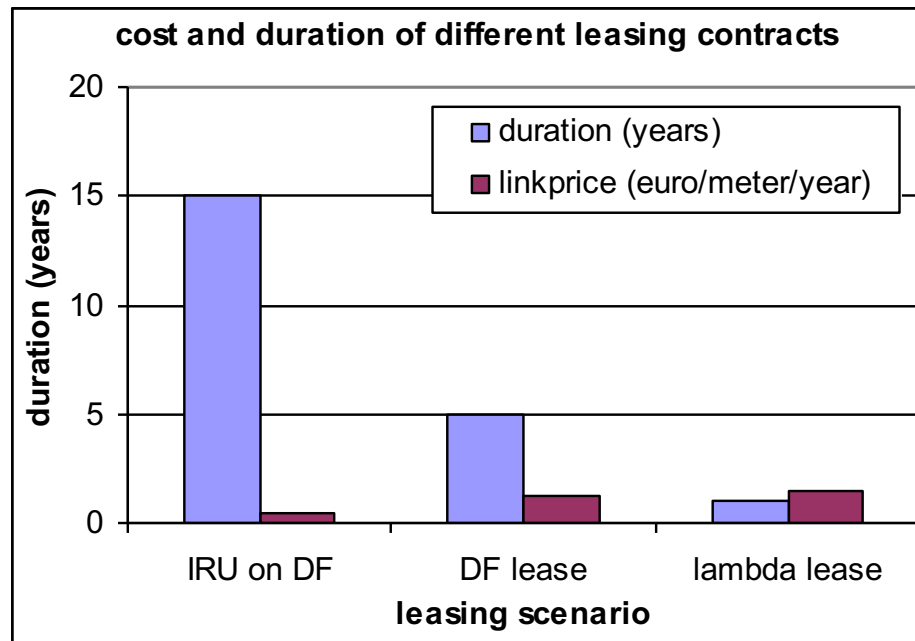
# Several ownership models for optical network deployment





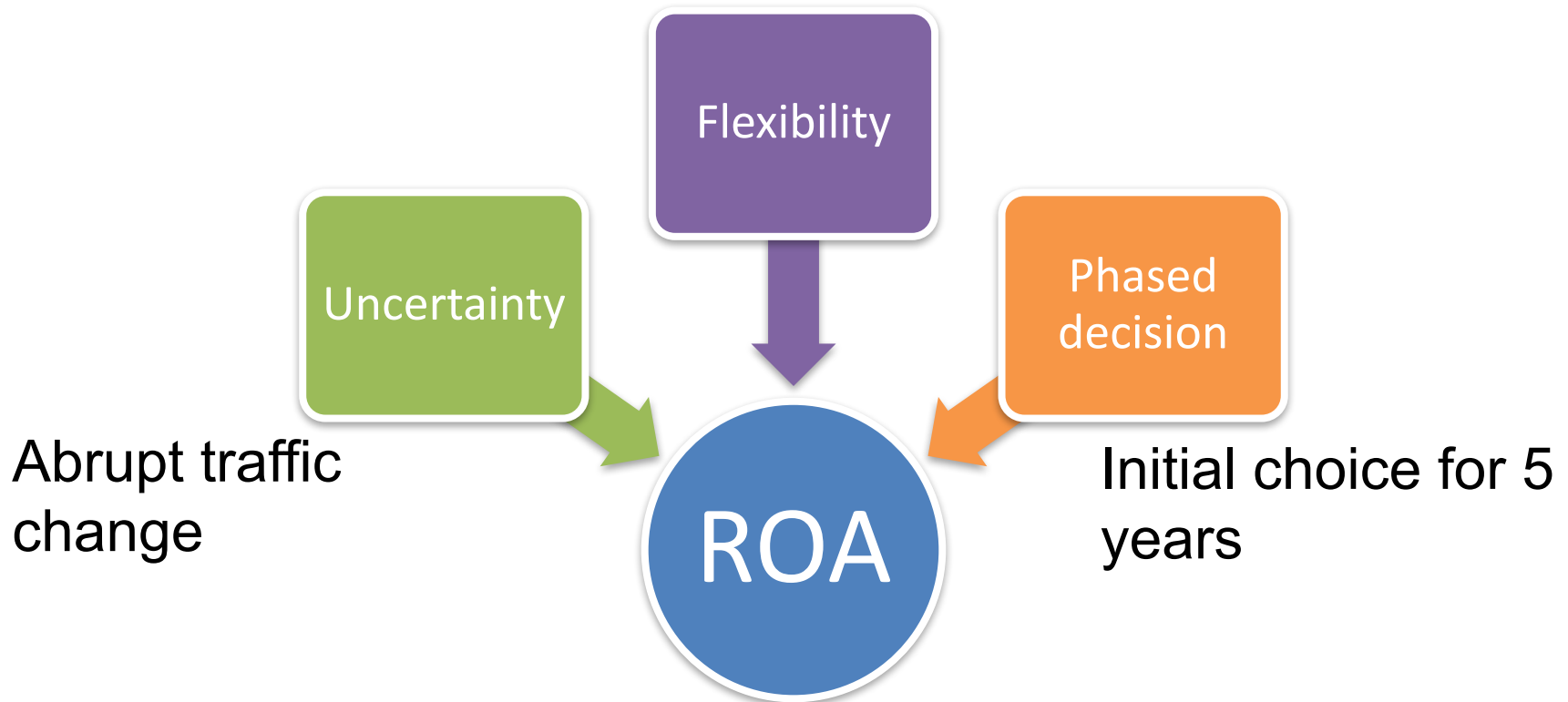
# Different ownership models

have different input information on cost and duration

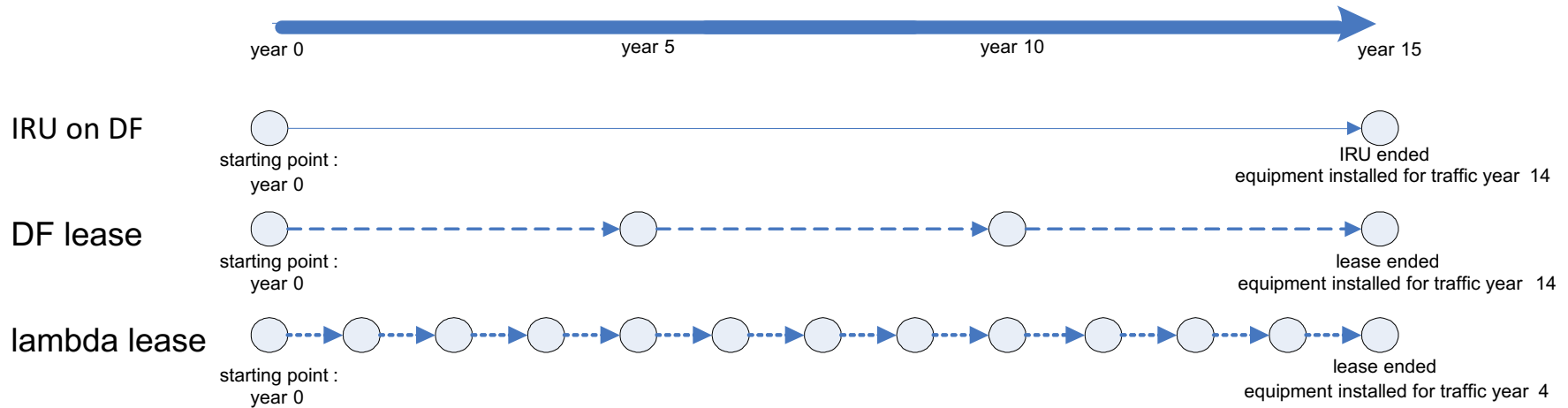


# Three conditions for a ROA for the case Make or lease dark fiber

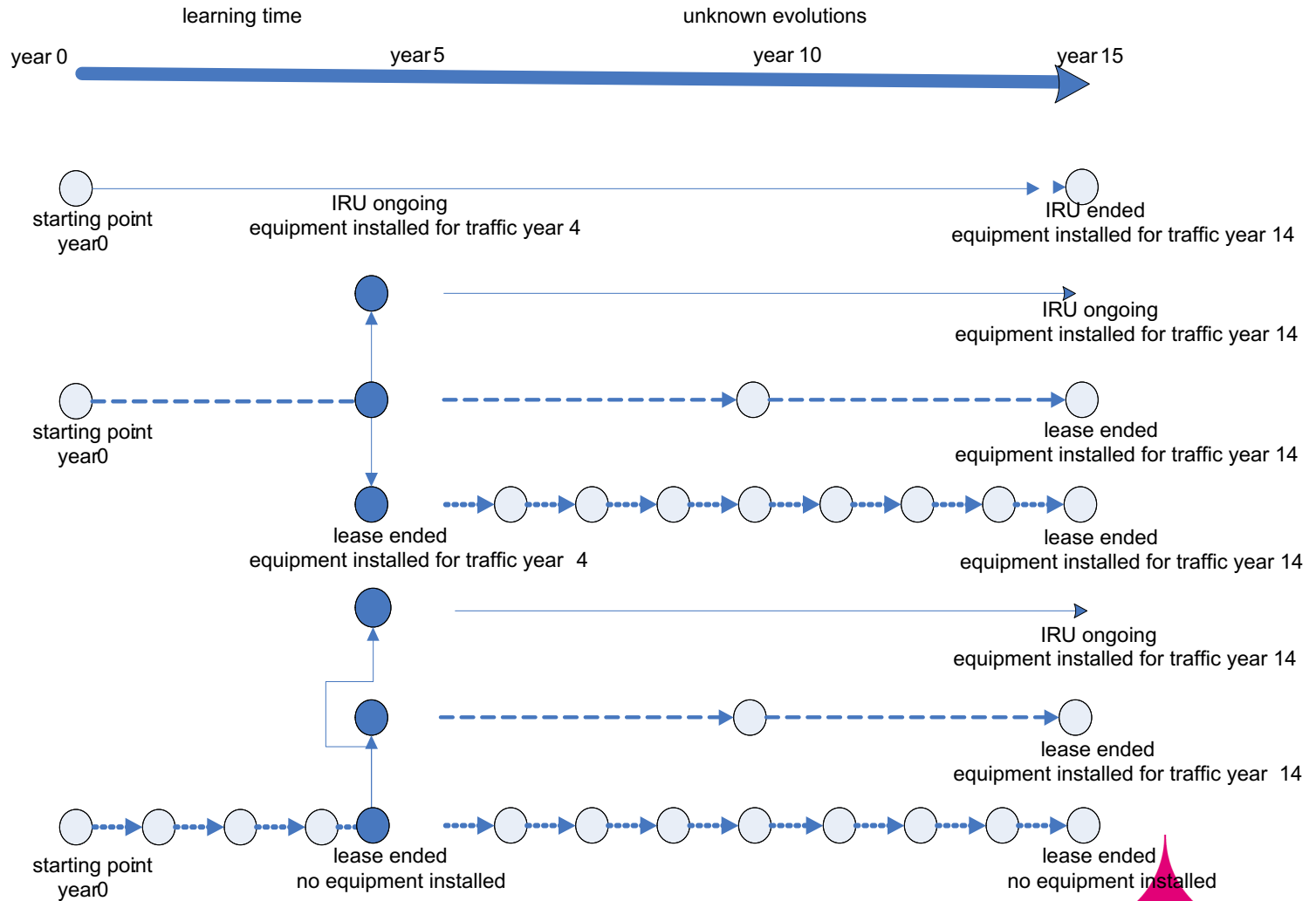
Flexibility within ownership model  
Possibilities to change model at contract end



# In-/decrease capacity within certain scenario is a first form of flexibility

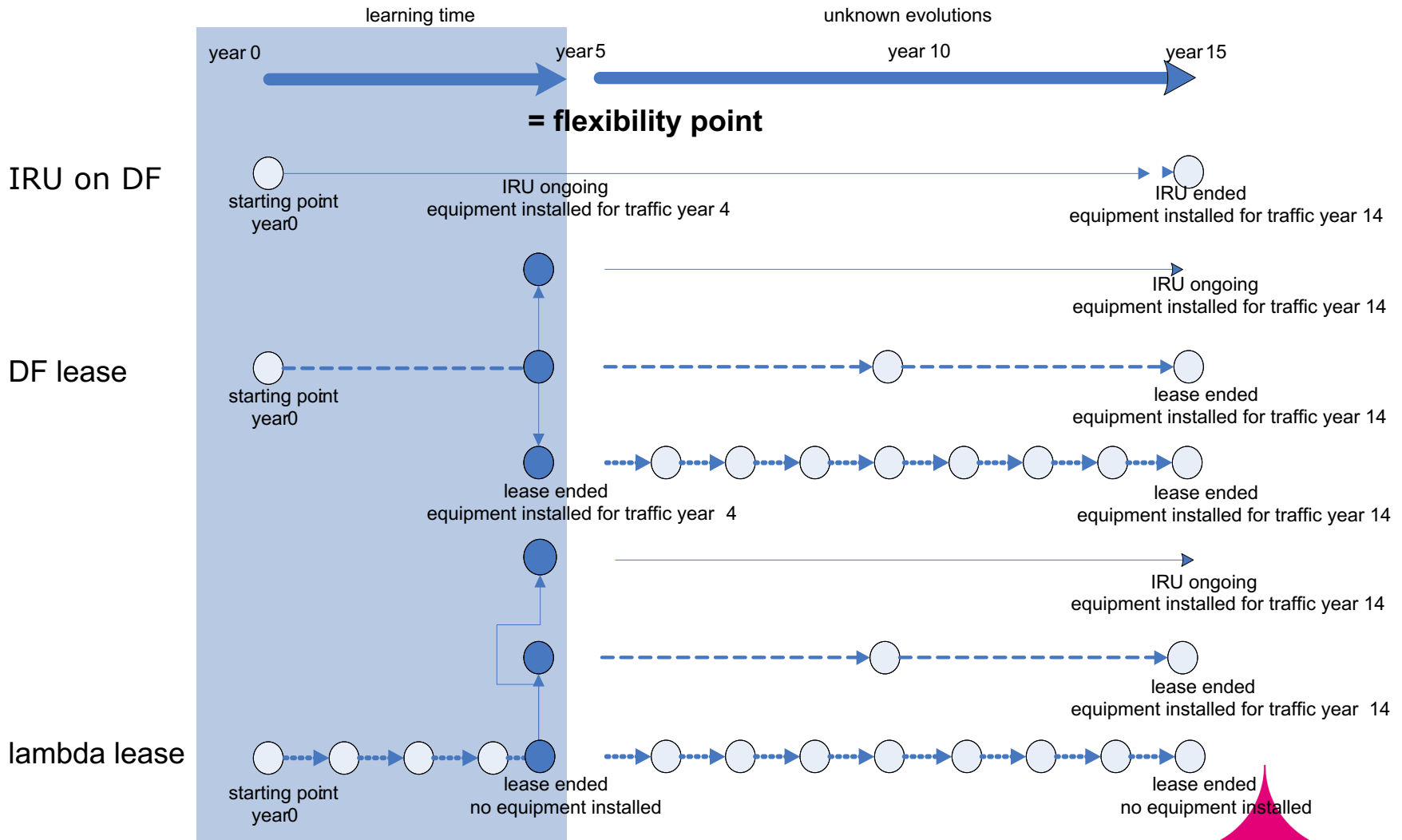


# Switch between scenarios at contract end is second form of flexibility

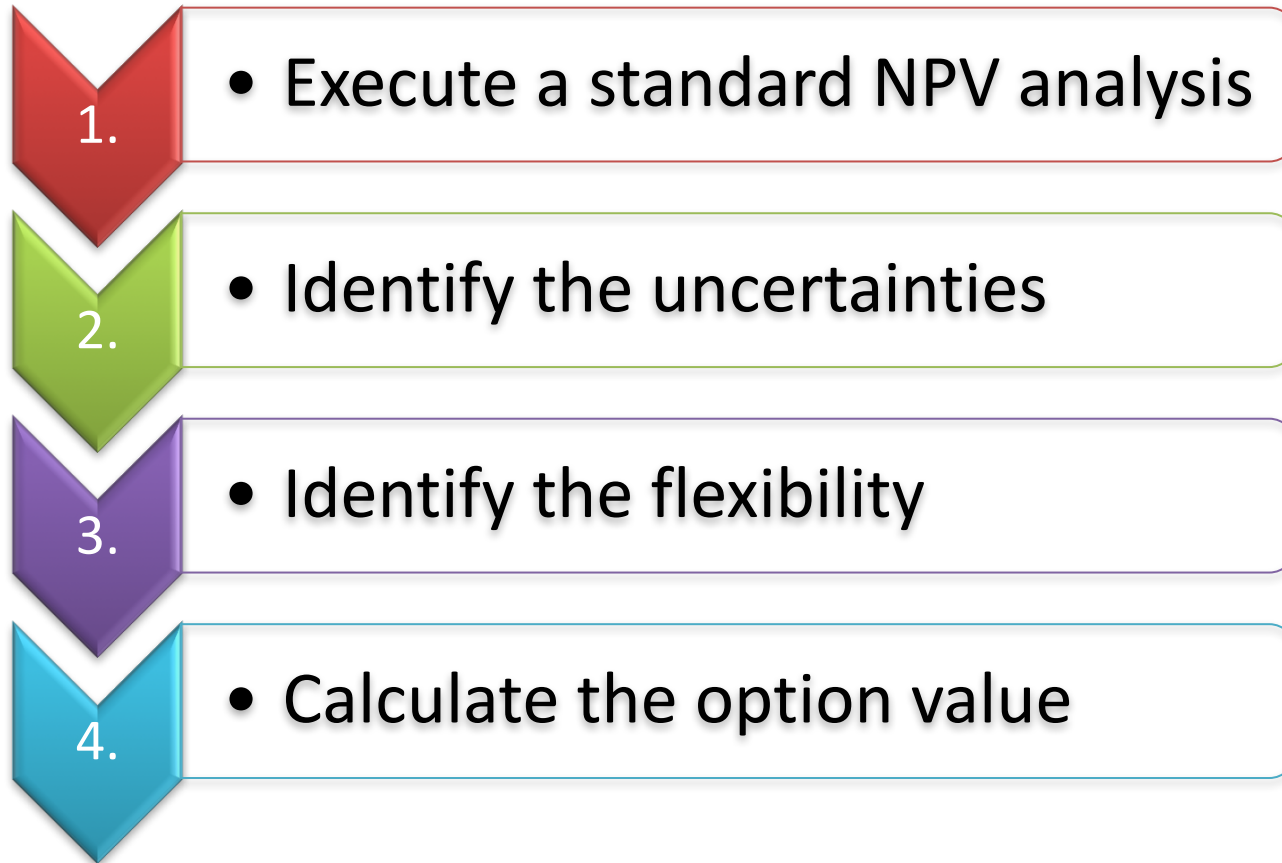


# Phased decision

is included via flexible upfront decision



# Methodology for calculation option value based on binominal tree for this case



# Formulae behind the evaluation

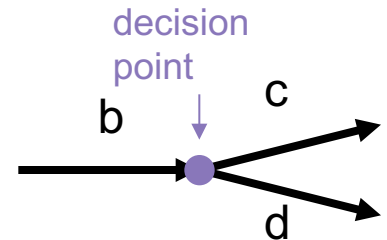
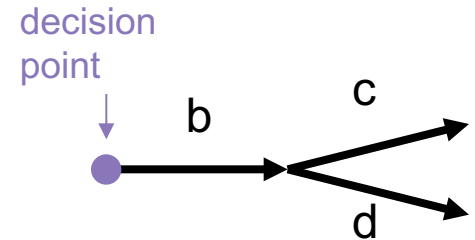
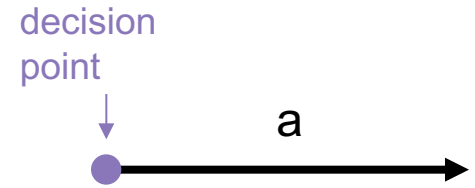
show the difference with and without option

**NO REAL  
OPTION**

Plan which is cheapest on average  
over all scenarios

**WITH  
REAL  
OPTION**

Plan which is cheapest on average  
taking into account flexibility during  
course of deployment

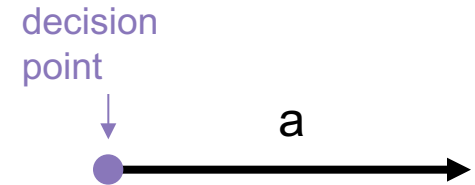


# Formulae behind the evaluation

## show the difference with and without option

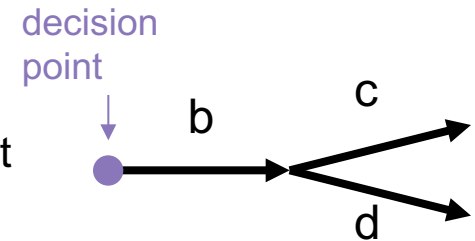
- Single deployment path:  
no flexibility (average over all uncertain scenarios)

$$E_{\text{uncertain traffic evolutions}}[\text{cost}(a)]$$



- Path with the alternative subpaths
  - Choice between alternatives is to be made at the beginning of the deployment path: no flexibility to react to changes happening during first subpath

**NO REAL OPTION**

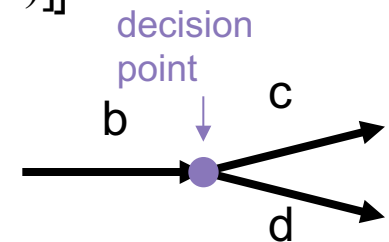


$$E_{\text{uncertain traffic evolutions}}[\text{cost}(b)] + \min[E_{\text{uncertain traffic evolutions}}[\text{cost}(c)], E_{\text{uncertain traffic evolutions}}[\text{cost}(d)]]$$

**WITH REAL OPTION**

- Choice between alternatives is only made at the end of first subpath: true flexibility

$$E_{\text{uncertain traffic evolutions}}[b + \min[\text{cost}(c), \text{cost}(d)]]$$



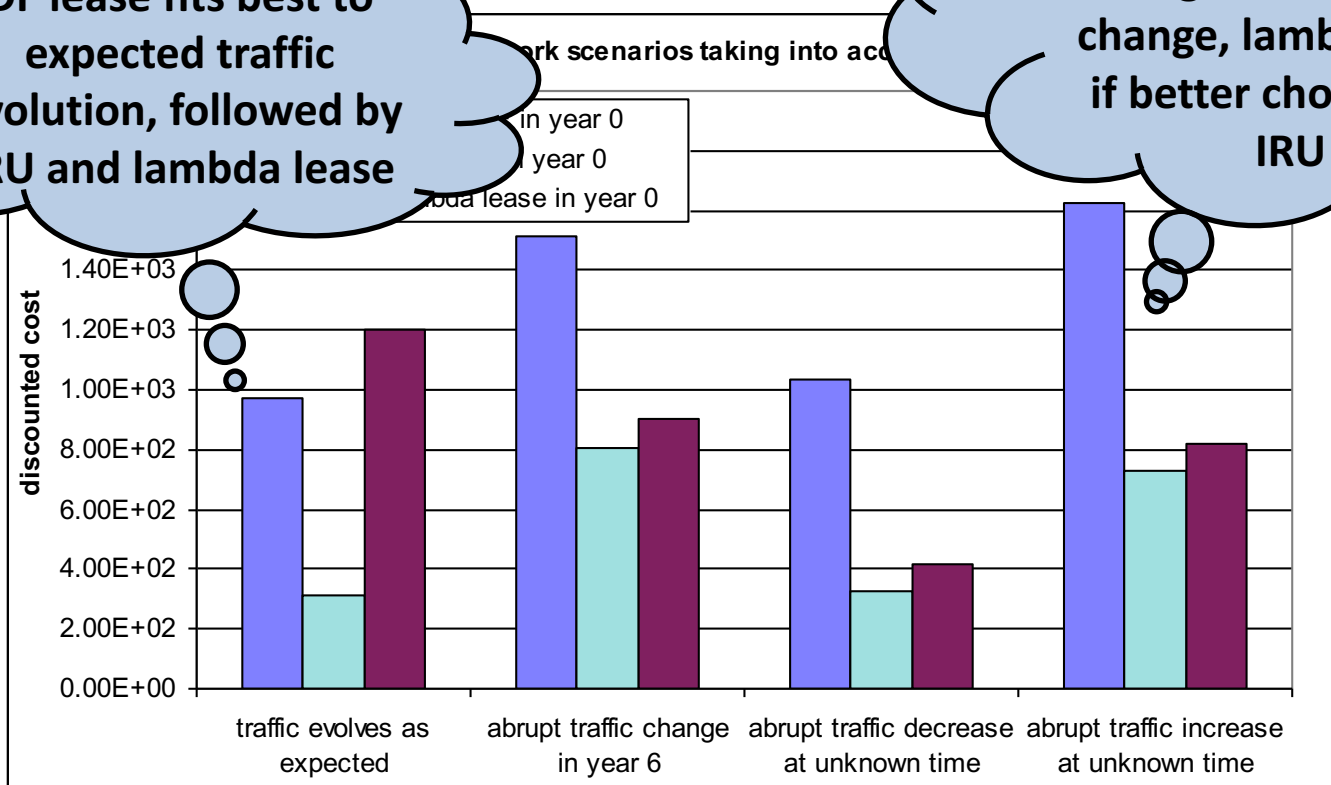


# Impact of flexibility

shows that lambda lease adopts better to change than IRU

DF lease fits best to expected traffic evolution, followed by IRU and lambda lease

If there are abrupt changes in the traffic change, lambda lease is better choice than IRU



# Case study summary

## Make or lease fiber network?

- Type of uncertainty (4 types of threats)
  - Operational Threats: Traffic Intensity uncertainty
- Option type (7S)
  - Switch option
- Calculation method
  - Binomial tree
  - Monte Carlo simulation
- Case results
  - Dark fiber lease outperform IRU on case study
  - Situation gets worse in case of abrupt changes

# Case study overview

where we applied ROA before

1. Make or lease fiber network?
2. Which areas to deploy wireless sensor network?
3. Optimal cabinet size for FTTcab roll-out?



Trial phase in  
a small area



Do I install the  
sensors in the  
entire city?

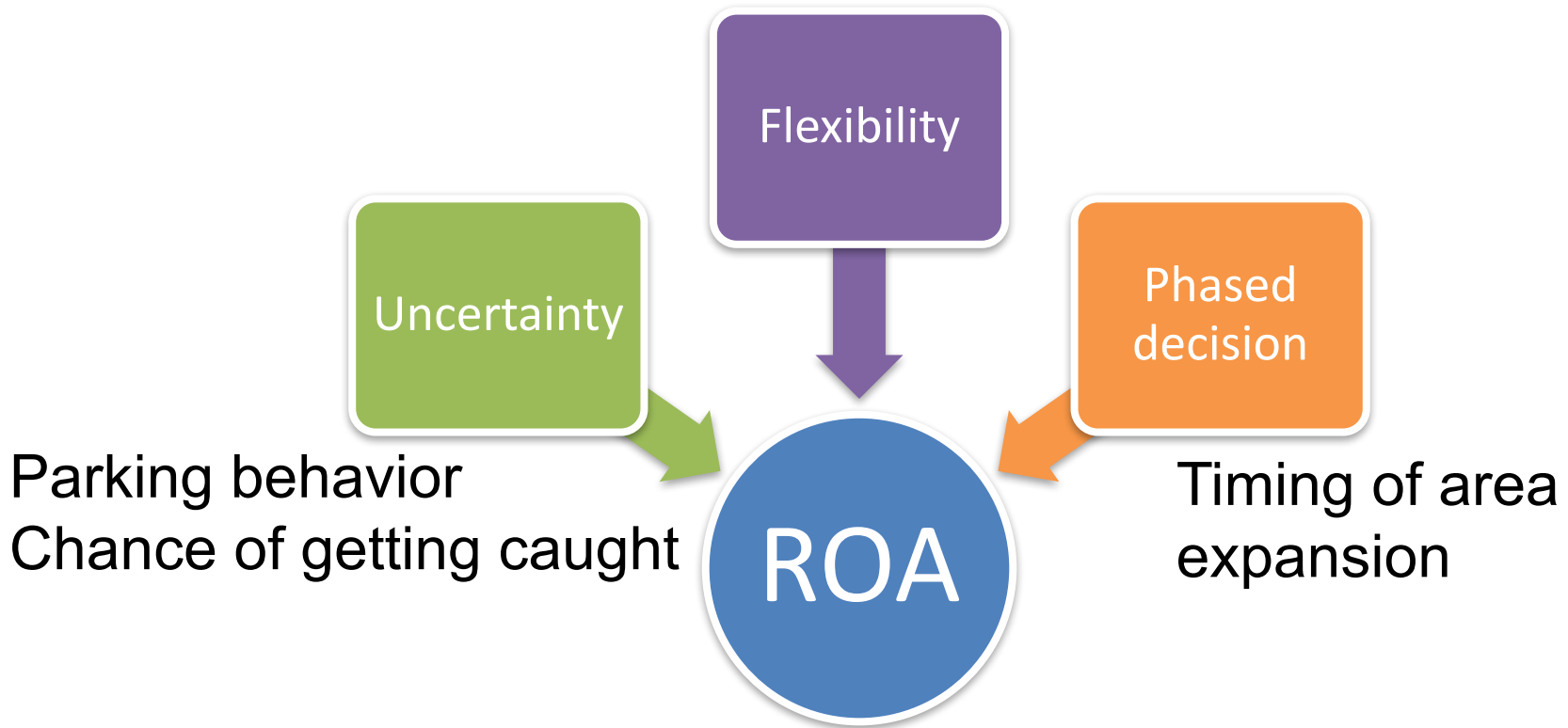
What is the optimal area  
to deploy the network?



# Three conditions for a ROA

for the case Which areas to deploy wireless sensor network

Area to deploy network in



# Uncertainty

Both technical and behavioral uncertainties

Chance of getting fined



Sensor lifetime



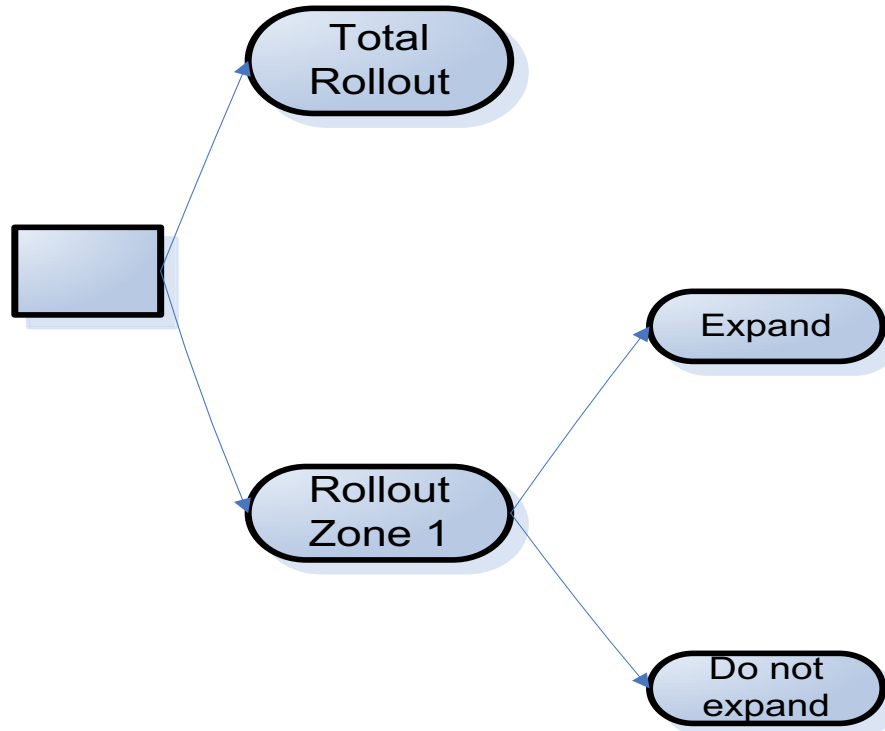
# Flexibility

Choose the zone to install the PSN in



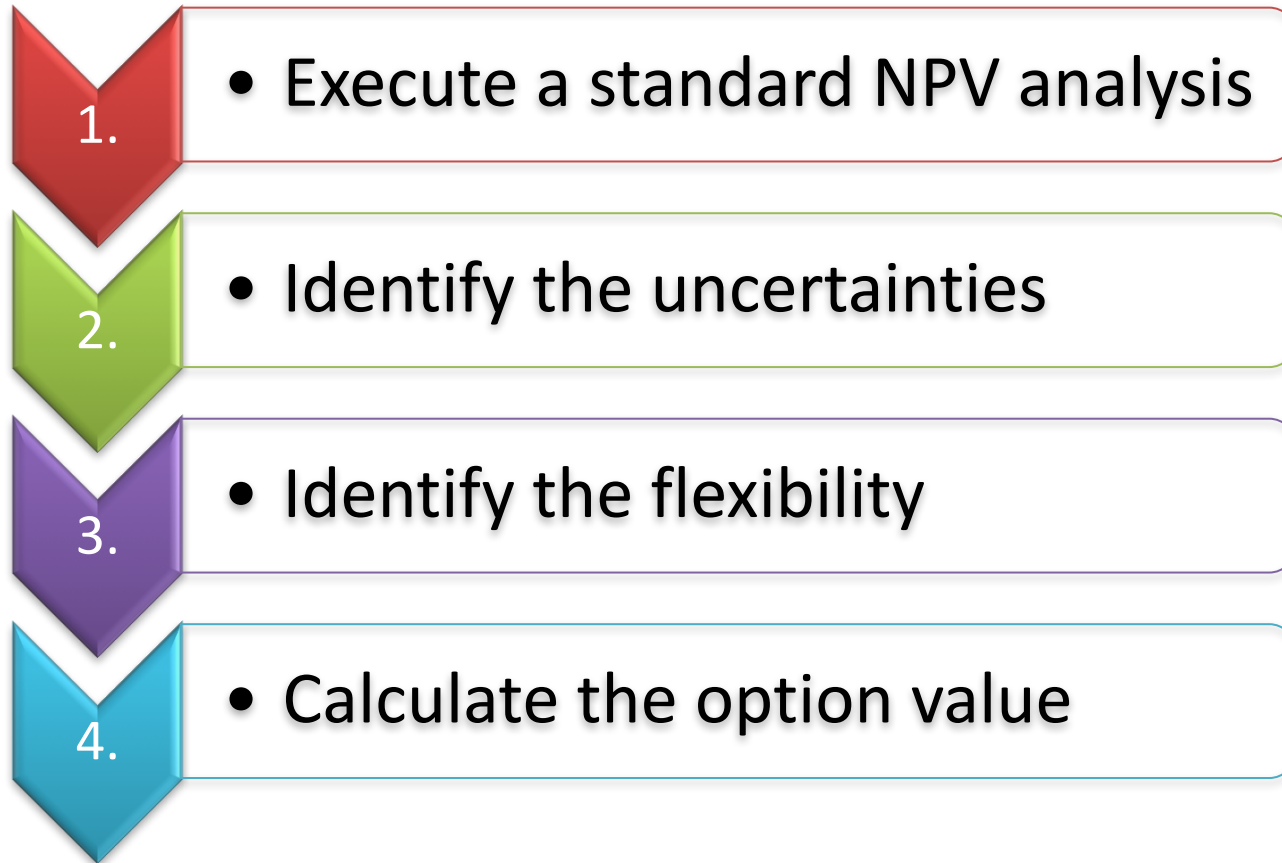
# Timing

Start small, decide later to scale



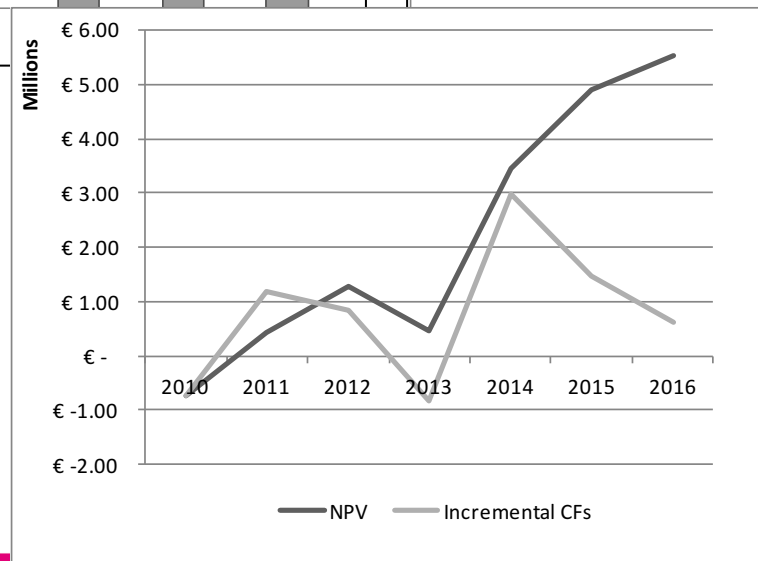
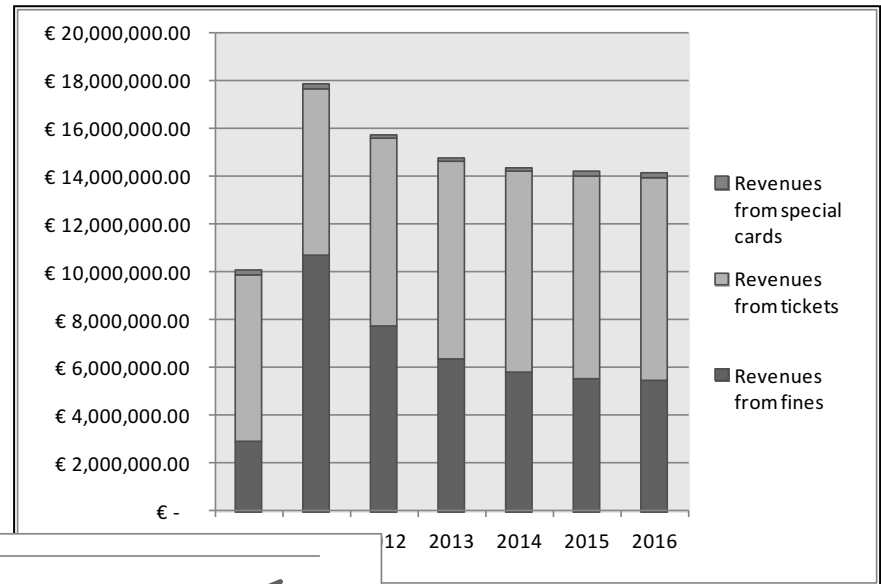
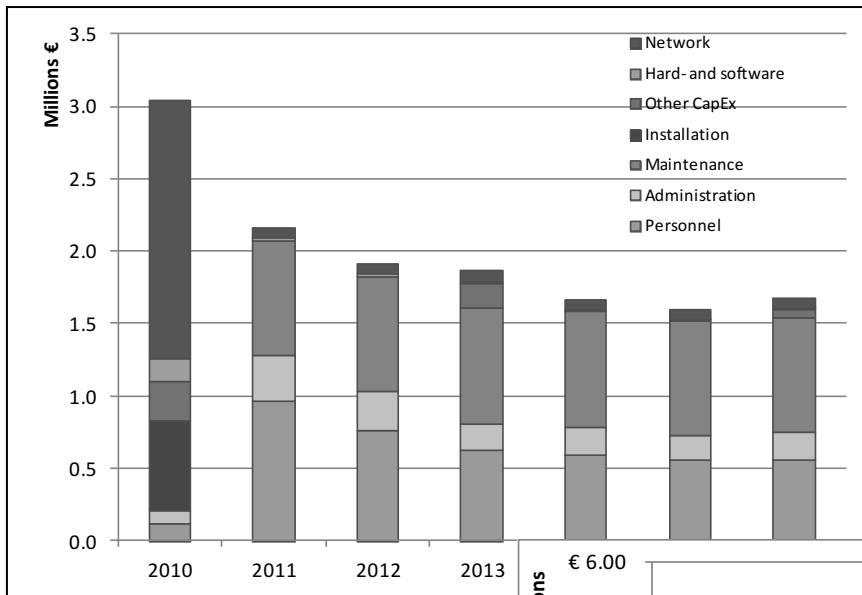


# Methodology for calculation option value based on simulations for this case



# 1. Execute a standard NPV analysis

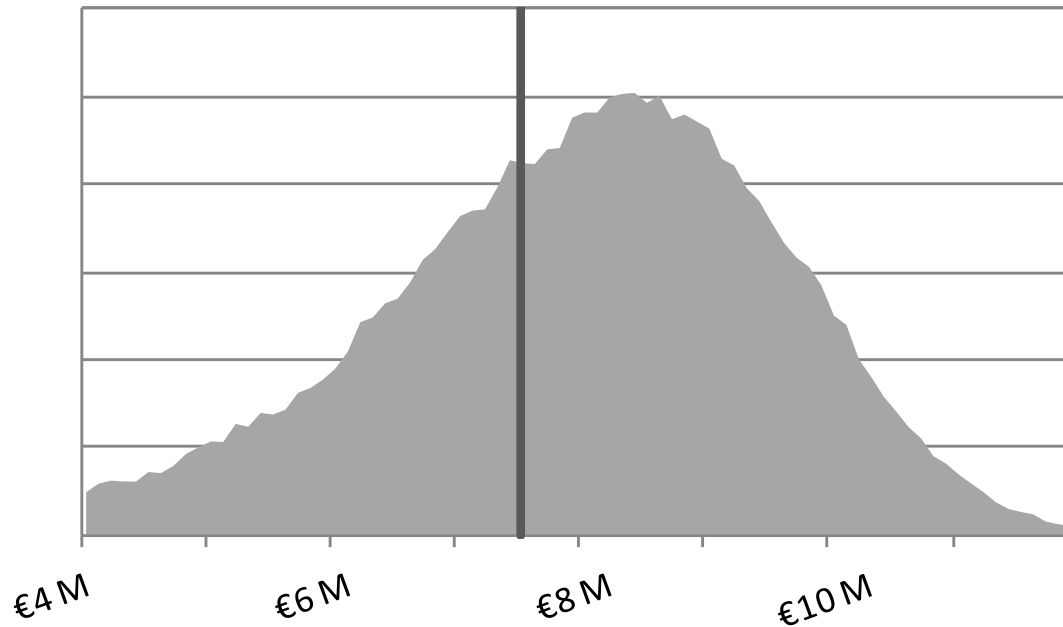
## Modeling costs and revenues



## 2. Identify the uncertainties

Input uncertainty impacts output

### Distribution NPV Standard



# 3. Identify the flexibility

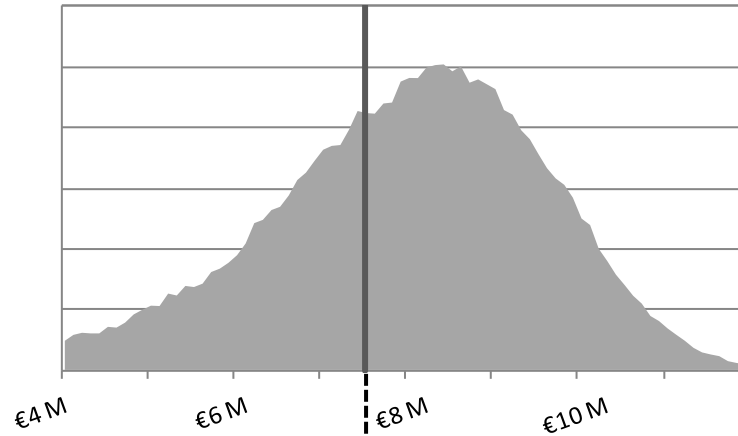
Different areas with different characteristics



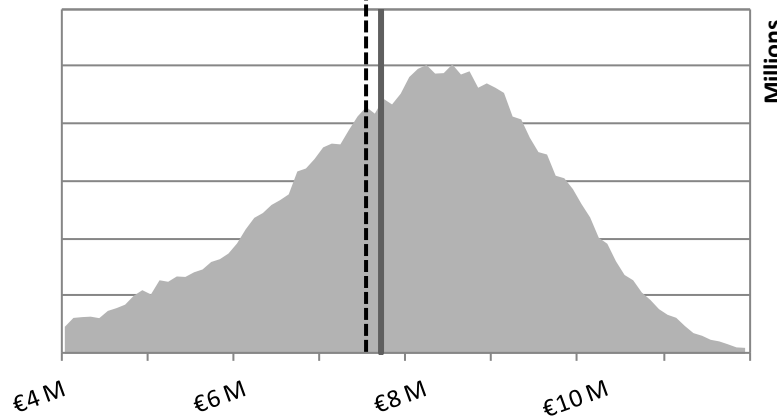
# 4. Calculate the option value

Option to expand positively impacts result

Distribution NPV Standard



Distribution NPV Options



# Case study summary

## Which areas to deploy wireless sensor network?

- Type of uncertainty (4 types of threats)
  - Operational – sensor lifetime
  - Strategic – impact on consumer behavior
- Option type (7S)
  - Scale up
- Calculation method: Monte Carlo simulation
- Case results
  - Scale option positively impacts case result

# Case study overview

where we applied ROA before

1. Make or lease fiber network?
2. Which areas to deploy wireless sensor network?
3. Optimal cabinet size for FTTcab roll-out?



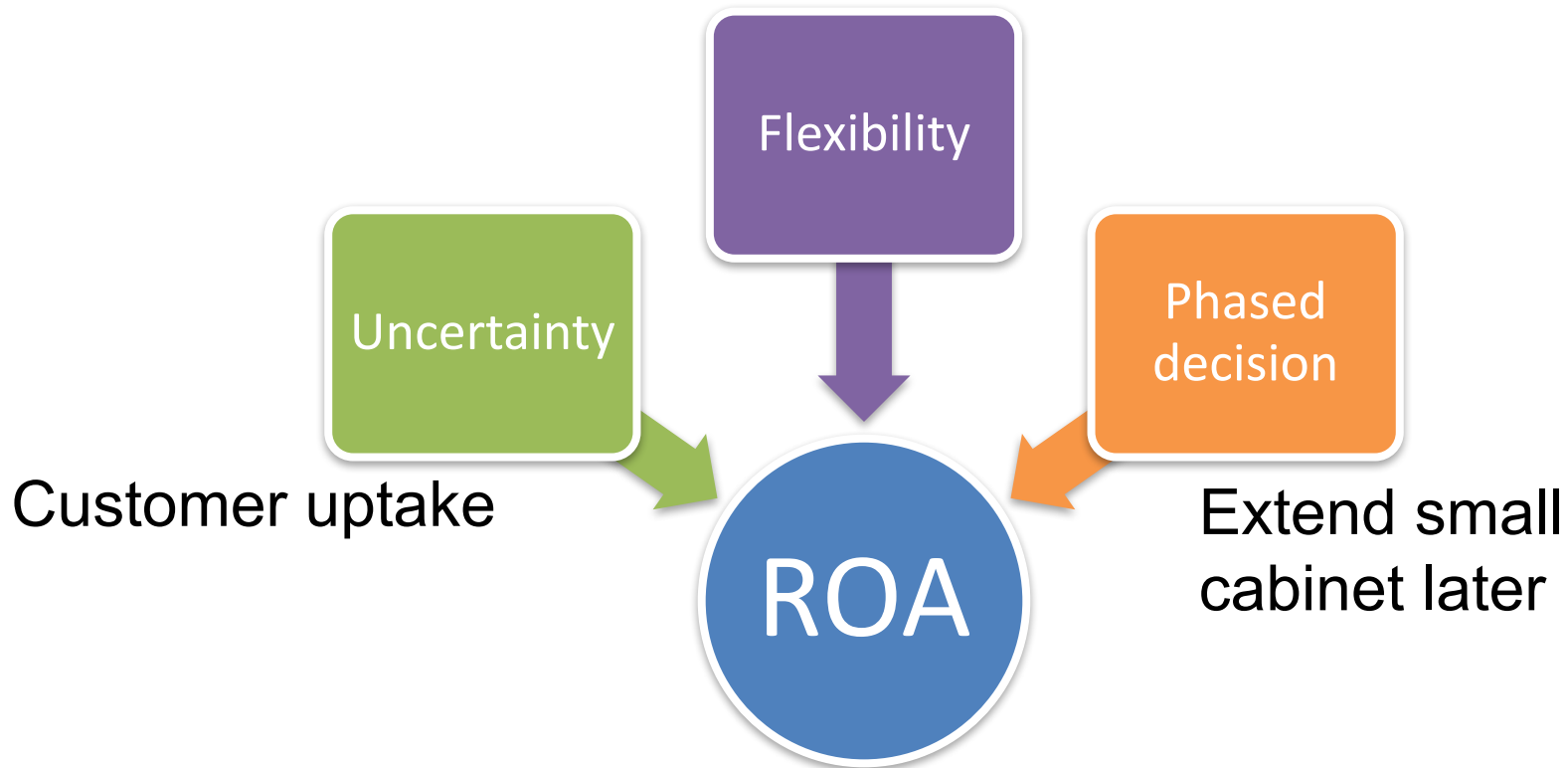
What is the optimal capacity to install in an FTTC rollout?



# Three conditions for a ROA

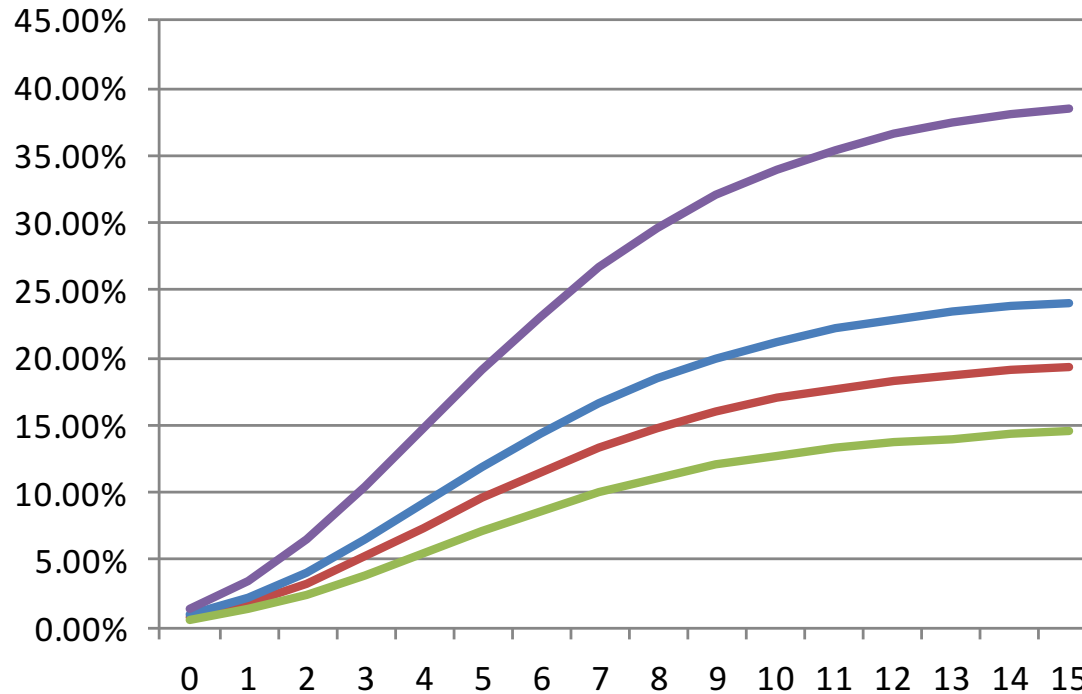
for the case Optimal cabinet size for FTTCab roll-out

Install large cabinet or small one with flexible extensions



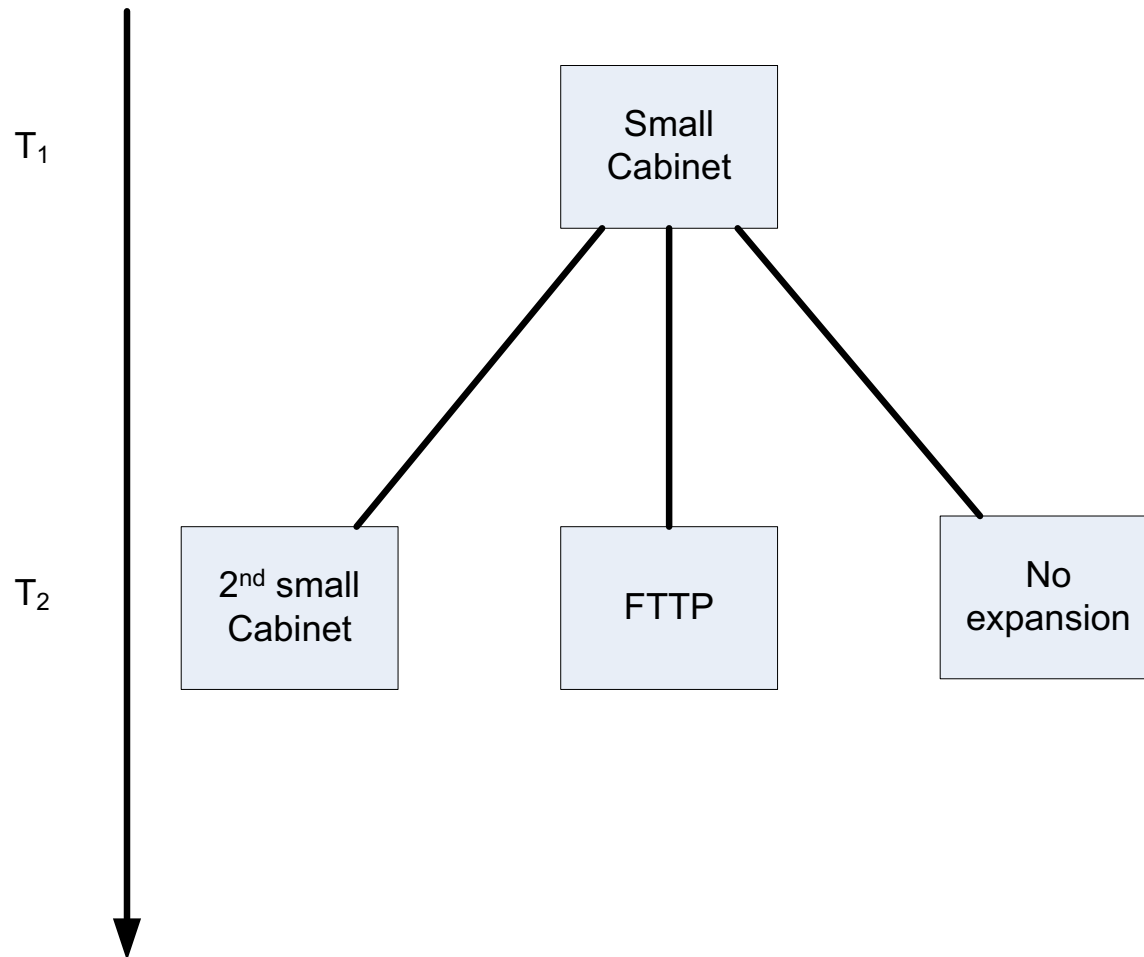
# Uncertainty

What is the expected customer uptake?



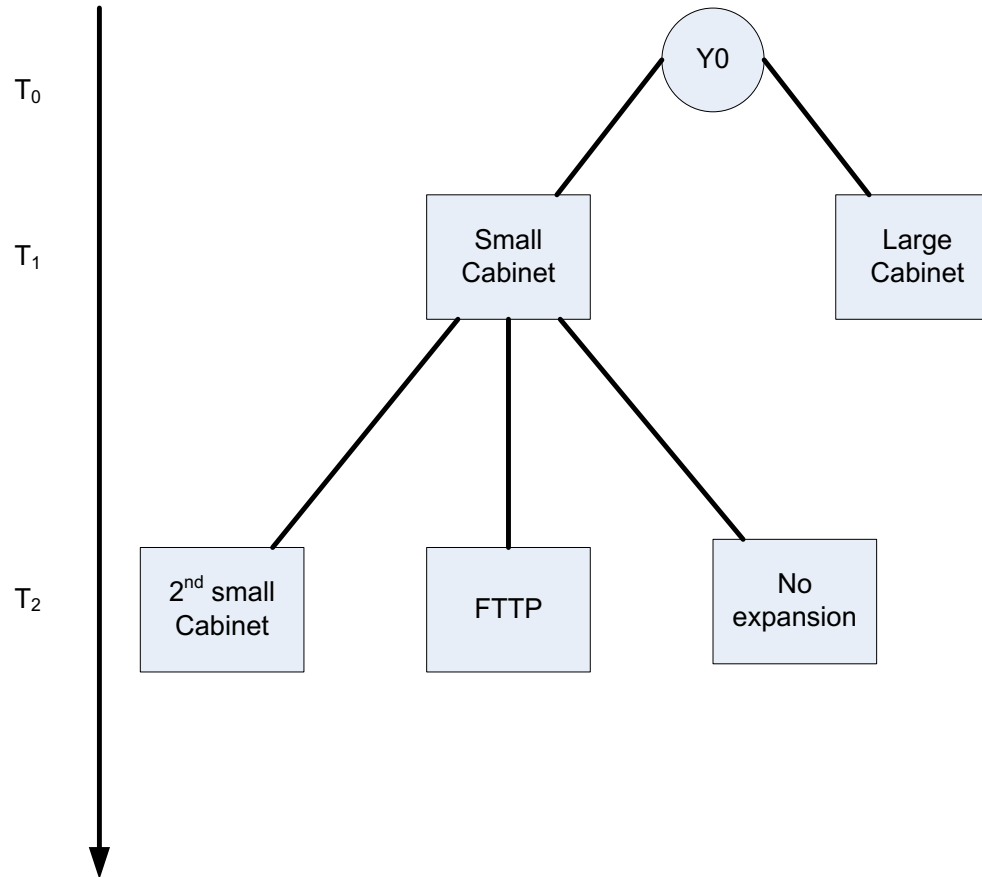
# Flexibility

## Different possible future migrations

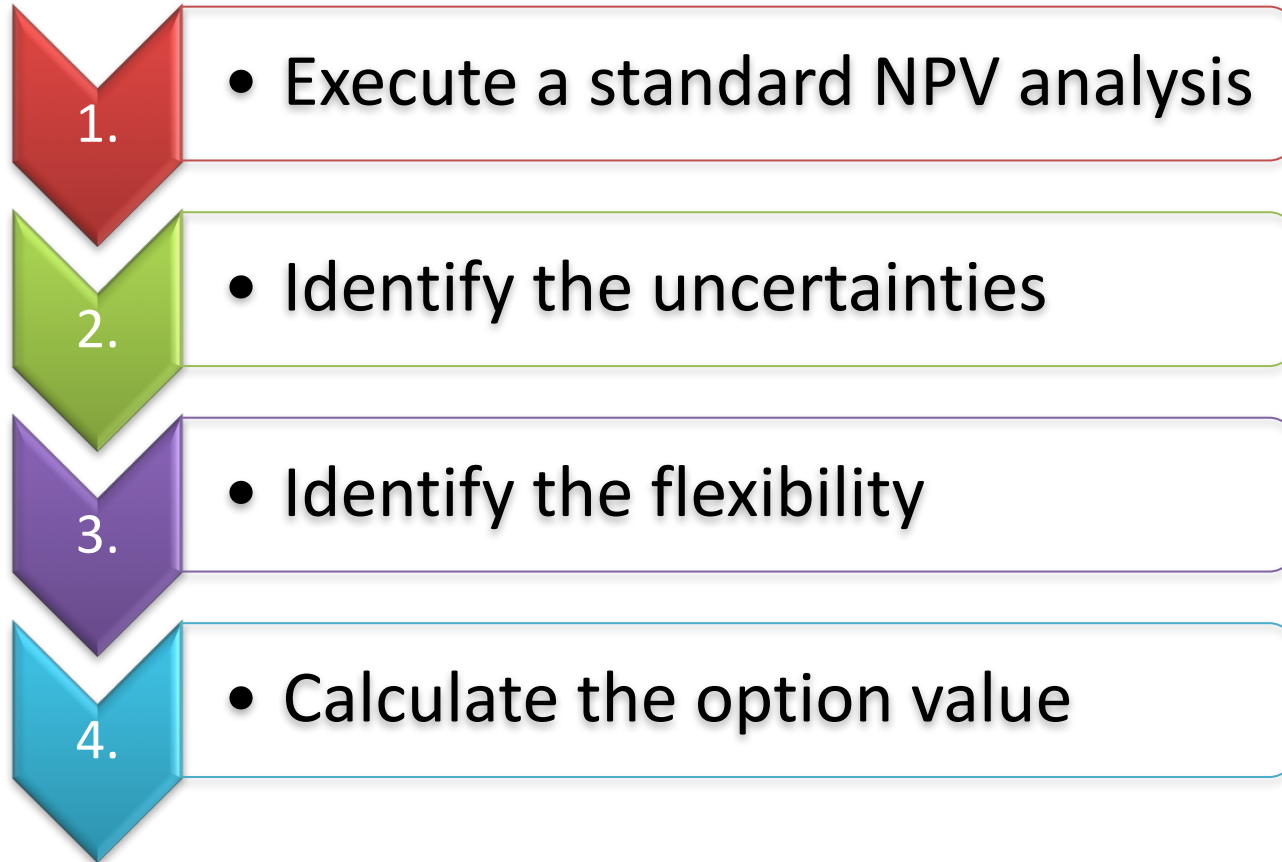


# Timing

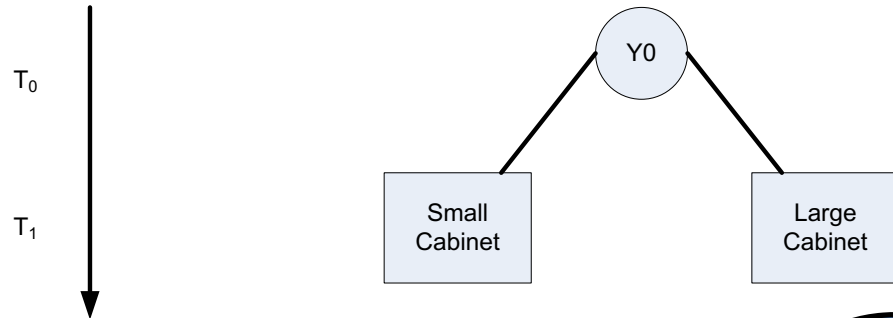
The migration choice can be postponed



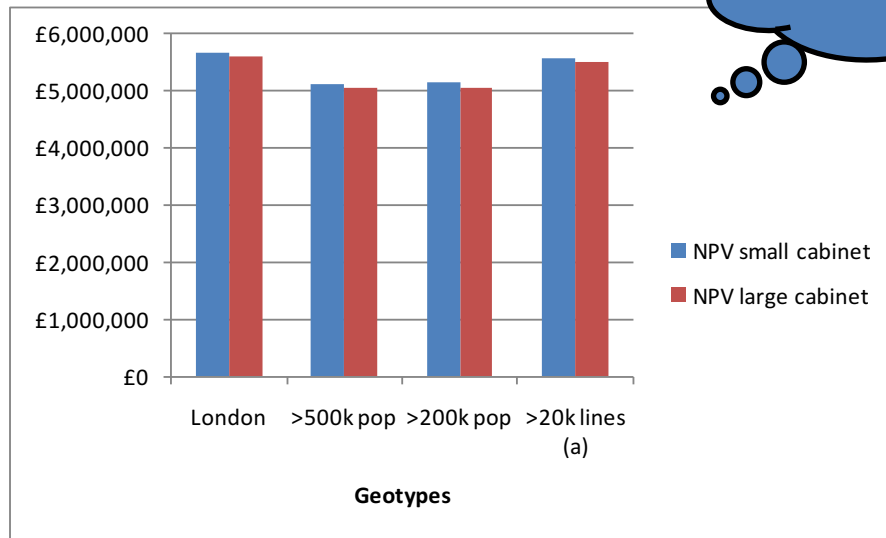
# Methodology for calculation option value based on simulations for this case



# 1. Execute a standard NPV analysis with expected adoption small cabinet is best

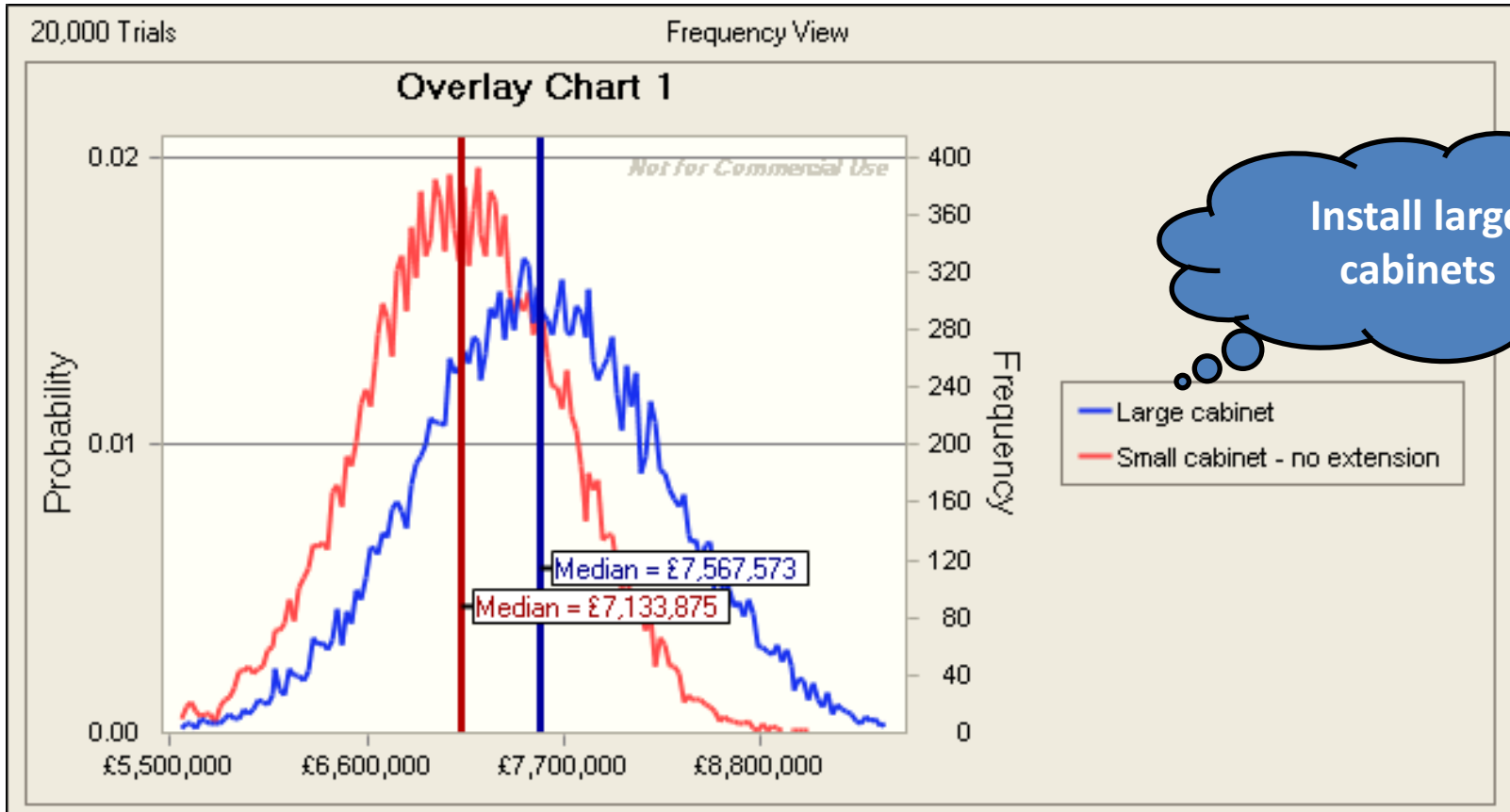


Install small cabinets



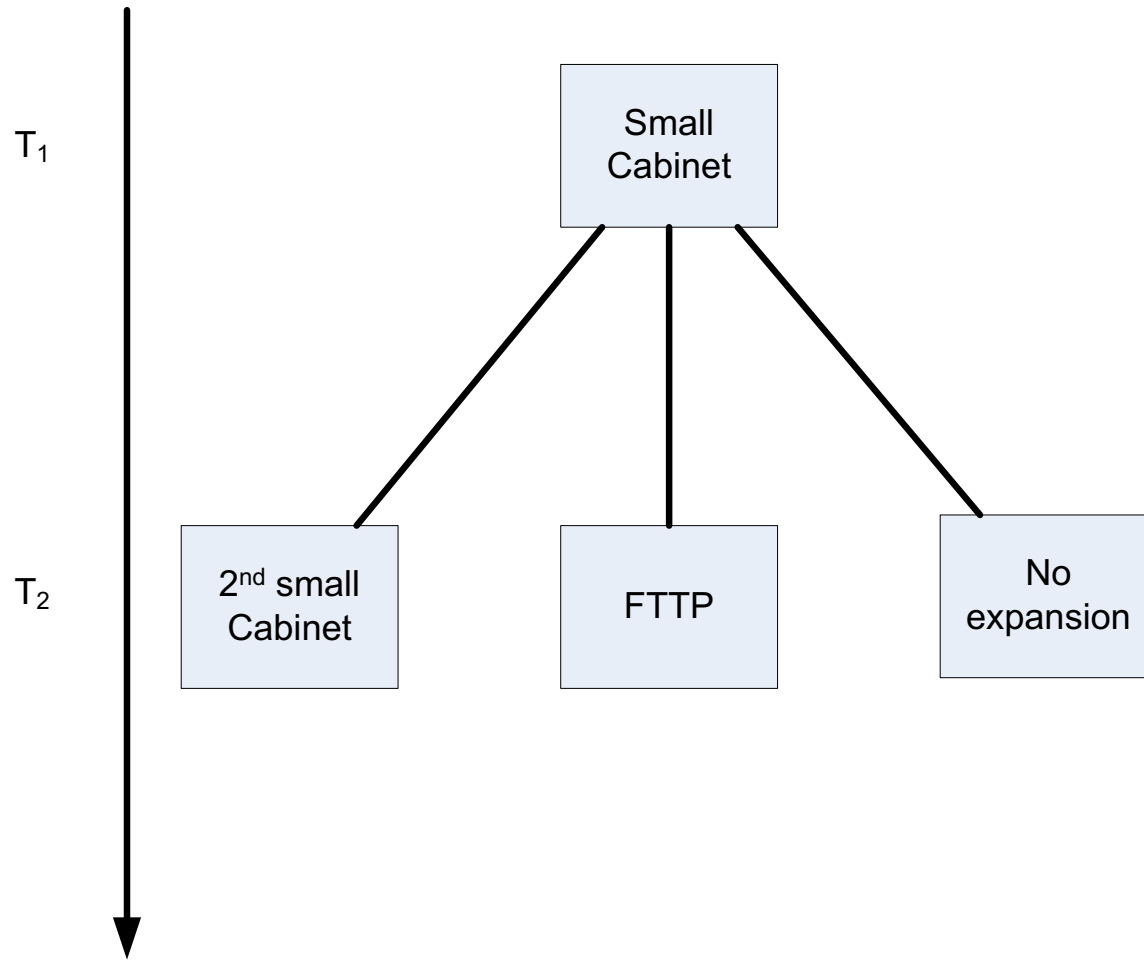
## 2. Identify the uncertainties

with range of adoptions, large cabinet is better on average



# 3. Identify the flexibility

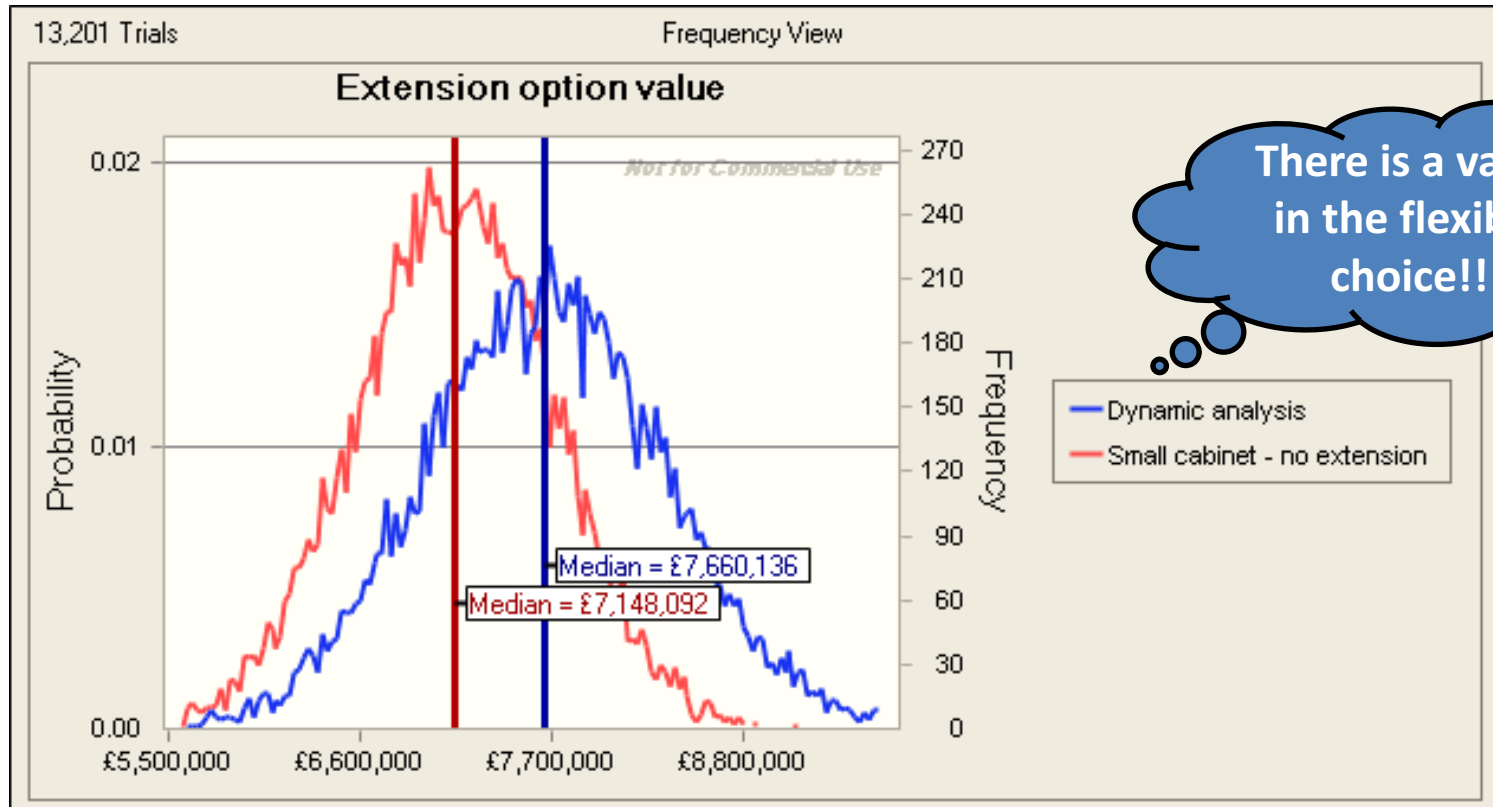
Different possible future migrations





# 4. Calculate the option value

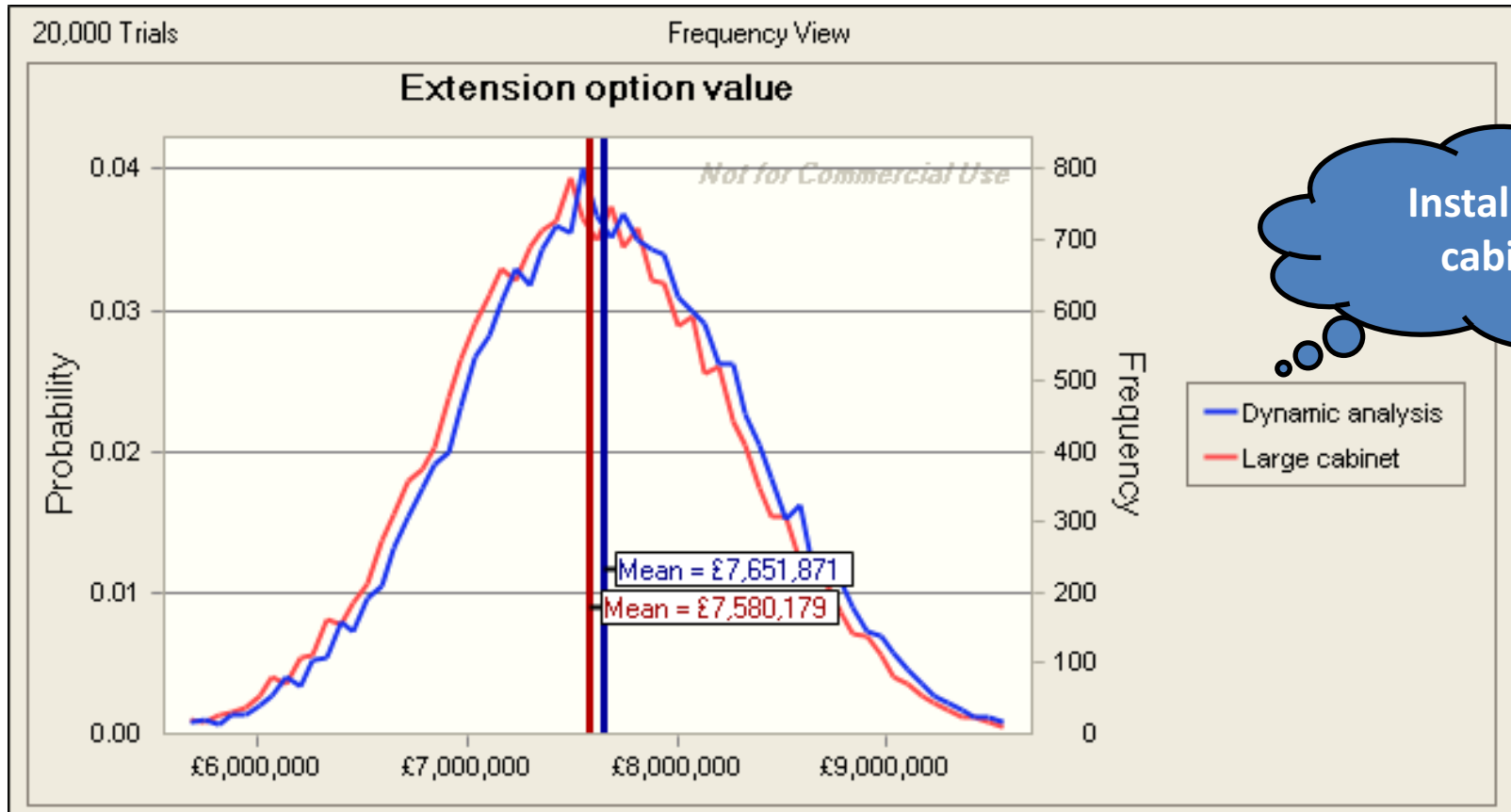
by comparing flexible path with static small cabinets



There is a value in the flexible choice!!

# 4. Calculate the option value

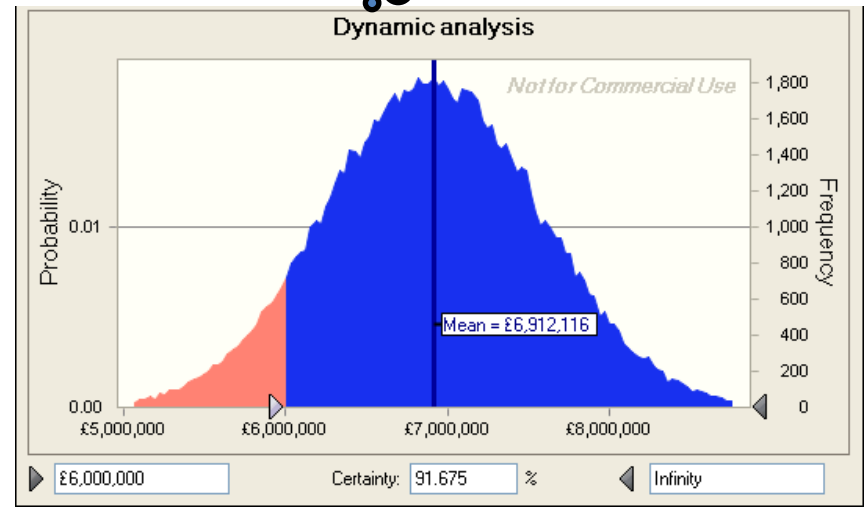
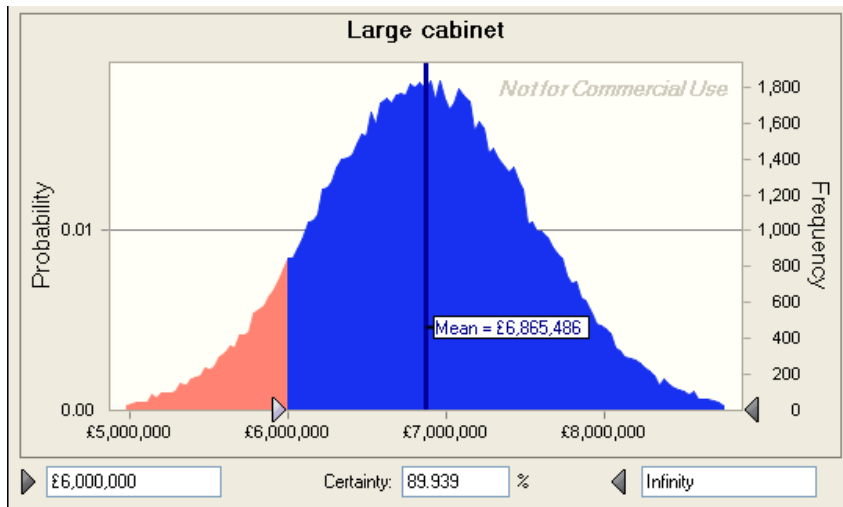
flexibility has more value than large cabinet installation



Install small cabinets

# ROA

shows that we can reduce the risk of negative outcome



10% risk: NPV < £6,000,000

8.3% risk: NPV < £6,000,000

# Case study summary

## Optimal cabinet size for FTTCab roll-out

- Type of uncertainty (4 types of threats)
  - Strategic – service uptake
  - Operational – re-usable ducts
- Option type (7S)
  - Scale up – install extra small cabinets
  - Switch up – migrate to FTTP
  - Scope up – offer enhanced services
- Calculation method: Monte Carlo simulation
- Case results
  - Small cabinets offer different options
  - These add significant value to change decision

# Extensions

Modeling competitive behavior

# Sources of uncertainty in telecom planning

allow to classify typical uncertain parameters

## Compliance Threats

- Regulatory change
- Corporate governance standards
- Radiation emission standards

## Operational Threats

- Technological change
- Traffic Intensity uncertainty
- Equipment Lifetime uncertainty

Telecom  
Uncertainty

## Strategic Threats

- Competition uncertainty
- Adoption uncertainty
- Willingness to pay evolution

## Financial Threats

- Component price evolution
- Evolution of borrowing capacity

# Competition uncertainty

How will competitors react to my strategy?

## Real options and strategies

- Scope: offering new services
- Scale: entering a new geographic market
- Switch: upgrading technology

Impacts the competitive equilibrium



# Game Theory

## Modeling competitive interaction

**Game theory** is “aimed at modeling situations in which decision makers have to make specific actions that have mutual, possibly conflicting, consequences” (Felegyhazi & Hubaux, 2006, p. 1).



# Solving the game

## Identifying the equilibria

- Nash
  - No player can gain a higher payoff by unilaterally changing his strategy
  - Competition equilibrium
- Pareto
  - No player can gain a higher payoff without reducing the payoff of another player
  - Social optimum

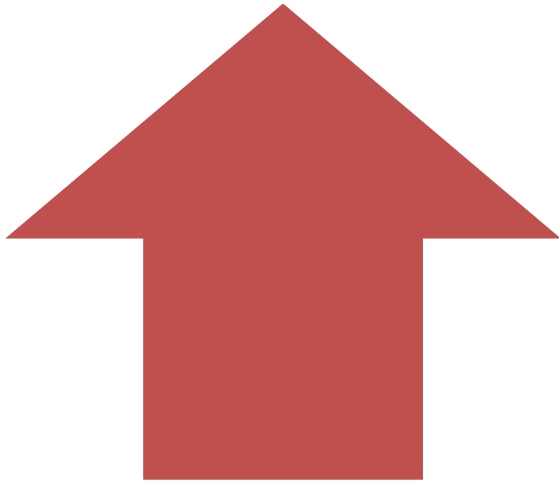
# Techno-economic Game Theory

		2. Municipality														
		enabler			independent			independent			independent			independent		
1. Commercial Wifi	3. 3G				18			19			20			21		
18	Scenario 1	0.33	1.81	0.52	-1.75	0.23	-0.17	-1.73	0.12	-0.10	-1.67	-0.04	0.07	-1.61	-0.26	0.23
	Scenario 2	0.18	1.68	0.87	-2.19	-0.15	0.40	-2.14	-0.26	0.43	-2.06	-0.44	0.55	-2.00	-0.70	0.69
	Scenario 3	<b>0.05</b>	<b>1.56</b>	<b>1.10</b>	-2.57	-0.51	0.80	-2.52	-0.62	0.85	-2.43	-0.82	0.96	-2.35	-1.10	1.05
	Scenario 4	0.21	1.70	0.74	-2.16	-0.10	0.26	-2.10	-0.21	0.30	-2.02	-0.40	0.41	-1.95	-0.64	0.52
19	Scenario 1	0.26	1.71	0.57	-1.77	0.36	-0.10	-1.74	0.26	-0.04	-1.67	0.08	0.13	-1.60	-0.13	0.29
	Scenario 2	0.12	1.59	0.91	-2.19	0.00	0.43	-2.14	-0.12	0.48	-2.06	-0.29	0.60	-1.98	-0.55	0.73
	Scenario 3	0.00	1.48	1.13	-2.61	-0.35	0.84	-2.54	-0.44	0.89	-2.44	-0.67	1.00	-2.36	-0.92	1.07
	Scenario 4	0.16	1.62	0.78	-2.13	0.03	0.30	-2.07	-0.07	0.34	-2.00	-0.25	0.46	-1.92	-0.49	0.57
20	Scenario 1	0.20	1.64	0.76	-1.83	0.58	0.07	-1.78	0.47	0.14	-1.69	0.30	0.30	-1.62	0.10	0.45
	Scenario 2	0.07	1.53	1.08	-2.28	0.22	0.57	-2.25	0.10	0.62	-2.15	-0.06	0.75	-2.06	-0.30	0.86
	Scenario 3	-0.05	1.42	1.27	-2.67	-0.12	0.98	-2.63	-0.22	1.02	-2.53	-0.44	1.08	-2.44	-0.68	1.17
	Scenario 4	0.11	1.57	0.93	-2.22	0.25	0.42	-2.18	0.15	0.47	-2.08	-0.02	0.58	-1.99	-0.26	0.71
21	Scenario 1	0.13	1.57	0.93	-1.94	0.79	0.25	-1.90	0.70	0.31	-1.80	0.53	0.47	-1.73	0.35	0.55
	Scenario 2	0.00	1.45	1.21	-2.40	0.44	0.72	-2.33	0.34	0.77	-2.22	0.16	0.88	-2.15	-0.07	1.01
	Scenario 3	-0.12	1.34	1.40	-2.82	0.13	1.07	-2.77	0.00	1.11	-2.65	-0.19	1.20	-2.53	-0.43	1.29
	Scenario 4	0.04	1.49	1.05	-2.32	0.48	0.55	-2.28	0.39	0.60	-2.18	0.22	0.73	-2.08	-0.01	0.84

- Modeling all strategic combinations
- Finding the equilibrium

# Real Options vs. Game Theory

Is it a strategy or an option?



## Real Options

- Managerial flexibility
- Counter uncertainty
- Competition as external factor



## Game Theory

- Dynamic interaction between competitors
- Competition as internal factor

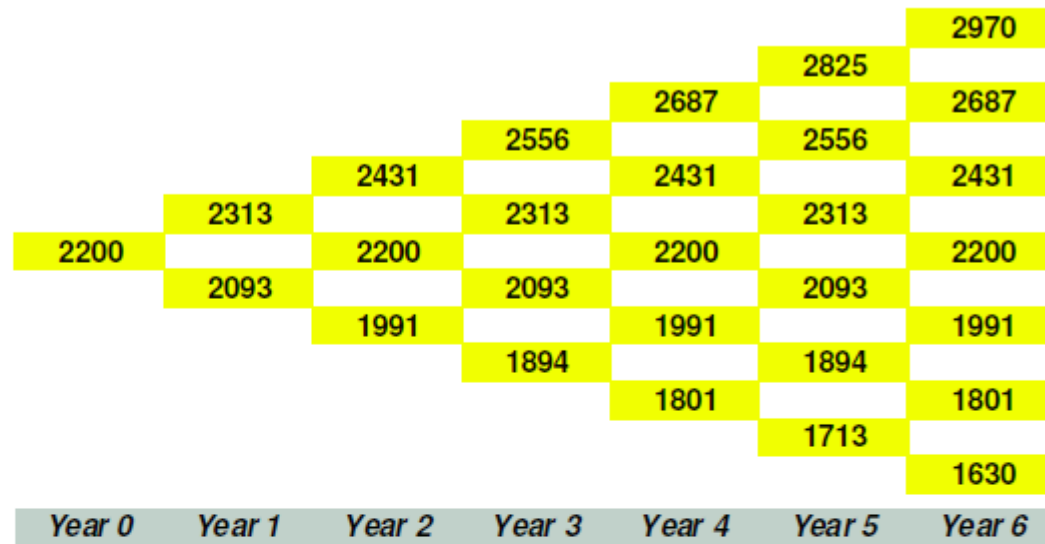
# Option games

## Combining Real Options and Game Theory

	Firm 2		
Firm 1		Invest	Wait
	Invest		
	Wait		

### Demand evolution

Per year in thousands of tons



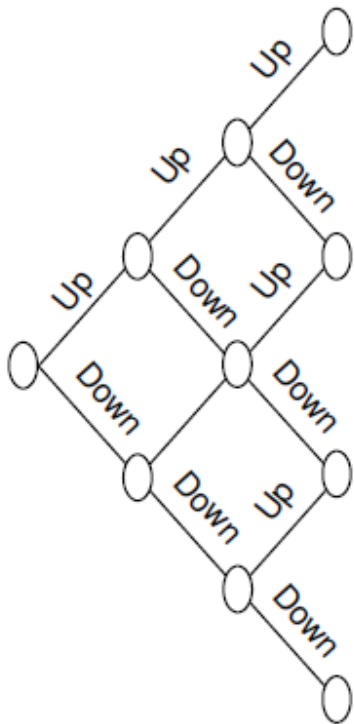
McKinsey, "Option Games": Filling the hole in the valuation toolkit for strategic investment, available online

# Option Games

## Combining Real Options and Games

Evolution of demand to Y3

Y0 Y1 Y2 Y3



		CompCo	
		Invest	Abandon
MineCo	Invest	(143, 71)	(410, 0)
	Abandon	(0, 405)	(0, 0)

Probability of reaching node

3%

Expected value of payoffs in year 3  
U.S. \$ millions

- Dominant strategy
- MineCo = 143
- CompCo = 71

		CompCo	
		Invest	Abandon
MineCo	Invest	(-2, -114)	(87, 0)
	Abandon	(0, 71)	(0, 0)

19%

- Mixed strategy (average)
- MineCo = 43.5
- CompCo = 35.5

		CompCo	
		Invest	Abandon
MineCo	Invest	(-45, -169)	(-11, 0)
	Abandon	(0, -102)	(0, 0)

44%

- Dominant strategy
- MineCo =  $\emptyset$
- CompCo =  $\emptyset$

		CompCo	
		Invest	Abandon
MineCo	Invest	(-57, -185)	(-55, 0)
	Abandon	(0, -158)	(0, 0)

34%

- Dominant strategy
- MineCo =  $\emptyset$
- CompCo =  $\emptyset$

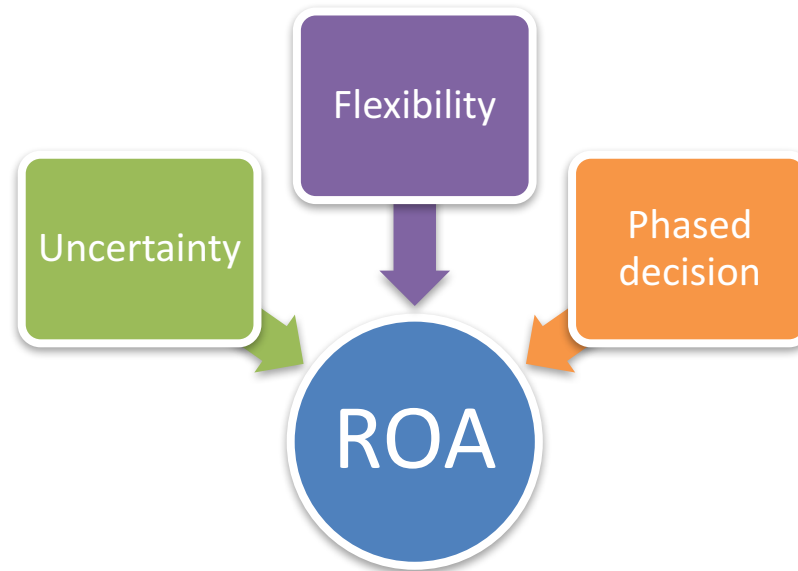
# Conclusions

# Summary

- ROA is a way to formalize a good practice
  - “I choose this solution because it is more flexible”

# Summary

- ROA is a way to formalize a good practice
  - “I choose this solution because it is more flexible”
- There are 3 essential conditions





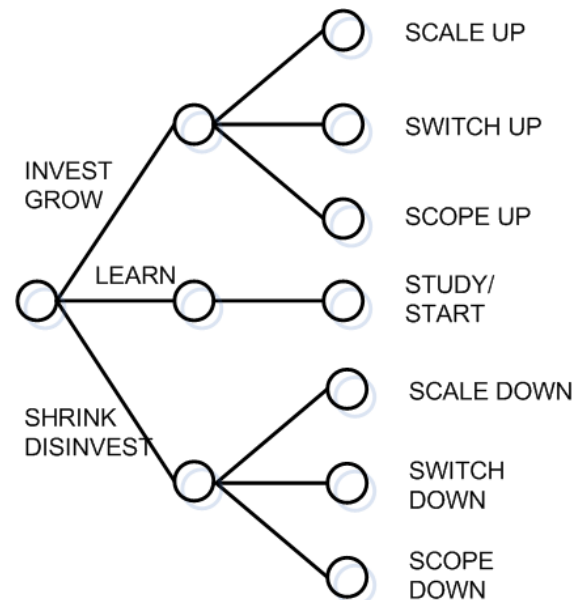
# Summary

- ROA is a way to formalize a good practice
  - “I choose this solution because it is more flexible”
- There are 3 essential conditions
- Find all uncertain parameters and model them



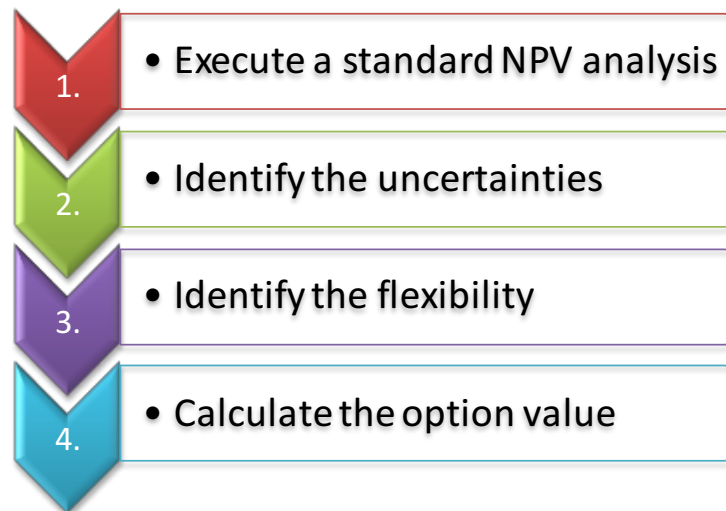
# Summary

- ROA is a way to formalize a good practice
  - “I choose this solution because it is more flexible”
- There are 3 essential conditions
- Find all uncertain parameters and model them
- Describe all flexibility in the project



# Summary

- ROA is a way to formalize a good practice
  - “I choose this solution because it is more flexible”
- There are 3 essential conditions
- Find all uncertain parameters and model them
- Describe all flexibility in the project
- Quantify the value of these options



# References

# Real options & sensitivity analysis methodology

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- L. Trigeorgis (Ed.), "Real Options in Capital Investment: Models, Strategies, and Applications", Praeger, 1995.
- J. C. Hull, "Options, futures, and other derivatives", 5de ed., Pearson Education, 2003.
- J. Alleman, "A new view on telecommunications economics", Telecommunications Policy, 2002, vol. 26, pp. 87-92. – not about RO???
- W. De Maeseneire, "The real options approach to strategic capital budgeting and company valuation", ISBN: 2-8044-2318-2, Financiële Cahiers, Larcier, 2006.
- Saltelly et al., "Global Sensitivity Analysis, The Primer", ISBN: 978-0-470-05997-5, John Wiley & Sons Ltd, 2008.

# Application of real option in cases

- Mathieu Tahon, Sofie Verbrugge, Peter J. Willis, Paul Botham, Didier Colle, Mario Pickavet, Piet Demeester, *Migration to Next Generation Access Networks: a Real Option Approach*, Real Option Conference 2012, London, UK, June 2012
- Mathieu Tahon, Sofie Verbrugge, Bart Lannoo, Jan Van Ooteghem, Pieter De Mil, Mario Pickavet, Piet Demeester, *Parking Sensor Network: Economic Feasibility Study of Parking Sensors in a City Environment*, CTTE 2010, the 9th Conference of Telecommunication, Media and Internet Techno-Economics, Ghent - Belgium, June 7-9, 2010
- S. Verbrugge, D. Colle, W. De Maeseneire, P. Demeester, *Valuing the flexibility in fiber deployment network planning: an application to a Belgian network*, 12th International Conference on Real Options: Theory meets Practice, Rio de Janeiro, Brasil, 9-12 July 2008
- S. Verbrugge, D. Colle, M. Pickavet, P. Demeester, "Cost versus flexibility of different capacity leasing approaches on the optical network layer", published in Lecture Notes in Computer Science, proceedings of ONDM2007, the 11th International IFIP TC6 Conference on Optical Network Design and Modeling, Vol. 4534 , May 2007.

# Application of real option in cases

- Stragier, J., Seys, C., Evens, T., Evenepoel, S., Vanooteghem, J., & Casier, K. (2012). A priori forecasting of FTTH uptake : coupling segmentation forecasting to timing forecasting. *11th Conference of Telecommunication, Media and Internet Techno-Economics, Proceedings*. Presented at the 11th Conference of Telecommunication, Media and Internet Techno-Economics (CTTE - 2012), Athens, Greece.
- Evenepoel, Simon, Jan Van Ooteghem, Sofie Verbrugge, Bart Lannoo, Didier Colle, and Mario Pickavet. 2012. "Can crowdsourced WiFi be a viable strategy to provide open internet access in a municipality?" In *The 51st International FITCE (Federation of Telecommunications Engineers of the European Community) Congress, Media and Internet Techno-Economics, Proceedings*, Poznan, Poland.

# Tools

- Crystal Ball

<http://www.oracle.com/us/products/applications/crystalball/index.html>

- TESS – java implementation

Marlies Van der Wee, Koen Casier, Karel Bauters, Sofie Verbrugge, Didier Colle, Mario Pickavet, *A modular and hierarchically structured techno-economic model for FTTH deployments. Comparison of technology and equipment placement as function of population density and number of flexibility point*, ONDM 2012.



Questions?

**Mathieu Tahon**  
**Sofie Verbrugge**  
**Simon Evenepoel**

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